



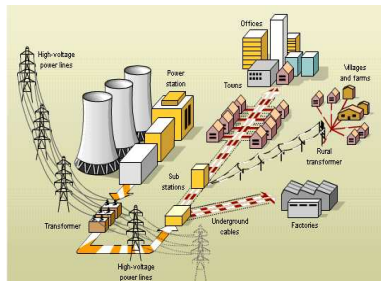
A Chance-constrained Unit Commitment Model for Power Systems with High Penetration of Renewable Energy

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Development of a solution framework for Unit Commitment (UC) problems with random generation:



- Identify feasible (or ϵ -optimal) schedules
- Capable of representing uncertainty with large samples
- Applicable to reasonably-sized systems

Unit Commitment Problem



Find a cost-effective combination of units that serves the power demand of the system, while satisfies operating constraints of the units and transmission.

■ Time horizon:

\mathcal{T}

■ Scheduling:

u_g, v_g

■ Dispatch:

p_g

$$\begin{aligned} \min \quad & \sum_{n \in \mathcal{N}} \sum_{t \in \mathcal{T}} c_n(p_{g_n}^t) + F u_{g_n}^t + S_n^t v_{g_n}^t \\ & (p_g, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} s p_n^t = S r^t, \\ & \sum_{n \in \mathcal{N}} s p_n^t + n p_n^t = S n^t \end{aligned}$$

■ $\mathcal{C}_{\text{dyn}}^{\text{gen}}$: ramping, up/down times

■ $\mathcal{C}_{\text{stat}}^{\text{gen}}$: generation limits

Unit Commitment Problem



Find a cost-effective combination of units that serves the power demand of the system, while satisfies operating constraints of the units and transmission.

■ Time horizon:

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■ Scheduling:

u_g, v_g

■ Dispatch:

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$$\begin{aligned} \min \quad & C(p_g, u_g, v_g) \\ & (p_g, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} s p_n^t = S r^t, \\ & \sum_{n \in \mathcal{N}} s p_n^t + n p_n^t = S n^t \end{aligned}$$

■ DC Power
Flow

■ Spinning
Reserve

■ Non-spinning
Reserve

Unit Commitment Model

Renewable generation



Given there is renewable generation, find a cost-effective combination of units that serves the power demand of the system, while satisfies operating constraints of the units and transmission.

$$\begin{aligned} \min \quad & C(p_g, u_g, v_g) \\ & (p_g, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + \mathbf{P}_{r_k}^t + p_{ij_k}^t = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} s p_n^t = S r^t, \\ & \sum_{n \in \mathcal{N}} s p_n^t + n p_n^t = S n^t \end{aligned}$$

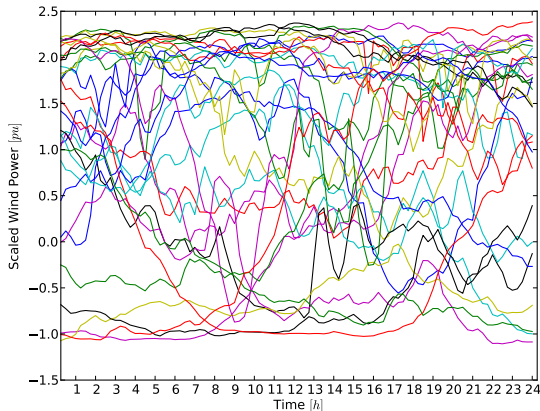
Unit Commitment Problem

Renewable generation: challenges



■ Forecast

■ System reserve



January 2014, ELIA - Belgium system

Stochastic Unit Commitment Formulation

Stochastic two-stage model



Given a set of realization: $\omega \in \Omega$

$$\begin{aligned} \min \quad & C_1(u_g, v_g) + \mathbb{E}[C_2(p_g)] \\ & (p_g(\omega), u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t(\omega) + \mathbf{p}_{r_k}^t(\omega) + p_{ij_k}^t(\omega) = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}(\omega)| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} sp_n^t(\omega) = Sr^t, \\ & \sum_{n \in \mathcal{N}} sp_n^t(\omega) + np_n^t(\omega) = Sn^t \end{aligned}$$

u_g, v_g is the (risk-neutral) commitment that minimizes the expected dispatch cost $\mathbb{E}[C_2(p_g)]$

Chance-Constrained Formulation

Scenarios $\omega \in \Omega$



Risk-averse UC and probabilistic reserve levels:

$$\begin{aligned} \min \quad & C(u_g, v_g, p_g) \\ & (p_g, sp, np, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \mathbb{P}\left[\sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \mathbf{L}_k^t - \mathbf{p}_{r_k}^t, k \in \mathcal{K}\right] \geq \pi, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \mathbb{P}\left[\sum_{n \in \mathcal{N}} sp_n^t = S r^t + \alpha \mathbf{p}_r^t\right] \geq \rho, \\ & \mathbb{P}\left[\sum_{n \in \mathcal{N}} sp_n^t + np_n^t = S n^t + \beta \mathbf{p}_r^t\right] \geq \rho \end{aligned}$$

(u_g, v_g, p_g) schedule determined by a risk-averse net-load operating level: $[L - p_r]_{\pi}$

(sp, np) system reserves allocated with a risk-averse renewable level: $[p_r]_{\rho}$

Chance-Constrained Formulation

Scenarios $\omega \in \Omega$



Risk-averse UC and probabilistic reserve levels:

$$\begin{aligned} \min \quad & C(u_g, v_g, p_g) \\ & (p_g, sp, np, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = w_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} sp_n^t = Sr^t + \alpha z^t, \\ & \sum_{n \in \mathcal{N}} sp_n^t + np_n^t = Sn^t + \beta z^t, \\ & w \in \mathcal{W}_\pi, z \in \mathcal{Z}_\rho \end{aligned}$$

Netload: $\mathcal{W}_\pi = \{w \in \mathbb{R}^{KT} : \mathbb{P}(\mathbf{L}_t^k - \mathbf{p}_{r_k}^t \leq w_k^t) \geq \pi\}$

Reserve renewable: $\mathcal{Z}_\rho = \{z \in \mathbb{R}^T : \mathbb{P}(\mathbf{p}_r^t \leq z^t) \geq \rho\}$

Decomposition Scheme



Introduce artificial variables: $\bar{p}_g, \bar{s}p, \bar{n}p, \bar{w}, \bar{z}$

$$\begin{aligned} \min \quad & C(u_g, v_g, p_g) \\ & (\bar{p}_g, \bar{s}p, \bar{n}p, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \bar{w}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} sp_n^t = Sr^t + \alpha \bar{z}^t, \\ & \sum_{n \in \mathcal{N}} sp_n^t + np_n^t = Sn^t + \beta \bar{z}^t, \\ & p_g = \bar{p}_g, sp = \bar{s}p, np = \bar{n}p, \\ & w = \bar{w}, z = \bar{z}, \\ & w \in \mathcal{W}_\pi, z \in \mathcal{Z}_\rho \end{aligned}$$

Decomposition Scheme



Relax artificial constraints: $\lambda_p, \lambda_{sp}, \lambda_{np}, \lambda_w, \lambda_z$

$$L(p, w, z) = C(u_g, v_g, p_g) + \lambda_p^\top (p_g - \bar{p}_g) + \lambda_{sp}^\top (sp - \bar{s}p) \\ + \lambda_{np}^\top (np - \bar{n}p) + \lambda_w^\top (w - \bar{w}) + \lambda_z^\top (z - \bar{z}),$$

Dispatch - OPF

p_g, sp, np

\bar{w}, \bar{z}

Commitment

u_g, v_g

$\bar{s}p, \bar{n}p, \bar{p}_g$

Netload

$\mathbb{P}(\mathbf{L}_k^t - \mathbf{p}_r^t \leq w) \geq \pi$

$w \in \mathcal{W}_\pi$

Reserve

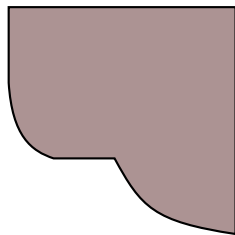
$\mathbb{P}(\mathbf{p}_r^t \leq z) \geq \rho$

$z \in \mathcal{Z}_\rho$

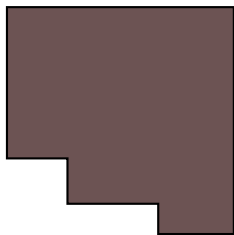
Stochastic subproblem



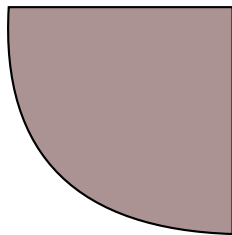
Feasible set example in 2D:



Mix. Uniform



Discrete



Gaussian

Given realizations: \mathcal{W}_π and \mathcal{Z}_ρ are non-convex (discrete).

Stochastic subproblem

Risk-averse netload



$$\mathcal{W}_\pi = \{w \in \mathbb{R}^{KT} : \mathbb{P}(\mathbf{L}_t^k - \mathbf{p}_{r_k}^t \leq w_k^t) \geq \pi\}$$

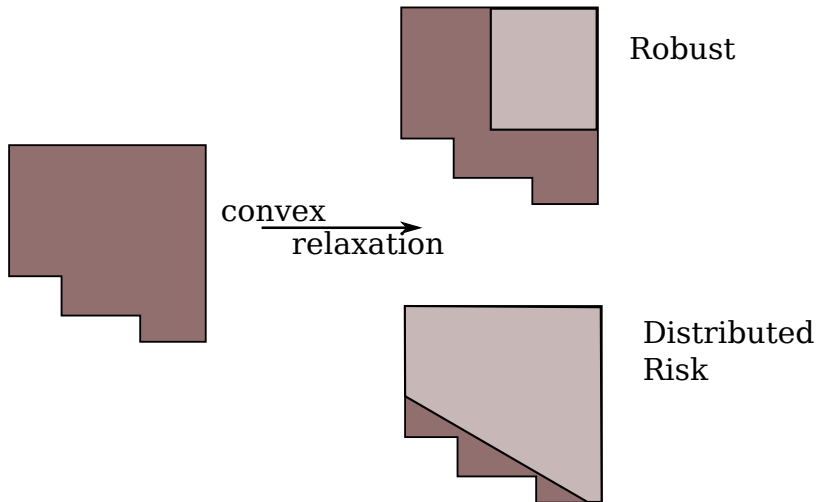
- Given a set of realizations $[\mathbf{L}_t^k - \mathbf{p}_{r_k}^t](\omega), \omega \in \Omega$ with probability $1/|\Omega|$
- Check the π -boundary: for every realization $e(\omega)$

$$e(\omega) = \begin{cases} 1 & [\mathbf{L}_t^k - \mathbf{p}_{r_k}^t](\omega) \leq w_k^t \\ 0 & \text{otherwise} \end{cases}$$

- $w \in \mathcal{W}_\pi$ if $\frac{1}{|\Omega|} \sum_{\omega \in \Omega} e(\omega) \geq \pi$

The subproblems: $\min\{\lambda_w^\top w | w \in \mathcal{W}_\pi\}$, $\min\{\lambda_z^\top z | z \in \mathcal{Z}_\rho\}$ are combinatorial problems, difficult to solve.

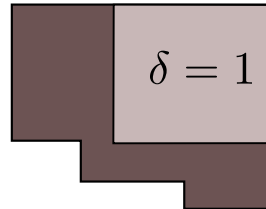
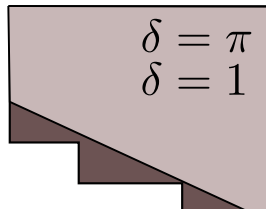
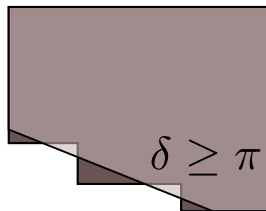
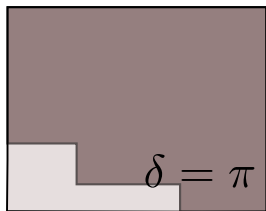
Relaxation Approach - Stochastic Subproblems



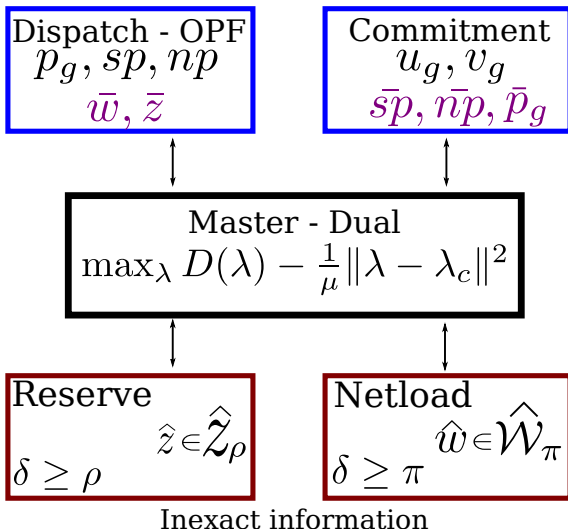
Relaxation Approach - Stochastic Subproblems



Scenarios $\omega \in \Omega$, $w(\omega)$, $z(\omega)$
 $\hat{w}_k^t = [w_k^t]_\delta$, $\hat{z}^t = [z^t]_\delta$, $\delta \geq \pi$



Approximate Bundle Method



Results - IEEE118 bus system

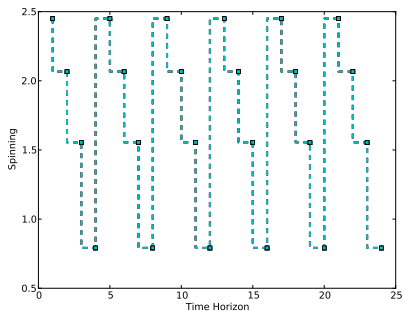
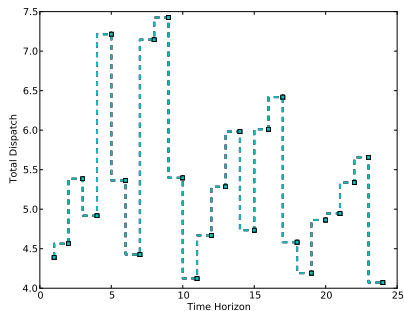


Wind farms: 53, 56, 32, 106, 6 – possible max generation 30%.

Nuclear: 30, 40, 37, 5.

Committed units:

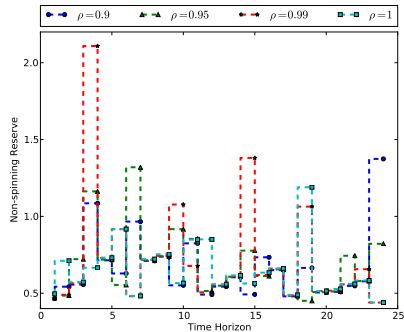
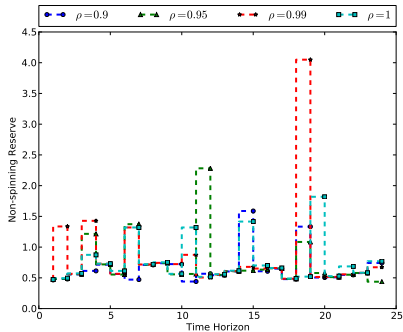
5,6,11,12,14,20,21,22,25,26,28,29,30,37,38,40,45,46,54



Results - IEEE118 bus system



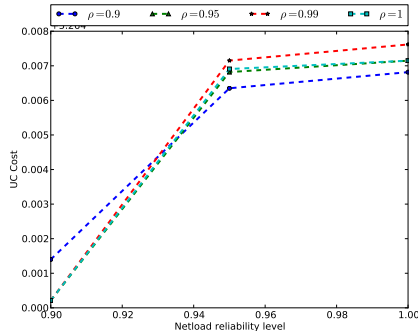
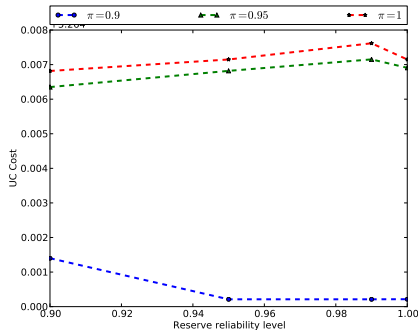
Wind farms: 53, 56, 32, 106, 6. Nuclear: 30, 40, 37, 5. Committed units: 5,6,11,12,14,20,21,22,25,26,28,29,30,37,38,40,45,46,54



Results - IEEE118 bus system



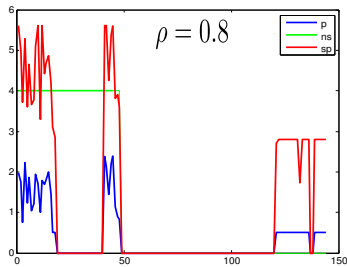
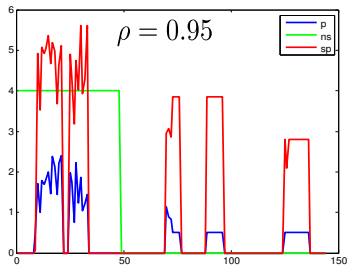
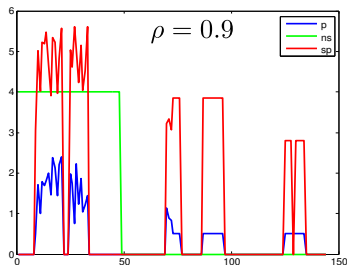
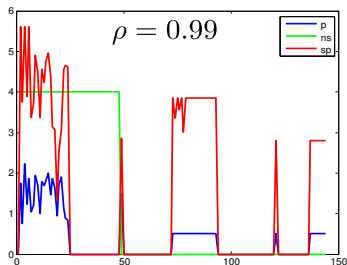
Wind farms: 53, 56, 32, 106, 6. Nuclear: 30, 40, 37, 5. Committed units: 5,6,11,12,14,20,21,22,25,26,28,29,30,37,38,40,45,46,54



Results - IEEE30 bus system



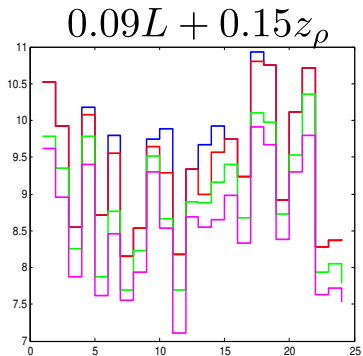
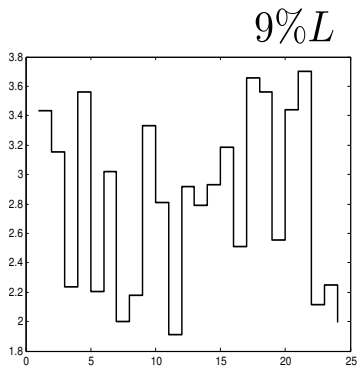
Wind farms: 1,5,21,22,26. Generators:1,2,22,27,23. $\pi = 0.9$



Results - IEEE30 bus system



Wind farms: 1,5,21,22,26. Generators:1,2,22,27,23. $\pi = 0.9$



— $\rho = 0.99$ — $\rho = 0.9$
— $\rho = 0.95$ — $\rho = 0.8$

The approach described has a number of advantages

- The risk-parameters can be set up by the user.
- The formulation is flexible and it can be implemented with OPF tools available - MATPOWER.
- Different number of realization can be used to estimate the percentiles at each period of time and node (where is needed)- important to accommodate forecast errors.
- Probabilistic reserves could be used to prepare the system for possible variations of wind power.
- The approach could be used to analyze safety renewable integration levels.
- The approach identifies risk-averse commitment



- Robust analysis of safety levels of renewable energy integration - UC
- Given UC and renewable integration levels: Refinement of dispatch
- Test the approach with different characterization of wind power: cluster representatives