

A Multi-Period OPF Approach to Improve Voltage Stability using Demand Response

Daniel K. Molzahn¹
Mengqi Yao²
Johanna L. Mathieu²

¹Argonne National Laboratory

²University of Michigan

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Power System Stability

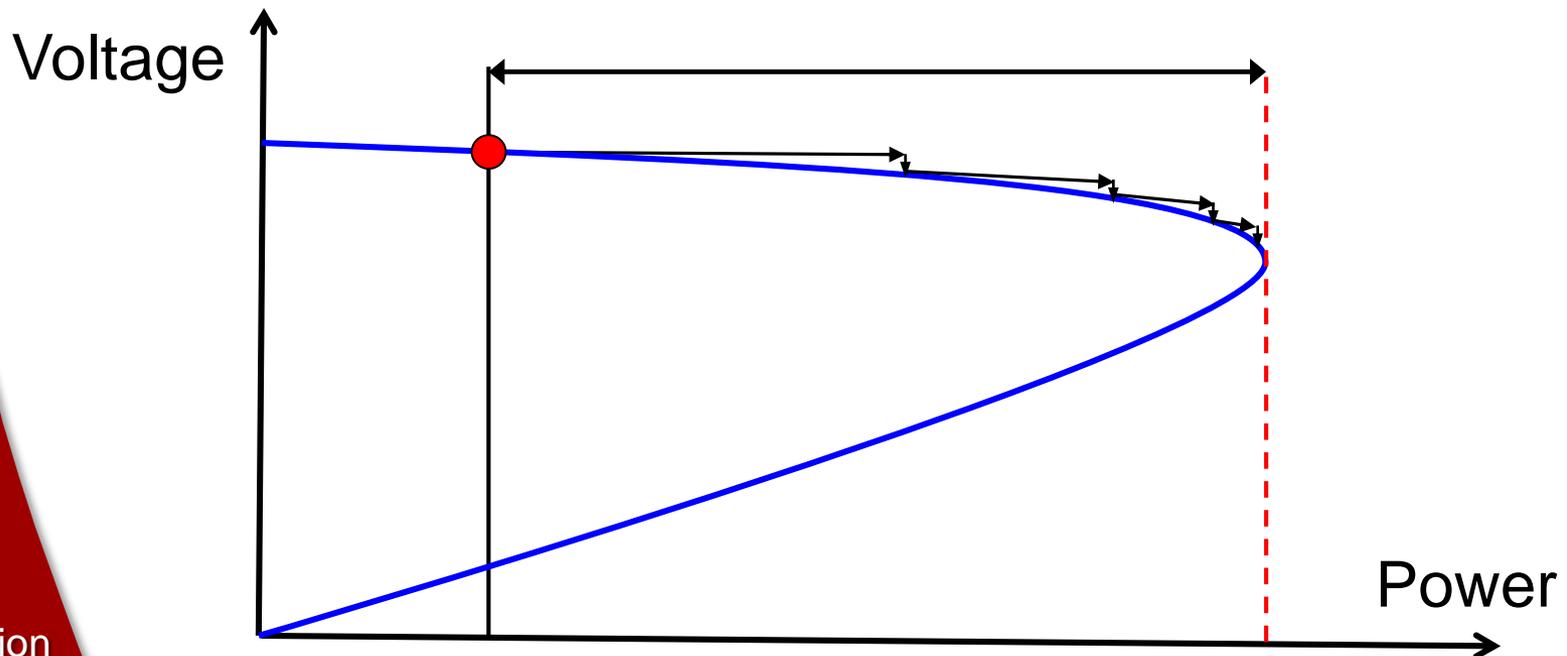
- Frequency instability
 - Associated with an **imbalance** between load and generation
 - Demand response based on **temporal shifting** of load
 - [Short, Infield, & Freris '07], [Molina-Garcia, Bouffard, & Kirschen '10],
[Mathieu, Koch, & Callaway '12], [Zhang, Lian, Chang, & Kalsi '13]
- Voltage instability
 - Associated with operation that nears the **limits of the network's** power transfer capability
 - Demand response based on **spatial shifting** of load

How to **control flexible loads** in order to **improve voltage stability** after a disturbance?

Voltage Stability

- Distance to the “nose point” of the PV curve
 - Often computed using continuation methods, which are difficult to embed within an optimization problem
 - A voltage stability metric based on power flow sensitivities is based on the smallest singular value of the power flow Jacobian

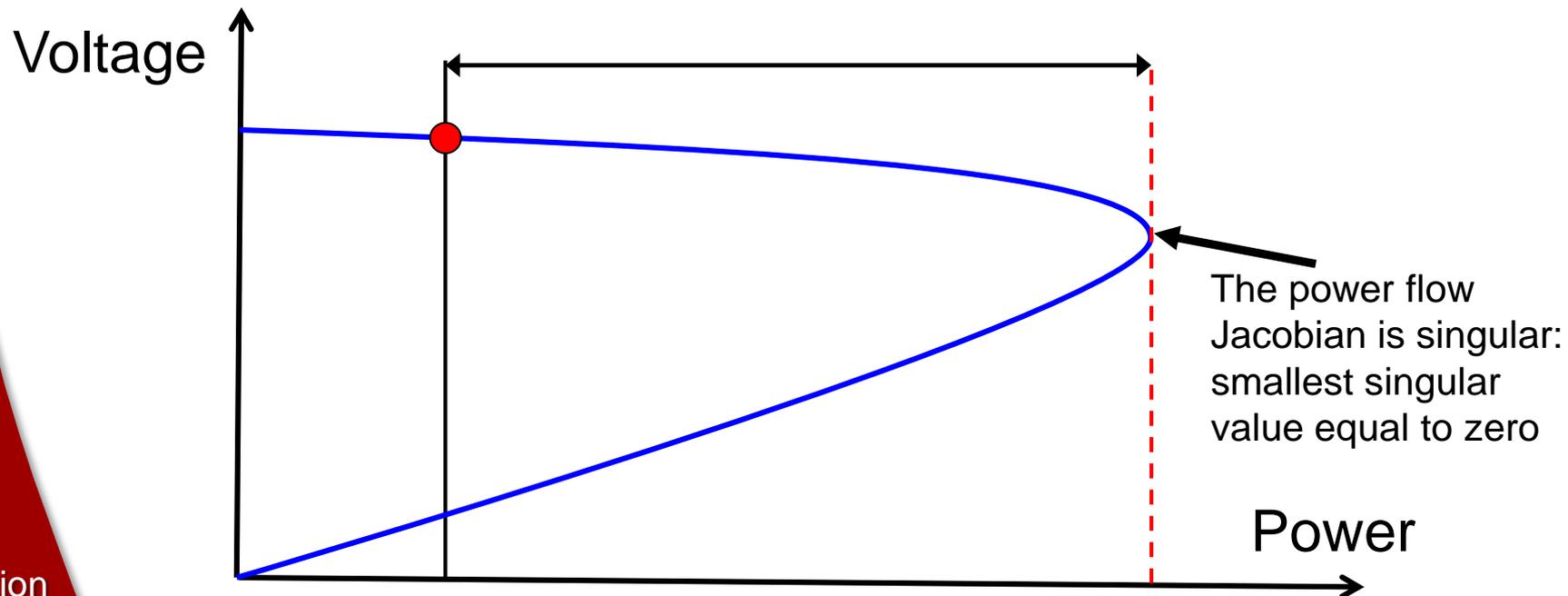
[Tiranuchit & Thomas '88], [Lof, Smed, Andersson, & Hill '92]



Voltage Stability

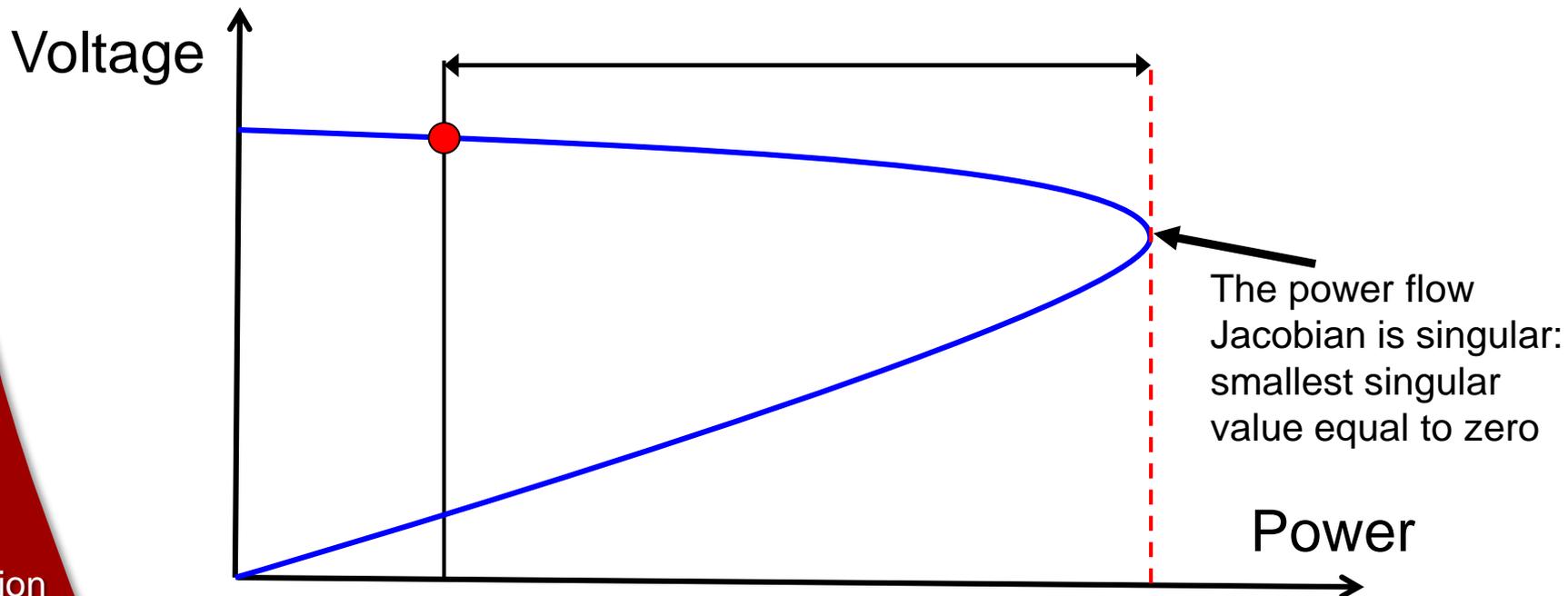
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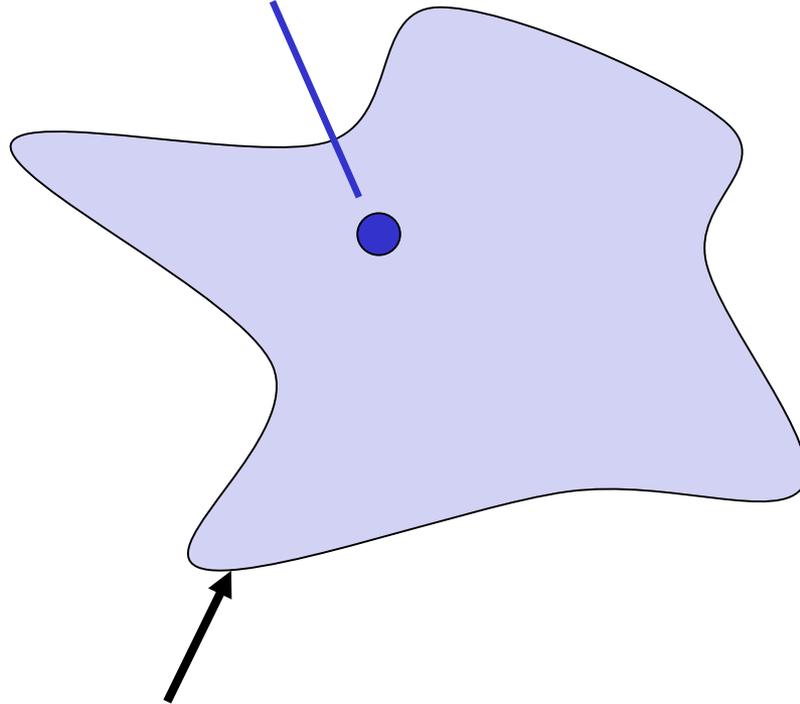
Our Approach

- Maximize the smallest singular value of the power flow Jacobian via control of flexible load demands
- Spatial shifting of loads with total demand held constant over time to maintain frequency stability



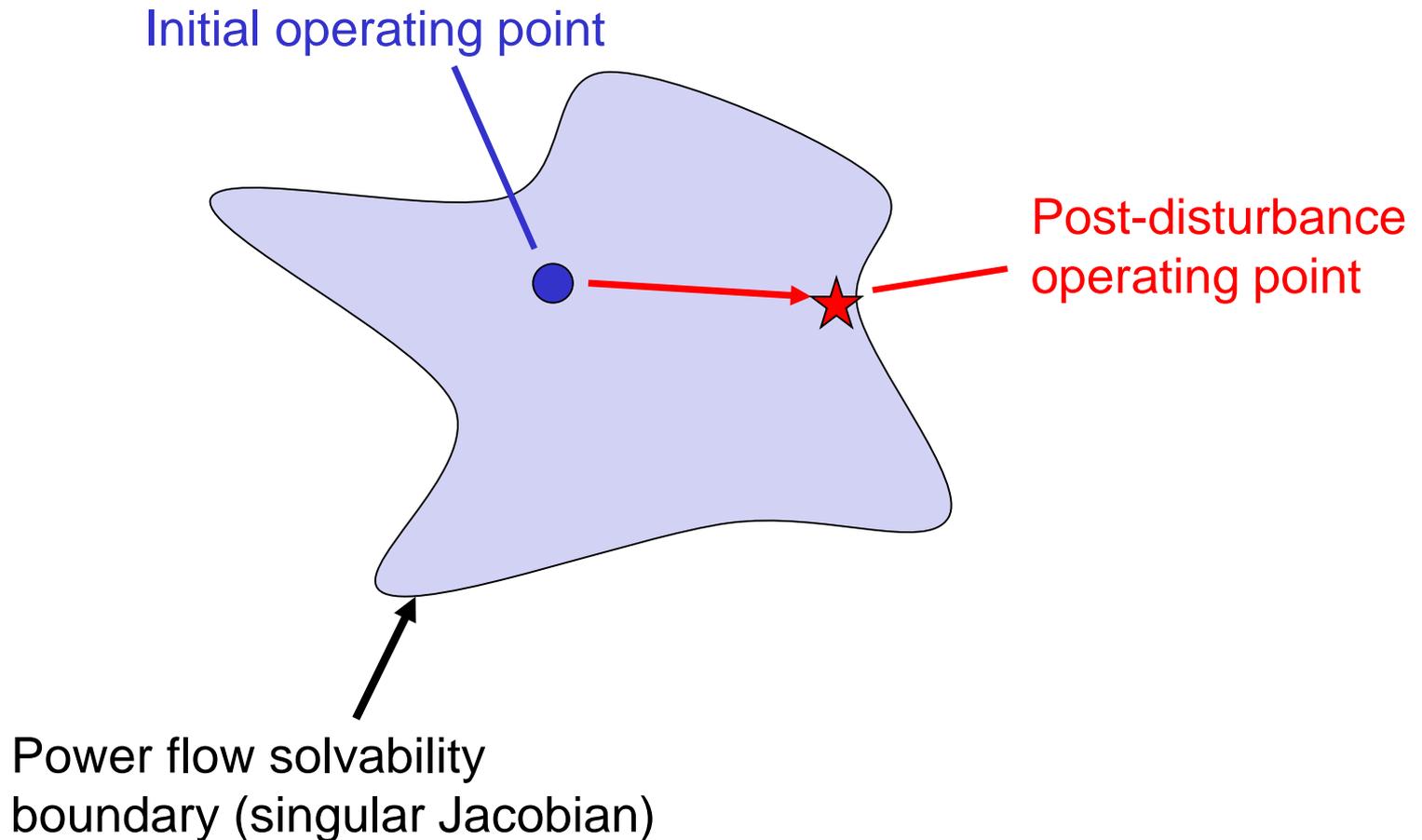
Multi-Period Approach

Initial operating point

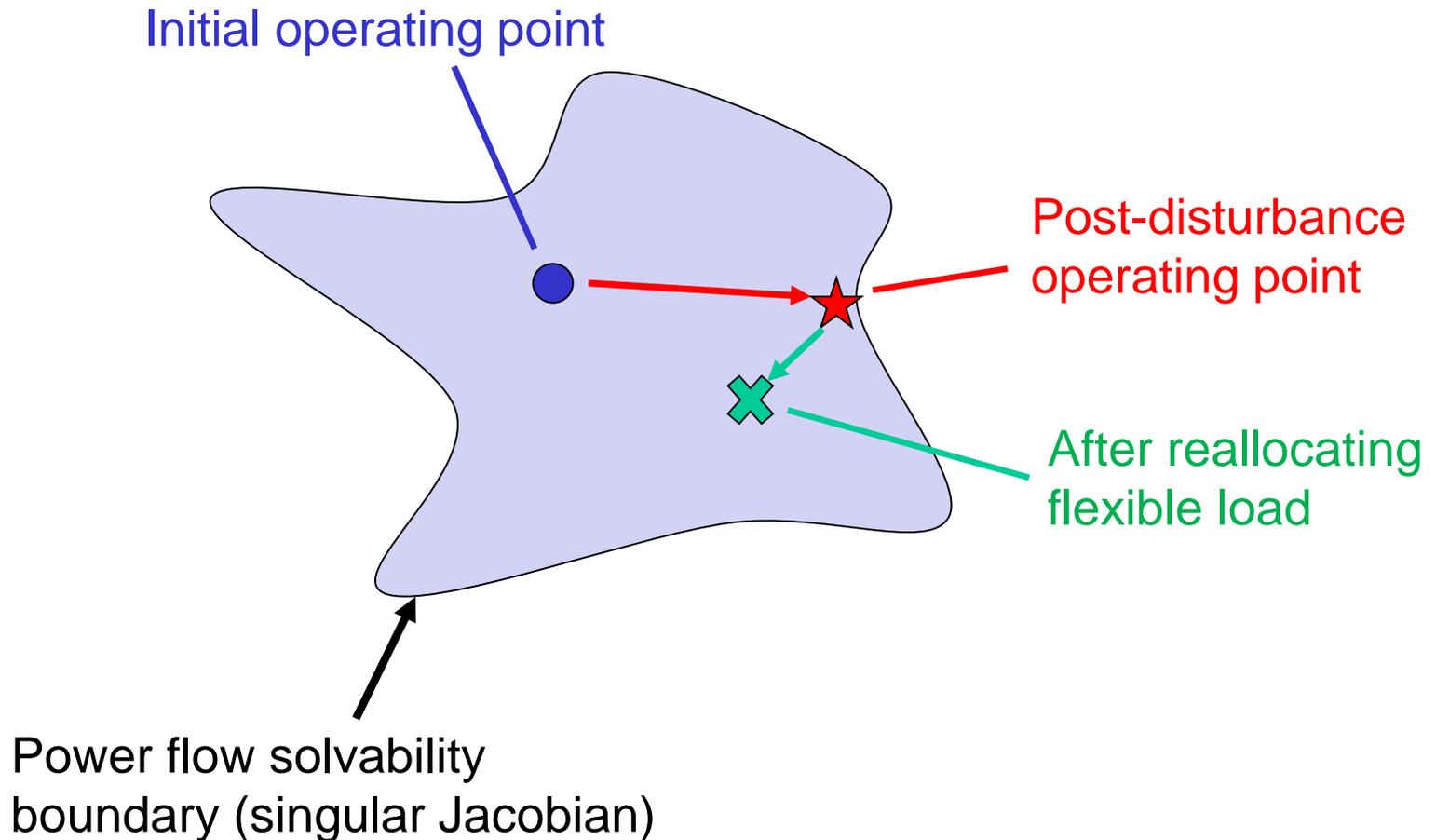


Power flow solvability
boundary (singular Jacobian)

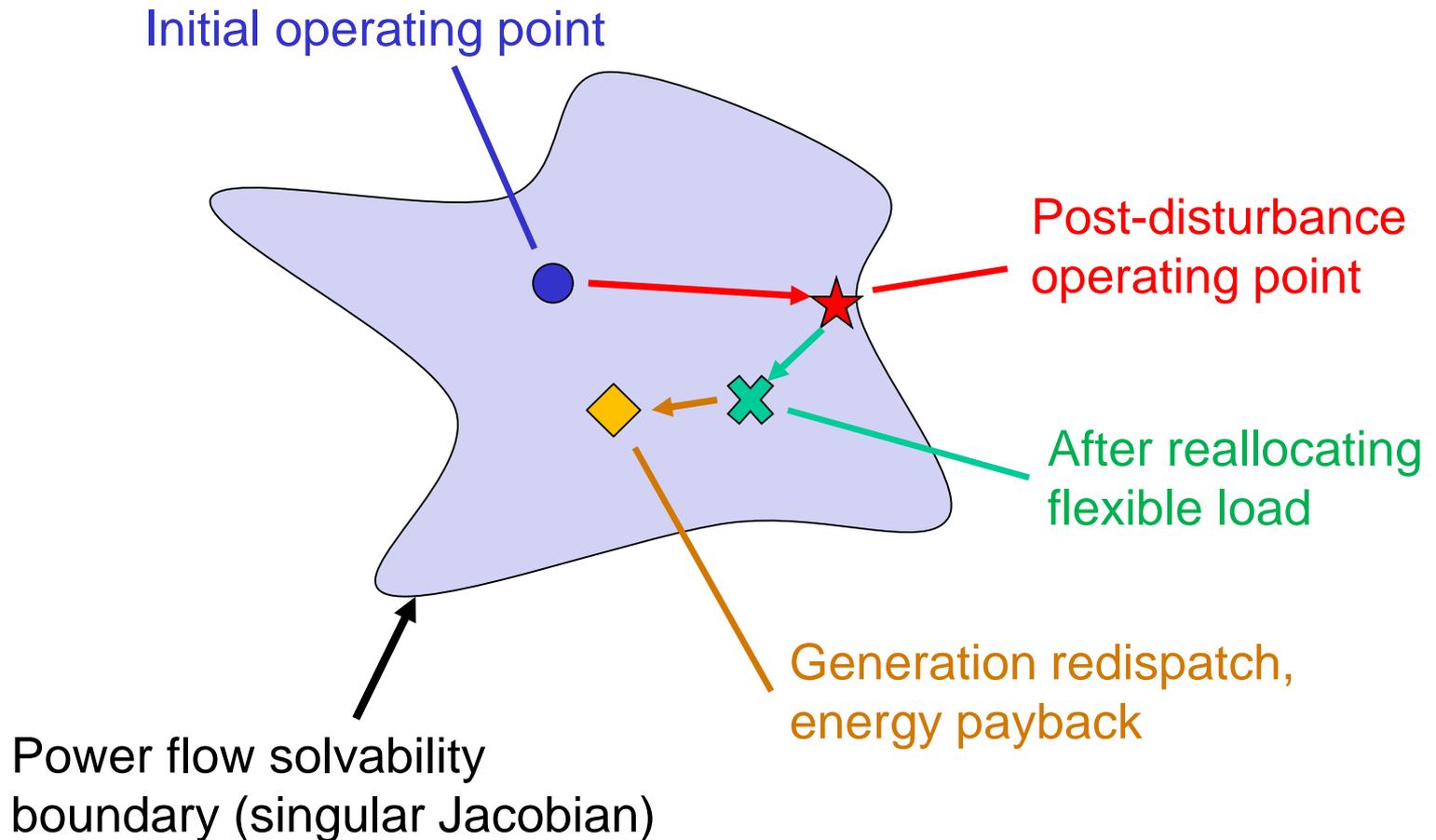
Multi-Period Approach



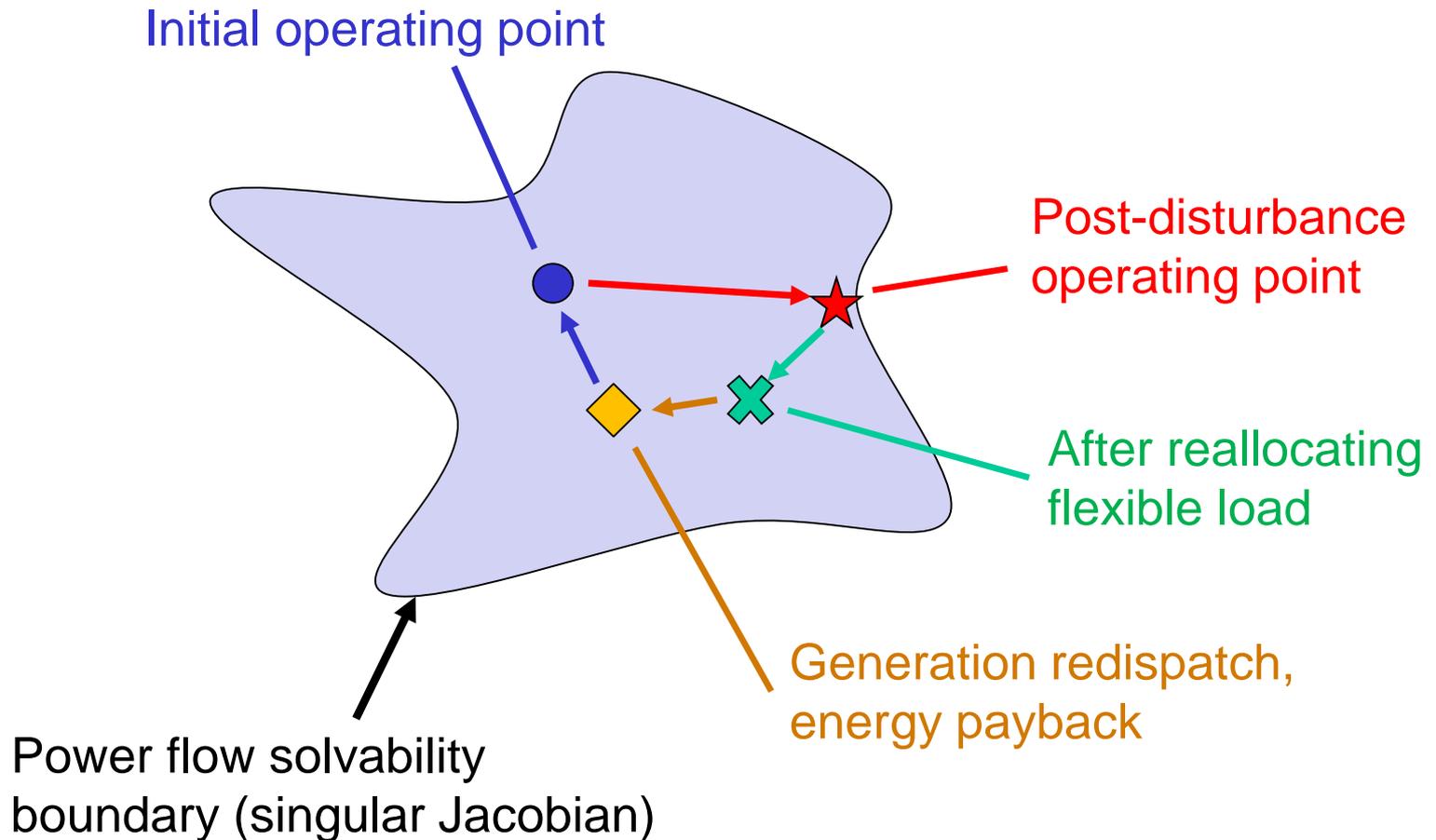
Multi-Period Approach



Multi-Period Approach



Multi-Period Approach



Problem Formulation

Assumptions

- Load models
 - Constant power factor
 - Flexible loads at some or all PQ buses
 - Total demand from flexible loads held constant at each period
- Generator models
 - Modeled as PV buses immediately after the disturbance
 - Active power generation redispatched in subsequent periods

We first show the single-period formulation,
and then extend to a multi-period setting.

Smallest Singular Value Maximization

$$\max \lambda_0$$

subject to

$$\mathbf{J}(\theta, V)^\top \mathbf{J}(\theta, V) - \lambda_0 \mathbf{I} \succeq 0 \quad \lambda_0 \leq \text{smallest singular value of the power flow Jacobian}$$

$$\sum_{i \in \mathcal{S}_{DR}} P_{d,i} = P_{d,total}$$

Total flexible load demand is constant

$$\mathcal{F}(x) = 0$$

AC power flow equations

$$\mathcal{G}(x) \geq 0$$

Operational limits

$$x = \{P_g, Q_g, P_d, Q_d, V, \theta\}$$

Directly solving this problem is challenging

Solution via Successive Linearization

- Use singular value sensitivities and a linearization of the AC power flow equations
- Sensitivity of the singular values λ_i for the Jacobian $\mathbf{J}(\xi)$ with respect to a parameter in $\xi = [\theta_1 \dots \theta_n \ V_1 \dots V_n]^T$:

$$\frac{\partial \lambda_i}{\partial \xi} = \underbrace{w_i^T}_{\text{Left eigenvector}} \frac{\partial ((\mathbf{J}(\xi))^T \mathbf{J}(\xi))}{\partial \xi} \underbrace{u_i}_{\text{Right eigenvector}}$$

Left eigenvector

Right eigenvector

The approximate change in λ_0 is

$$\Delta \lambda_0 = \sum_{i=1}^n \left[w_0^T \frac{\partial ((\mathbf{J}(\xi))^T \mathbf{J}(\xi))}{\partial \theta_i} u_0 \right] \Delta \theta_i + \left[w_0^T \frac{\partial ((\mathbf{J}(\xi))^T \mathbf{J}(\xi))}{\partial V_i} u_0 \right] \Delta V_i$$

Incremental Formulation

$$\max \quad \Delta\lambda_0$$

Take a step that seeks to increase the smallest singular value

subject to

$$\Delta\lambda_0 = \sum_{i=1}^n \left[w_0^T \frac{\partial ((\mathbf{J}(\xi))^T \mathbf{J}(\xi))}{\partial \theta_i} u_0 \right] \Delta\theta_i + \left[w_0^T \frac{\partial ((\mathbf{J}(\xi))^T \mathbf{J}(\xi))}{\partial V_i} u_0 \right] \Delta V_i$$

The singular value sensitivity

$$\sum_{i \in \mathcal{S}_{DR}} \Delta P_{d,i} = 0$$

Total flexible load demand is constant

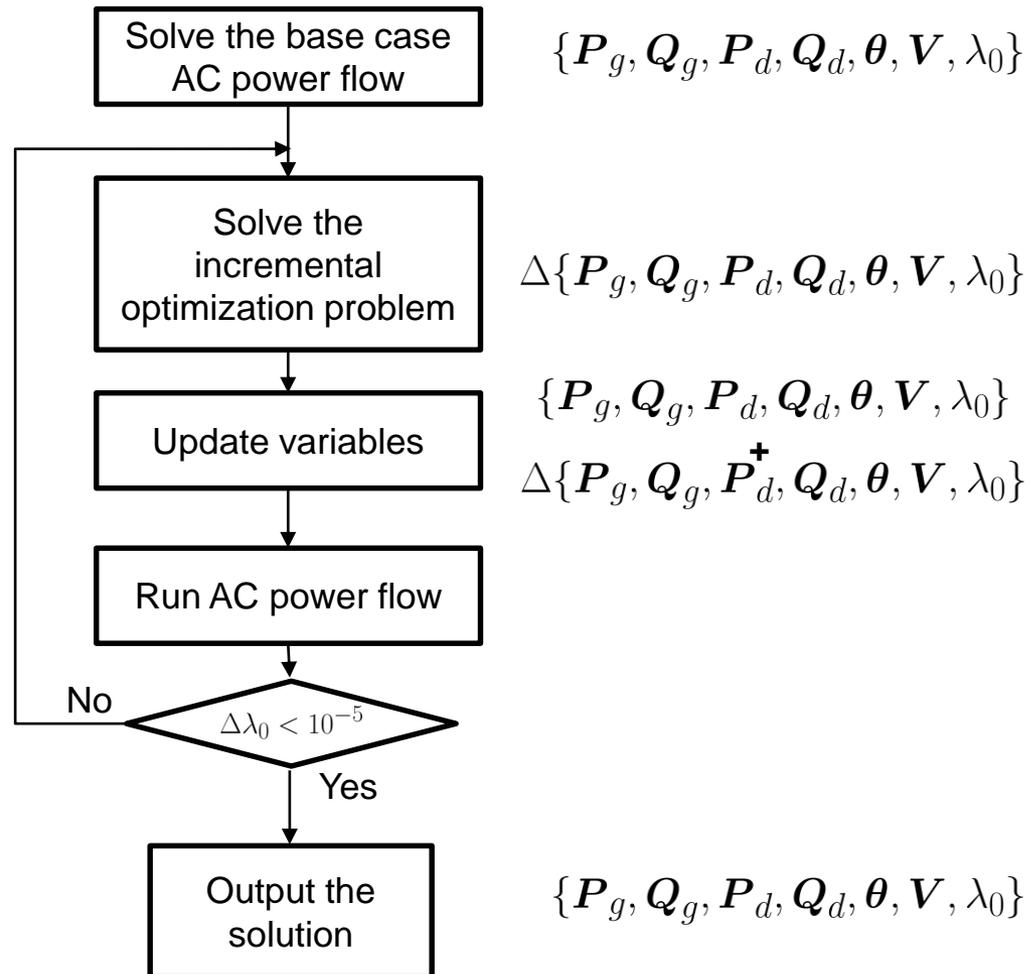
$$f(\Delta x) = 0$$

Linearized AC power flow equations

$$g(\Delta x) \geq 0$$

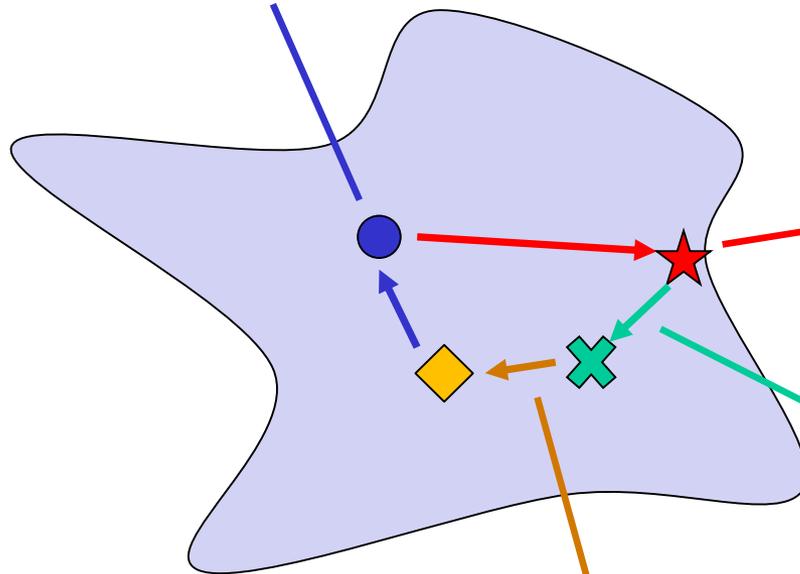
Linearized operational constraints

Successive Linearization Algorithm



Recall the Multi-Period Approach

Initial operating point

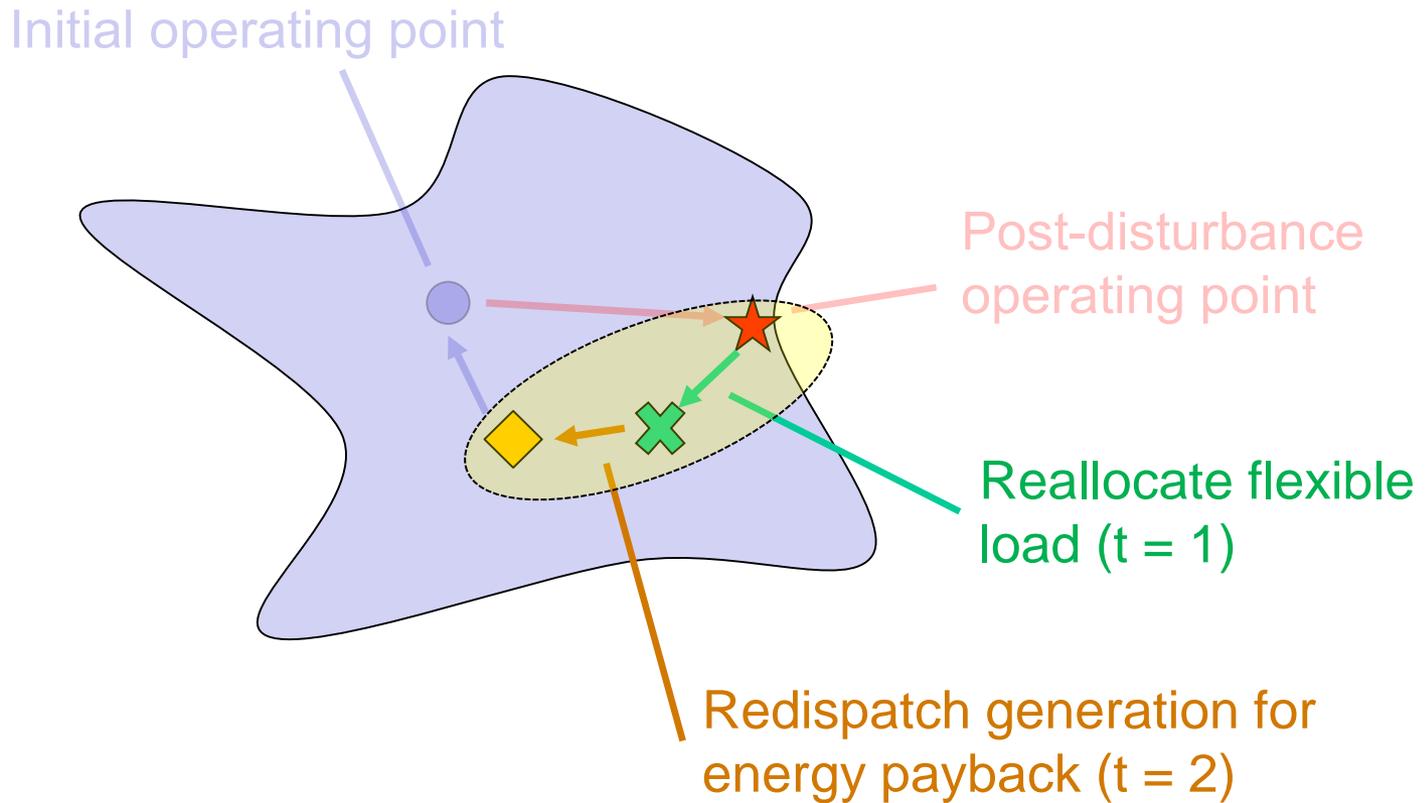


Post-disturbance
operating point

Reallocate flexible
load ($t = 1$)

Redispatch generation for
energy payback ($t = 2$)

Recall the Multi-Period Approach



Optimize flexible loads in these steps

Multi-Period Formulation

$$\min_{\mathbf{x}(t)} \quad -\alpha \lambda_0(1) + \beta \mathcal{C}(P_G(2))$$

Optimize a weighted sum of the smallest singular value and the generation redispatch cost for energy payback

subject to

$$\mathbf{J}(t)^\top \mathbf{J}(t) - \lambda_0(t) \mathbf{I} \succeq 0$$

$\lambda_0(t) \leq$ smallest singular value of the power flow Jacobian

$$\sum_{i \in \mathcal{S}_{DR}} P_{d,i}(1) = P_{d,total}$$

Total flexible load demand is constant

$$P_{d,i}(1) + P_{d,i}(2) = P_{d,i}^\circ, \quad \forall i \in \mathcal{S}_{DR}$$

Power demand shifted from flexible loads is “paid back”

$$\mathcal{F}(x(t)) = 0, \quad \mathcal{G}(x(t)) \geq 0$$

AC power flow equations and operational limits

t=1: Smallest singular value maximization

t=2: Energy payback for flexible loads

Multi-Period Formulation

$$\min_{\mathbf{x}(t)} \quad -\alpha \lambda_0(1) + \beta \mathcal{C}(P_G(2))$$

Optimize a weighted sum of the smallest singular value and the generation redispatch cost for energy payback

subject to

$$\mathbf{J}(t)^\top \mathbf{J}(t) - \lambda_0(t) \mathbf{I} \succeq 0$$

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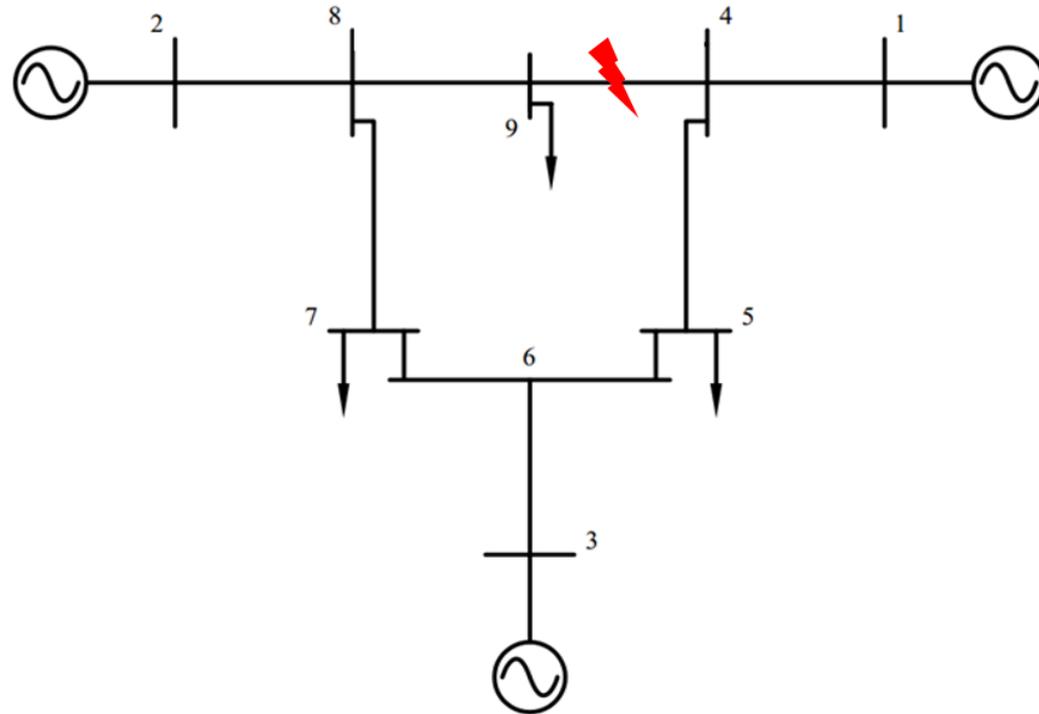
AC power flow equations and operational limits

Solve using a successive linearization algorithm

Test Cases



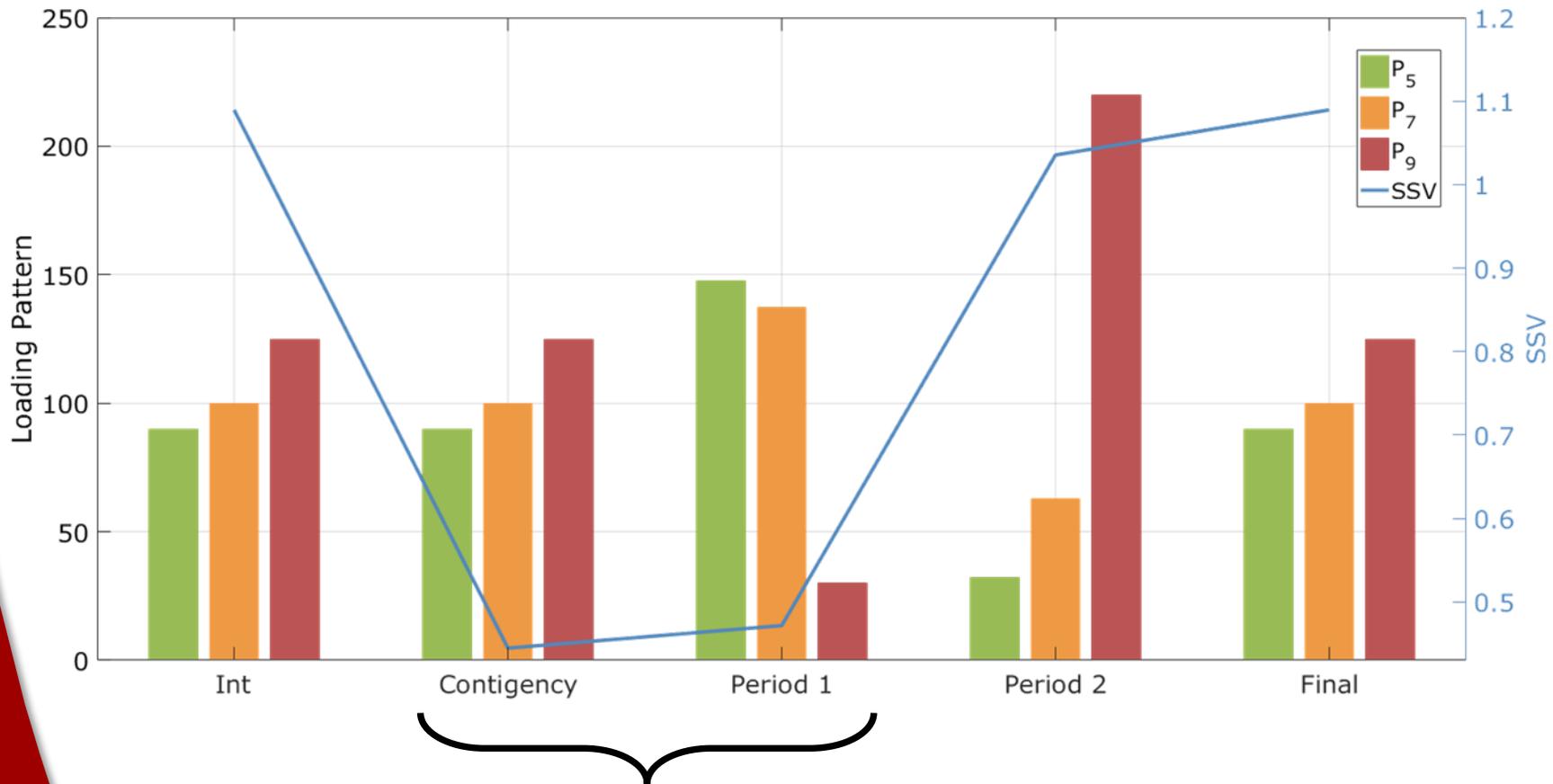
Nine-Bus Test Case



Smallest Singular Value: 1.0895 \longrightarrow 0.4445

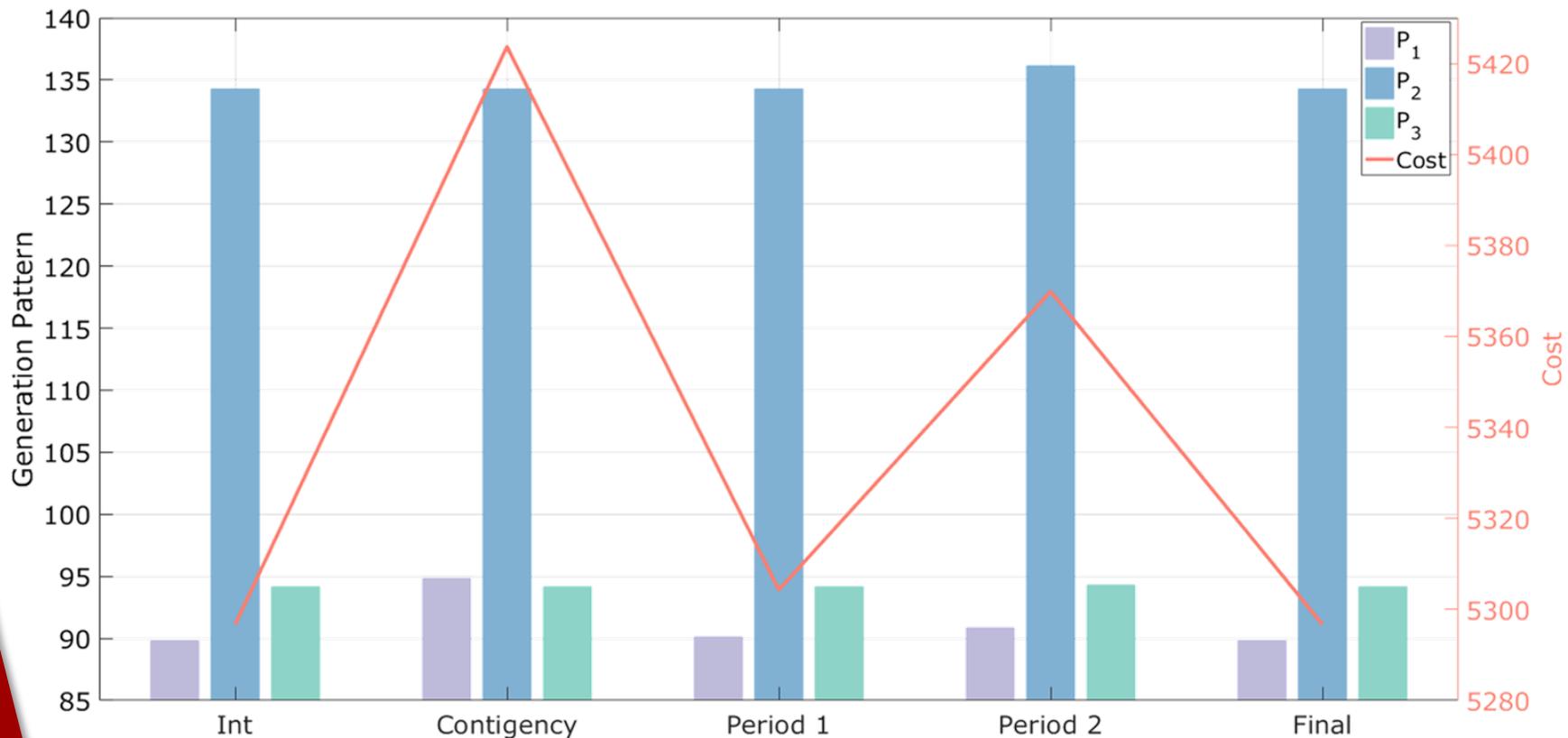
59% decrease

Results: Smallest Singular Value



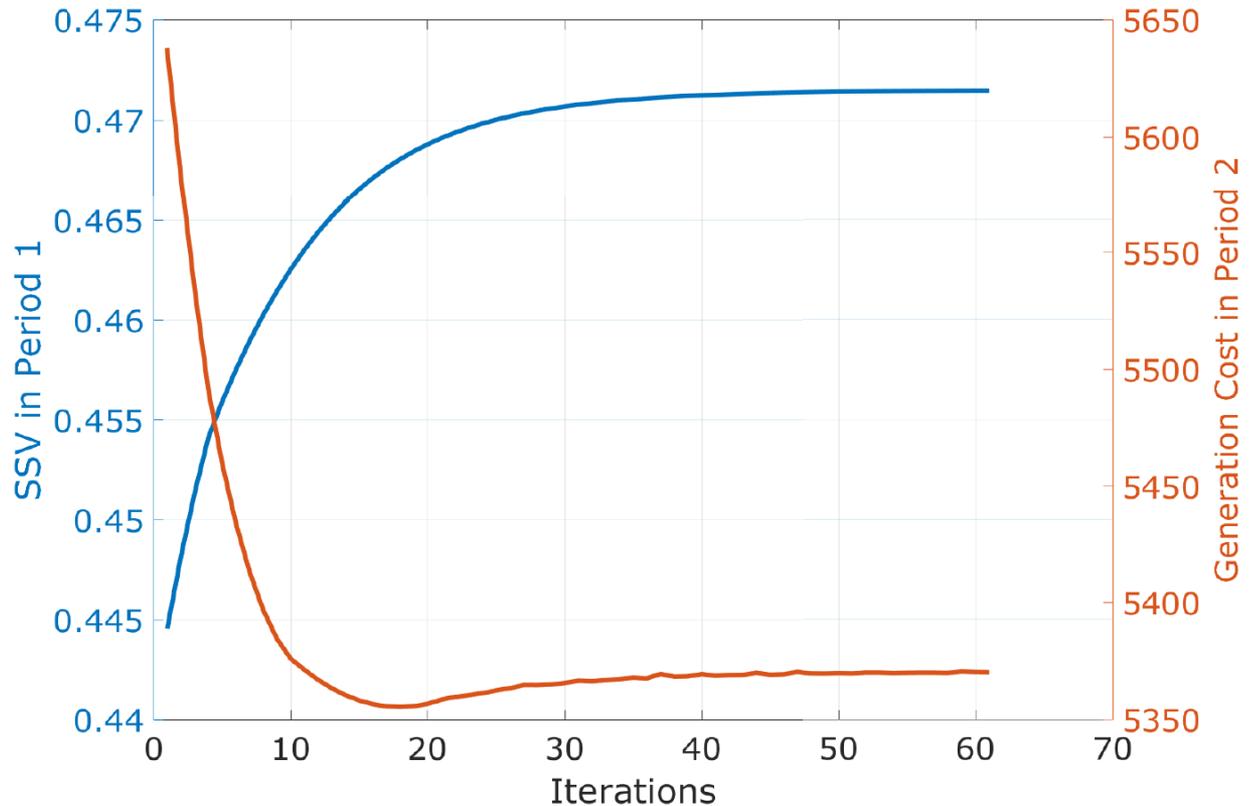
6.1% improvement in the smallest singular value from spatially shifting controllable loads

Results: Generation Cost



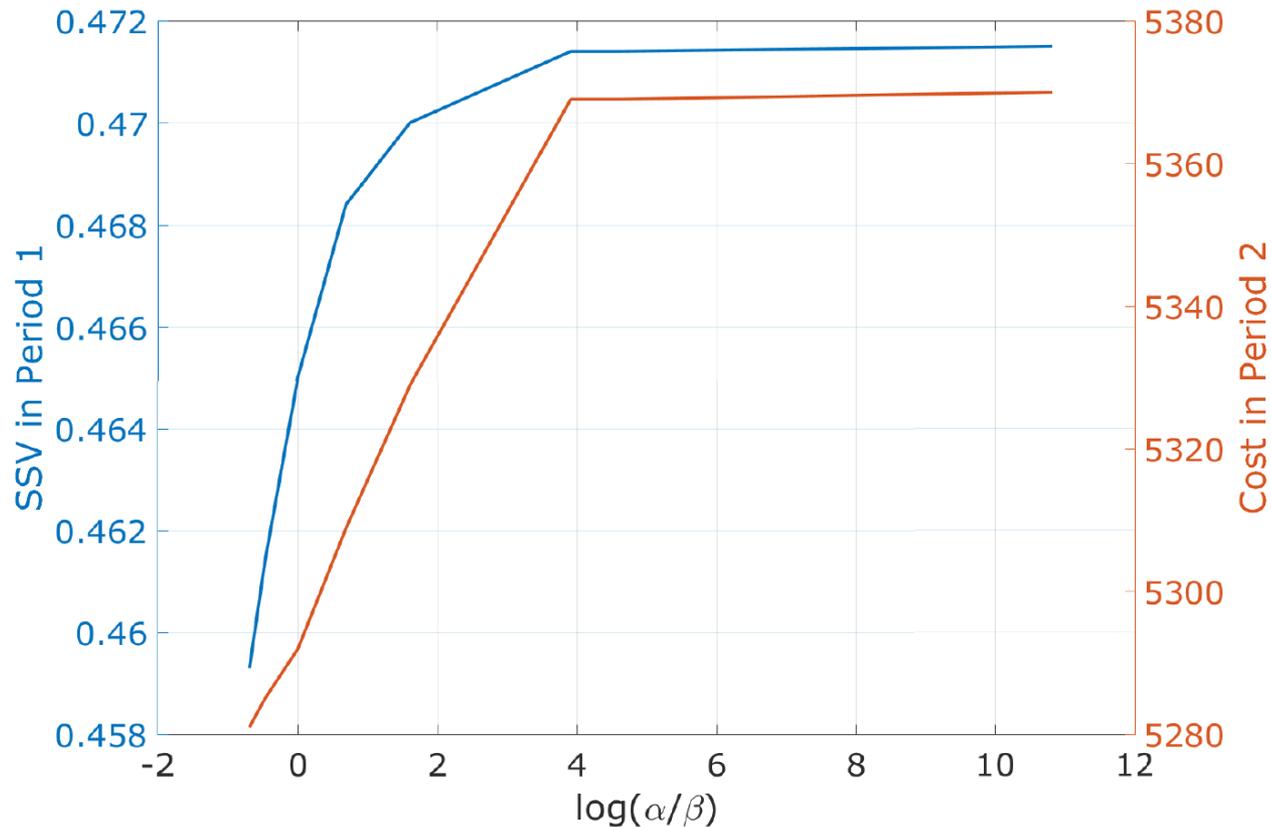
0.8% increase in generation cost from spatially shifting controllable loads

Convergence Rate



The successive linear programming algorithm typically **converges in a few tens of iterations**

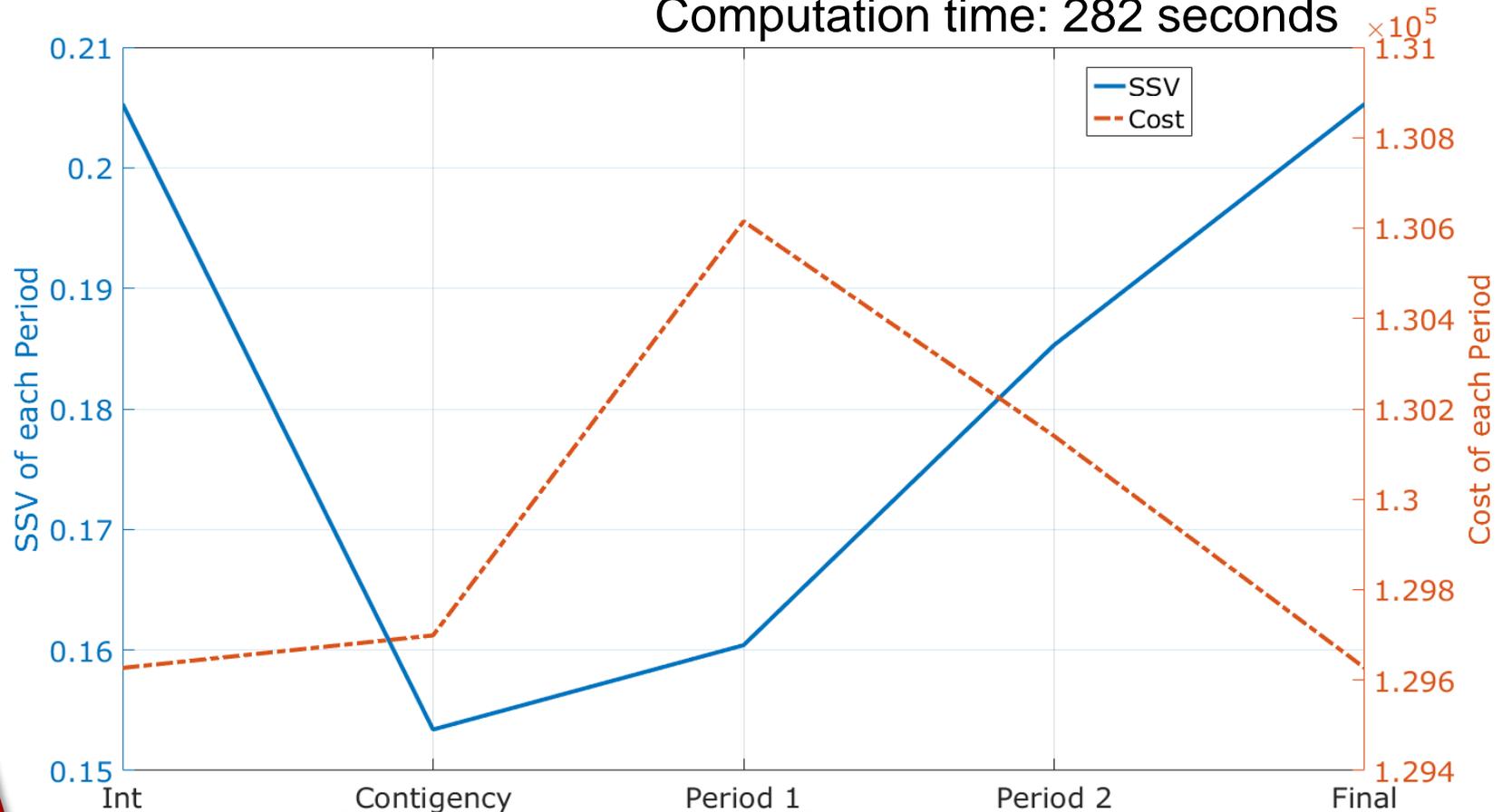
Trade-Off Between Smallest Singular Value and Generation Cost



The weights in the objective function effectively **control the trade-off** between higher generation cost and improved voltage stability margins

IEEE 118-Bus Test Case

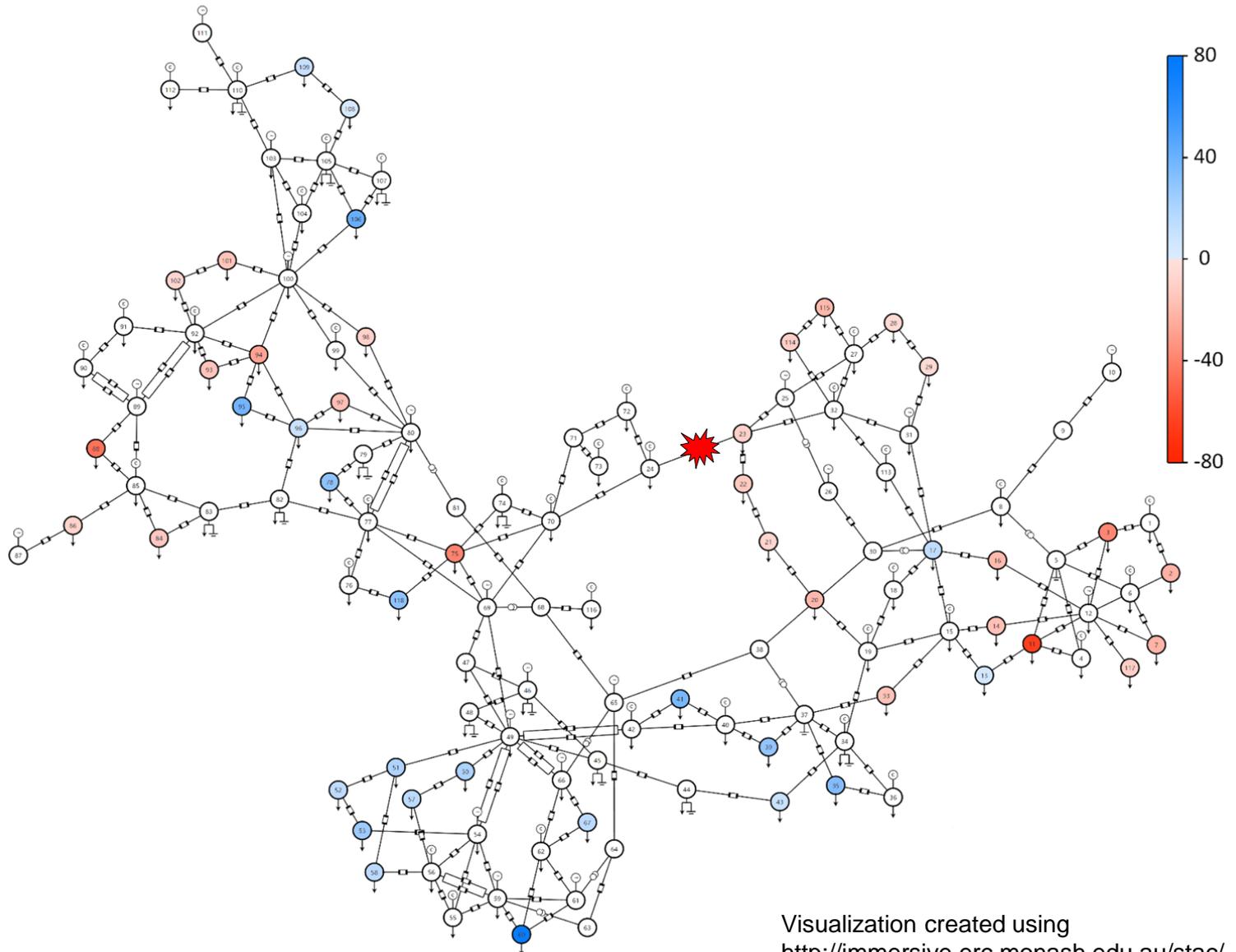
Computation time: 282 seconds



4.6% improvement in the smallest singular value

0.2% increase in the total generation cost

IEEE 118-Bus Test Case



Conclusion



Conclusion

- Spatial shifting of load can improve voltage stability margins after a disturbance
- To determine appropriate load control, we formulated a multi-period optimization problem and applied a successive linearization solution algorithm
- Future work:
 - Incorporating more detailed load models (ZIP loads)
 - Improving computational speed
 - Characterizing closeness to global optimality using convex relaxation techniques

Questions?

Daniel K. Molzahn

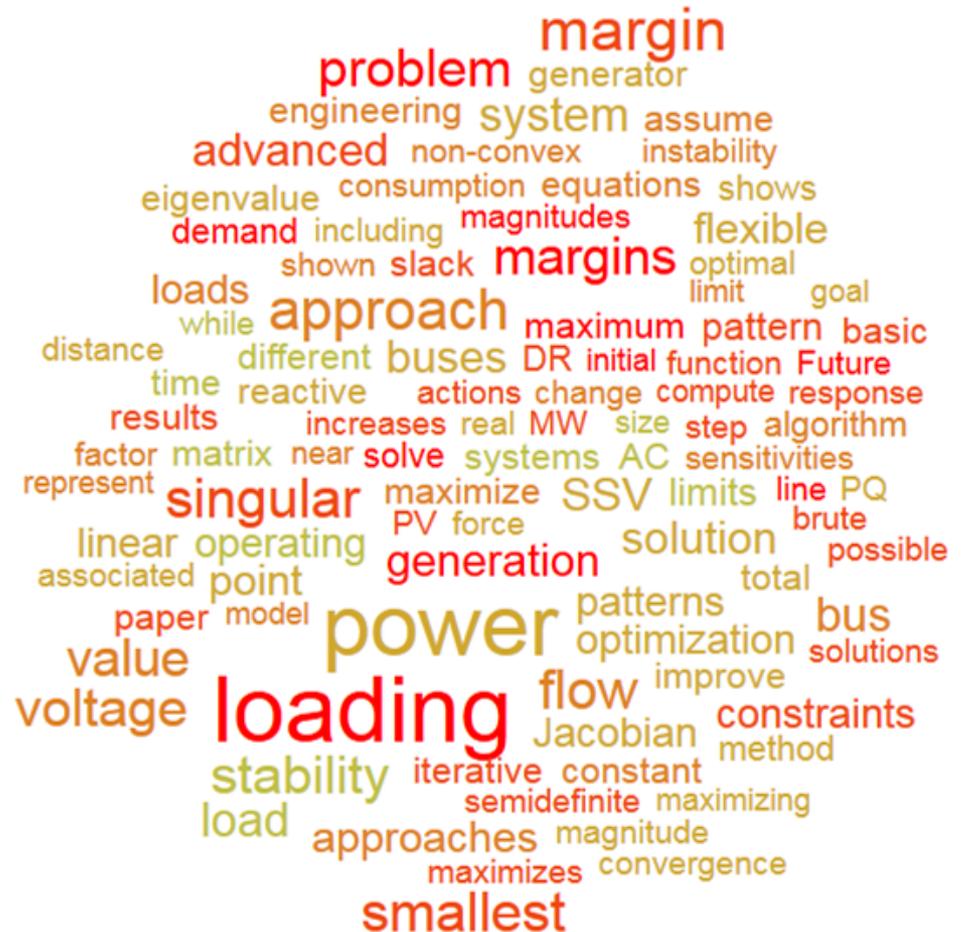
dmolzahn@anl.gov

Mengqi Yao

mgyao@umich.edu

Johanna L. Mathieu

jlmath@umich.edu



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