## A Configuration Based Pumped-storage Hydro Unit Model in MISO Day-ahead Market

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# Outline

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Case Study

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# Pumped-Storage Hydro Unit (PSHU)

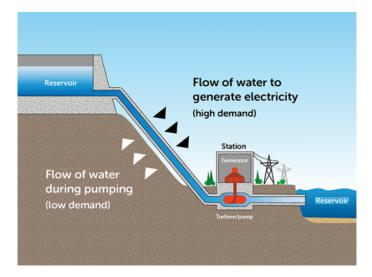


Figure: A Pumped-Storage Hydro Unit [Kenning, 2017]

#### Background

# **Storage Technologies and Applications**

#### Table: Storage Technologies and Applications [Barton et al., 2004]

| Full Power<br>Duration<br>of Storage | Applications<br>of Storage  | Compressed Air<br>Energy Storage<br>(CAES) | Pumped-storage<br>Hydro | Battery<br>Technologies | Flywheel |
|--------------------------------------|---|--|-------------------------|-------------------------|----------|
| 3 Days                               | Weekly smoothing of loads<br>and most weather variations                                  | Y  | Y                       |                         |          |
| 8 Hours                              | Daily load cycle, PV, Wind,<br>transmission line repair                                   | Y  | Y                       | Y                       |          |
| 2 Hours                              | Peak load lopping,<br>standing reserve,<br>wind power smoothing                           | Y  | Y                       | Y                       |          |
| 20 Minutes                           | Spinning reserve,<br>wind power smoothing,<br>clouds on PV                                | Y  | Y                       | Y                       | Y        |
| 3 Minutes                            | Spinning reserve,<br>wind power smoothing of gusts  |  | Y                       | Y                       | Y        |
| 20 Seconds                           | Line or local faults,<br>voltage and frequency control,<br>governor controlled generation |  |                         | Y                       | Y        |

# **Motivation**

- Pumped-storage hydro unit (PSHU) can provide a wide range of services and such services are substantially important to the system operation.
- Under current MISO practice, pumped-storage hydro unit owners specify pump/generate periods and offer costs/prices.
- As a market participant with limited information, PSHUs' forecast may be poor.
- PSHUs' decisions are **sub-optimal** to the system welfare.
- The pump/generate decisions made based on the forecasts may impair profits.
- The first step is to include the PSHUs more fully into MISO's **day-ahead market** clearing process solving unit commitment (UC) and economic dispatch (ED) problems.

# **Literature Review**

- Models of the operation of a PSHU with continuous variables.
  - Two continuous variables for a pump and a generator and state of charge constraints [Castronuovo and Lopes, 2004] [Duque et al., 2011].
  - A variable is introduced to represent the energy spilled from the pumped-storage hydro system [Brown et al., 2008].
  - A single variable represent generating (positive) and pumping (negative) [Ni et al., 2004].
- Models of the operation of the PSHU with integer variables.
  - An integer variable indicates the total number of turbines that are in pumping mode among the N identical turbines [Garcia-Gonzalez et al., 2008].
  - Binary variables (pump/generate) are introduced to each of the the PSHU in the system [Jiang et al., 2012].
  - Three modes, pumping, generating and idle are modeled for each of the PSHUs [Khodayar et al., 2013].

## **Conclusion of the Literature**

- Pumped-storage hydro model has been studied for a stand alone system [Ma et al., 2015] or a market participant [Ma et al., 2014].
- The model of a PSHU in the day-ahead unit commitment problem remained obscure.
- Three modes are necessary for day-ahead market schedules, so there should be an "alloff" or "offline" mode specified.
- There is typically a minimum output for the generating mode.
- Pump is typically block loaded or with minimum pumping limit.
- Constantly charging or discharging the pumped-storage hydro unit is not always the best strategy for system operation.

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# **Operation Modes**

• Configuration based model for combined cycle gas unit [Chen and Wang, 2017] is applied.

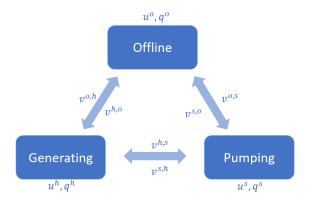


Figure: Mode transition diagram of a PSHU in two consecutive time intervals.

- Let  $q^h$  be the output of the generate mode and let  $q^s$  be the output of the pump mode.
- Let  $\boldsymbol{u}$  be the unit commitment of each mode and let  $\boldsymbol{v}$  be the transition between modes. Formulation

### **Formulation**

The system operation costs are shown in (1).

$$\min_{q,u} \sum_{g \in G_{sh}} \sum_{t \in T} f_{g,t}^h - C_{g,t}^s q_{g,t}^s + \sum_{g \in G} \sum_{t \in T} C(q_{g,t})$$
(1)

Energy balance constraint is shown in (2).

$$\sum_{g \in G} q_{g,t} + \sum_{g \in G_{sh}} q_{g,t}^h = D_t + \sum_{g \in G_{sh}} q_{g,t}^s \ \forall t \in T$$

$$\tag{2}$$

The output of a PSHU  $q_{g,t}^h$  and  $q_{g,t}^s$  are constrained by their capacities and the amount of energy stored in the reservoir  $e_{r,t}$ .

$$\underline{Q}_{g}^{h}u_{g,t}^{h} \leq q_{g,t}^{h} \ \forall g \in G_{sh} \ \forall t \in T$$
(3)

$$q_{g,t}^{h} \leq \overline{Q}_{g}^{h} u_{g,t}^{h} \quad q_{g,t}^{h} \leq \eta_{g}^{h} e_{r,t} \quad \forall g \in G_{sh} \quad \forall r \in R \quad \forall t \in T$$

$$\tag{4}$$

$$\underline{Q}_{g}^{s} u_{gt}^{s} \leq q_{g,t}^{s} \leq u_{g,t}^{s} \overline{Q}_{g}^{s} \quad \forall g \in G_{sh} \quad \forall t \in T$$
(5)

### Unit Commitment and Transition Logic [Dai et al., 2018]

The first constraint guarantees that the configurations are mutually exclusive:

$$\sum_{y \in \mathcal{Y}} u_{g,t}^y = 1, \, \forall g, \, \forall t.$$
(6)

where  ${\mathcal Y}$  is the set of modes in a pumped storage unit.

The second constraint links on/off variables with transition variables:

$$u_{g,t}^{y} - u_{g,t-1}^{y} = \sum_{\substack{y' \in \mathcal{M}^{T,y} \\ \text{Entering State } y \text{ at } t}} v_{g,t}^{y'y} - \sum_{\substack{y' \in \mathcal{M}^{F,y} \\ \text{Leaving State } y \text{ at } t}} v_{g,t}^{yy'}, \forall g, \forall t, \forall y.$$

$$(7)$$

where  $\mathcal{M}^{F,y}$  is the set of reachable configurations from y, and  $\mathcal{M}^{T,y}$  is the set of reachable configurations to y.

At most one transition per interval:

$$\sum_{y' \in \mathcal{M}} v_{g,t}^{yy'} \le 1, \, \forall g, \forall t.$$
(8)

where  ${\cal M}$  is the set of all ordered pairs of states correspond to feasible transitions.

y

#### Storage Energy Balance and State of Charge

$$e_{r,t+1} = e_{r,t} + \sum_{g \in G_{sh,r}} \eta_g^s q_{g,t}^s - \sum_{g \in G_{sh,r}} \frac{q_{g,t}^h}{\eta_g^h} \quad \forall r \in R \quad \forall t \in T$$

$$\tag{9}$$

$$e_{r,1} = E_{r,1} \quad \forall r \in R \tag{10}$$

$$e_{r,T+1} = E_{r,T+1} \quad \forall r \in R \tag{11}$$

$$\underline{E_r} \le e_{r,t} \le \overline{E_r} \quad \forall r \in R \quad \forall t \in T$$
(12)

where  $\eta_g^h$  and  $\eta_g^s$  are the efficiencies of generating and pumping indicating energy losses at each mode. Energy stored in the reservoir r at time t is  $e_{r,t}$  and it is constrained by the state of charges and the capacity of the reservoir [Castronuovo and Lopes, 2004]-[Garcia-Gonzalez et al., 2008].

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# Case Study of Two PSHU Turbines

- Day-ahead UC and ED problems are solved for a 24 hours net-load scenario.
- Reserve requirements ignored.
- Ramp constraints ignored.
- Transmission security constraints ignored.
- The PSHU has two turbines that share a same reservoir. Pump is block loaded.
- Maintenance and operation costs of the PSHU is ignored. Profits = income from generating mode price paid for pumping mode.

| Unit Mode        | Cost/Price<br>\$ | $\frac{\underline{q}^m}{MW}$ | $\overline{q}^m$ MW | $\eta_g^m$ |
|------------------|------------------|------------------------------|---------------------|------------|
| 1: PSHU1 Pump    | 24               | 200                          | 200                 | 0.9        |
| 1: PSHU1 Gen     | 26               | 100                          | 200                 | 0.9        |
| 2: PSHU2 Pump    | 24               | 200                          | 200                 | 0.9        |
| 2: PSHU2 Gen     | 26               | 100                          | 200                 | 0.9        |
| 3: Thermal Gen 1 | 30               | 0                            | 600                 | NA         |
| 4: Thermal Gen 2 | 20               | 0                            | 300                 | NA         |
| 5: Thermal Gen 3 | 15               | 0                            | 500                 | NA         |

Table: Units

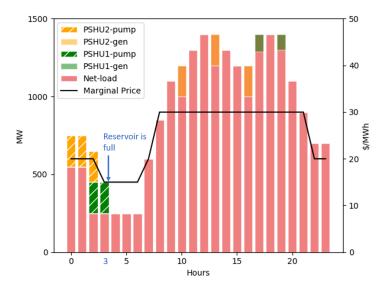
### **Example to Illustrate Current Practice in MISO**

- PSHU owners offer opportunity costs for generation mode and bid prices for pump mode.
- State of charges of the reservoir are not enforced.
- The PSHU owner determines the pump/generate window.
- Pump window: 0 6 AM; Generate window: 7 AM 11 PM.
- Maximum Daily Generation constraint is applied on PSHU for the generate mode.
- Although state of charges are not represented in the clearing algorithm, the PSHU must stop pumping when the reservoir is full.

| Reservoir | $\frac{E_r}{MW}$ h | $\overline{E_r}$ MWh | $E_{r,1}$ MWh | $E_{r,T+1}$ MWh |
|-----------|--------------------|----------------------|---------------|-----------------|
| Reservoir | 1000               | 3500                 | 2600          | 2600            |

#### Table: Reservoir

## **Economic Dispatch Results with Current Practice**



• Net-load = system load - renewable energy (e.g. solar) not including PSHU outputs.

## **Data for Proposed Model**

| Unit Mode        | Cost/Price | $q^m$ | $\overline{q}^m$ | $\eta_q^m$ |
|------------------|------------|-------|------------------|------------|
| Unit Mode        | \$         | ΜW    | MW               | 5          |
| 1: PSHU1 Pump    | 0          | 200   | 200              | 0.9        |
| 1: PSHU1 Gen     | 0          | 100   | 200              | 0.9        |
| 2: PSHU2 Pump    | 0          | 200   | 200              | 0.9        |
| 2: PSHU2 Gen     | 0          | 100   | 200              | 0.9        |
| 3: Thermal Gen 1 | 30         | 0     | 600              | NA         |
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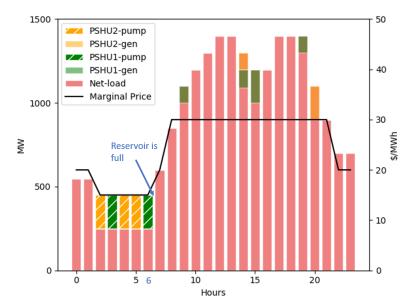
### **Remove Generation Costs and Pump Prices of PSHUs in Objective**

$$\min_{p,u} \sum_{g \in G_{sh}} \sum_{t \in T} f_{gt}^{h} - C_{gt}^{s} q_{g,t}^{s} + \sum_{g \in G} \sum_{t \in T} C(q_{gt})$$

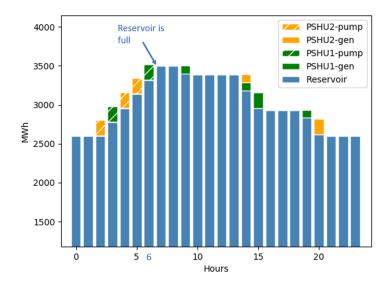
$$\sum_{g \in G} q_{gt} + \sum_{g \in G_{sh}} q_{gt}^{h} = D_t + \sum_{g \in G_{sh}} q_{gt}^{s} \quad \forall t \in T$$
(2)

- The objective doesn't contain costs or bid prices from PSHUs.
- The value of pumping and generation of a PSHU comes from the energy balance equation.

## **Economic Dispatch Results with Proposed Model**



## State of Charges at Reservoir



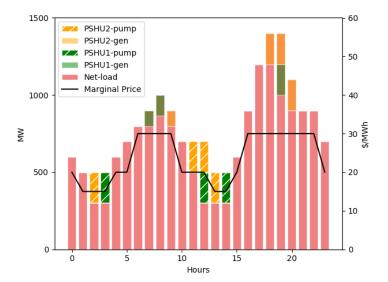
### **Generation Costs and PSHU Profits**

- PSHU pumps and generates the same amount but at different times from the two approaches.
- In current MISO practice, PSHUs are dispatched according to the comparison of their offer/bid to the system generation costs.
- In the proposed model, because of the state of charge constraints, the PSHUs are positioned such that the system costs are reduced the most.
- The profits of PSHU owner in the current practice varies from their offer/bid. But the profits given by the proposed model is the maximum they can get.

|              | Current Practice | Proposed Model |
|--------------|------------------|----------------|
|              | \$               | \$             |
| PSHU Profits | 5,300            | 9,300          |
| System Costs | 429,200          | 426,461        |

Table: PSHU Owner Profits and Social Welfare

## A Different Scenario with Proposed Model



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## **Conclusion and Future Work**

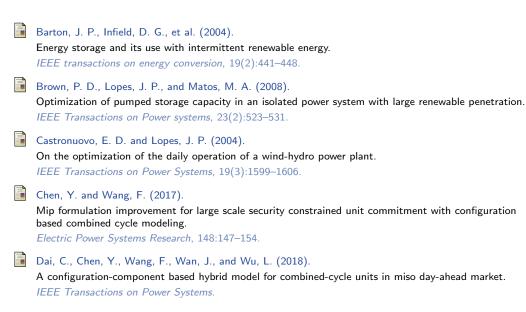
#### Conclusion

- A configuration based three modes pumped-storage hydro unit model in the day-ahead market is presented.
- A numerical study is presented with two identical turbines sharing a reservoir.
- The proposed model is compared with current MISO practice showing differences at unit dispatches and benefits in terms of system generation costs and PSHU owner's profits.
- Flexible operations of the PSHUs with the proposed model are demonstrated with examples. **Future Work**
- Computational case study with MISO system is ongoing.
- Use an integer variable to represent the status of a multi-turbine PSHU.

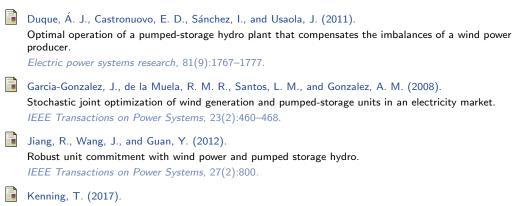




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