



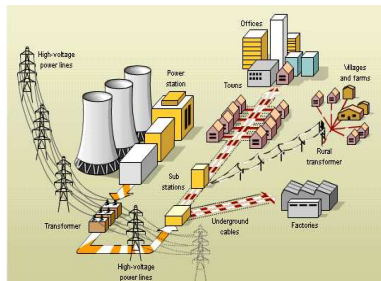
A Chance-constrained Unit Commitment Model for Power Systems with High Penetration of Renewable Energy

Gabriela Martínez
Lindsay Anderson

Department of Biological and Environmental Engineering
Cornell University

FERC Technical Conference on Increasing Real-Time and Day-Ahead Market Efficiency through Improved Software

Development of a solution framework for Unit Commitment (UC) problems with random generation:



- Identify feasible (or ϵ -optimal) schedules
- Capable of representing uncertainty with large samples
- Applicable to reasonably-sized systems

Unit Commitment Problem



Find a cost-effective combination of units that serves the power demand of the system, while satisfies operating constraints of the units and transmission.

■ Time horizon:

\mathcal{T}

■ Scheduling:

u_g, v_g

■ Dispatch:

p_g

$$\begin{aligned} \min \quad & \sum_{n \in \mathcal{N}} \sum_{t \in \mathcal{T}} c_n(p_{g_n}^t) + F u_{g_n}^t + S_n^t v_{g_n}^t \\ & (p_g, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} s p_n^t = S r^t, \\ & \sum_{n \in \mathcal{N}} s p_n^t + n p_n^t = S n^t \end{aligned}$$

■ $\mathcal{C}_{\text{dyn}}^{\text{gen}}$: ramping, up/down times

■ $\mathcal{C}_{\text{stat}}^{\text{gen}}$: generation limits

Unit Commitment Problem



Find a cost-effective combination of units that serves the power demand of the system, while satisfies operating constraints of the units and transmission.

■ Time horizon:

\mathcal{T}

■ Scheduling:

u_g, v_g

■ Dispatch:

p_g

$$\begin{aligned} \min \quad & C(p_g, u_g, v_g) \\ & (p_g, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} s p_n^t = S r^t, \\ & \sum_{n \in \mathcal{N}} s p_n^t + n p_n^t = S n^t \end{aligned}$$

■ DC Power
Flow

■ Spinning
Reserve

■ Non-spinning
Reserve

Unit Commitment Model

Renewable generation



Given there is renewable generation, find a cost-effective combination of units that serves the power demand of the system, while satisfies operating constraints of the units and transmission.

$$\begin{aligned} \min \quad & C(p_g, u_g, v_g) \\ & (p_g, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + \mathbf{P}_{r_k}^t + p_{ij_k}^t = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} s p_n^t = S r^t, \\ & \sum_{n \in \mathcal{N}} s p_n^t + n p_n^t = S n^t \end{aligned}$$

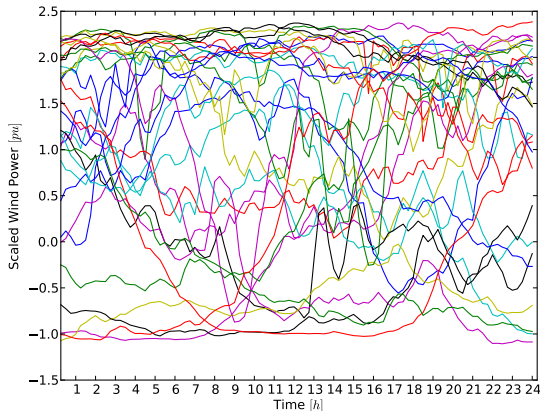
Unit Commitment Problem

Renewable generation: challenges



■ Forecast

■ System reserve



January 2014, ELIA - Belgium system

Stochastic Unit Commitment Formulation

Stochastic two-stage model



Given a set of realization: $\omega \in \Omega$

$$\begin{aligned} \min \quad & C_1(u_g, v_g) + \mathbb{E}[C_2(p_g)] \\ & (p_g(\omega), u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t(\omega) + \mathbf{p}_{r_k}^t(\omega) + p_{ij_k}^t(\omega) = \mathbf{L}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}(\omega)| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} sp_n^t(\omega) = Sr^t, \\ & \sum_{n \in \mathcal{N}} sp_n^t(\omega) + np_n^t(\omega) = Sn^t \end{aligned}$$

u_g, v_g is the (risk-neutral) commitment that minimizes the expected dispatch cost $\mathbb{E}[C_2(p_g)]$

Chance-Constrained Formulation

Scenarios $\omega \in \Omega$



Risk-averse UC and probabilistic reserve levels:

$$\begin{aligned} \min \quad & C(u_g, v_g, p_g) \\ & (p_g, sp, np, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \mathbb{P}\left[\sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \mathbf{L}_k^t - \mathbf{p}_{r_k}^t, k \in \mathcal{K}\right] \geq \pi, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \mathbb{P}\left[\sum_{n \in \mathcal{N}} sp_n^t = Sr^t + \alpha \mathbf{p}_r^t\right] \geq \rho, \\ & \mathbb{P}\left[\sum_{n \in \mathcal{N}} sp_n^t + np_n^t = Sn^t + \beta \mathbf{p}_r^t\right] \geq \rho \end{aligned}$$

(u_g, v_g, p_g) schedule determined by a risk-averse net-load operating level: $[L - p_r]_\pi$

(sp, np) system reserves allocated with a risk-averse renewable level: $[p_r]_\rho$

Chance-Constrained Formulation

Scenarios $\omega \in \Omega$



Risk-averse UC and probabilistic reserve levels:

$$\begin{aligned} \min \quad & C(u_g, v_g, p_g) \\ & (p_g, sp, np, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = w_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} sp_n^t = Sr^t + \alpha z^t, \\ & \sum_{n \in \mathcal{N}} sp_n^t + np_n^t = Sn^t + \beta z^t, \\ & w \in \mathcal{W}_\pi, z \in \mathcal{Z}_\rho \end{aligned}$$

Netload: $\mathcal{W}_\pi = \{w \in \mathbb{R}^{KT} : \mathbb{P}(\mathbf{L}_t^k - \mathbf{p}_{r_k}^t \leq w_k^t) \geq \pi\}$

Reserve renewable: $\mathcal{Z}_\rho = \{z \in \mathbb{R}^T : \mathbb{P}(\mathbf{p}_r^t \leq z^t) \geq \rho\}$

Decomposition Scheme



Introduce artificial variables: $\bar{p}_g, \bar{s}p, \bar{n}p, \bar{w}, \bar{z}$

$$\begin{aligned} \min \quad & C(u_g, v_g, p_g) \\ & (\bar{p}_g, \bar{s}p, \bar{n}p, u_g, v_g) \in \mathcal{C}_{\text{dyn}}^{\text{gen}} \cap \mathcal{C}_{\text{stat}}^{\text{gen}}, \\ & \sum_{n \in \mathcal{N}_k} p_{g_n}^t + p_{ij_k}^t = \bar{w}_k^t, k \in \mathcal{K}, \\ & |p_{ij_l}| \leq F_l, l \in \mathcal{B}, \\ & \sum_{n \in \mathcal{N}} sp_n^t = Sr^t + \alpha \bar{z}^t, \\ & \sum_{n \in \mathcal{N}} sp_n^t + np_n^t = Sn^t + \beta \bar{z}^t, \\ & p_g = \bar{p}_g, sp = \bar{s}p, np = \bar{n}p, \\ & w = \bar{w}, z = \bar{z}, \\ & w \in \mathcal{W}_\pi, z \in \mathcal{Z}_\rho \end{aligned}$$

Decomposition Scheme



Relax artificial constraints: $\lambda_p, \lambda_{sp}, \lambda_{np}, \lambda_w, \lambda_z$

$$L(p, w, z) = C(u_g, v_g, p_g) + \lambda_p^\top (p_g - \bar{p}_g) + \lambda_{sp}^\top (sp - \bar{s}p) \\ + \lambda_{np}^\top (np - \bar{n}p) + \lambda_w^\top (w - \bar{w}) + \lambda_z^\top (z - \bar{z}),$$

Dispatch - OPF

p_g, sp, np

\bar{w}, \bar{z}

Commitment

u_g, v_g

$\bar{s}p, \bar{n}p, \bar{p}_g$

Netload

$\mathbb{P}(\mathbf{L}_k^t - \mathbf{p}_r^t \leq w) \geq \pi$

$w \in \mathcal{W}_\pi$

Reserve

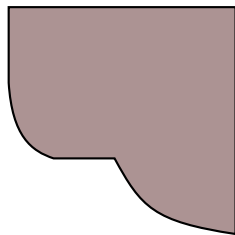
$\mathbb{P}(\mathbf{p}_r^t \leq z) \geq \rho$

$z \in \mathcal{Z}_\rho$

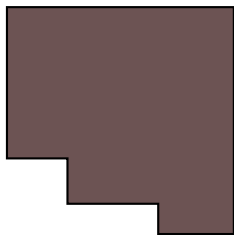
Stochastic subproblem



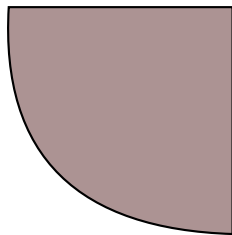
Feasible set example in 2D:



Mix. Uniform



Discrete



Gaussian

Given realizations: \mathcal{W}_π and \mathcal{Z}_ρ are non-convex (discrete).

Stochastic subproblem

Risk-averse netload



$$\mathcal{W}_\pi = \{w \in \mathbb{R}^{KT} : \mathbb{P}(\mathbf{L}_t^k - \mathbf{p}_{r_k}^t \leq w_k^t) \geq \pi\}$$

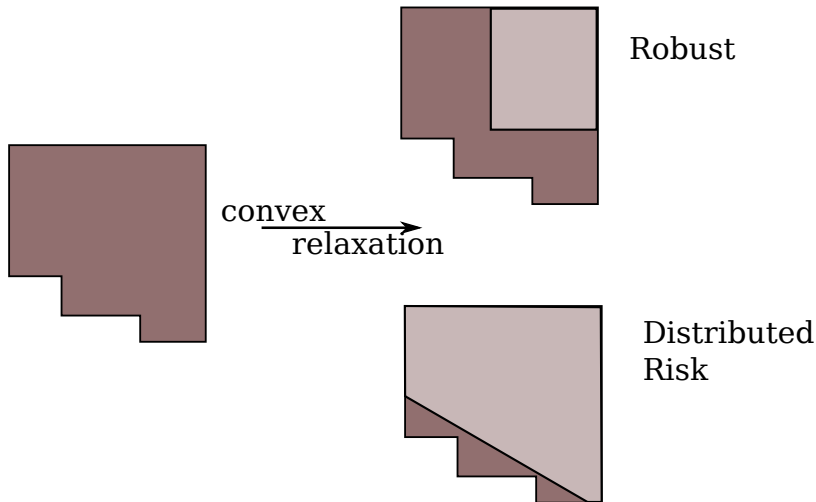
- Given a set of realizations $[\mathbf{L}_t^k - \mathbf{p}_{r_k}^t](\omega), \omega \in \Omega$ with probability $1/|\Omega|$
- Check the π -boundary: for every realization $e(\omega)$

$$e(\omega) = \begin{cases} 1 & [\mathbf{L}_t^k - \mathbf{p}_{r_k}^t](\omega) \leq w_k^t \\ 0 & \text{otherwise} \end{cases}$$

- $w \in \mathcal{W}_\pi$ if $\frac{1}{|\Omega|} \sum_{\omega \in \Omega} e(\omega) \geq \pi$

The subproblems: $\min\{\lambda_w^\top w | w \in \mathcal{W}_\pi\}$, $\min\{\lambda_z^\top z | z \in \mathcal{Z}_\rho\}$ are combinatorial problems, difficult to solve.

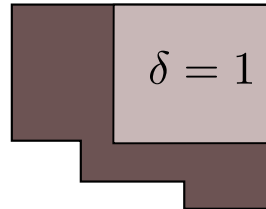
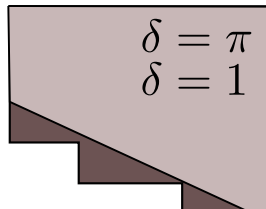
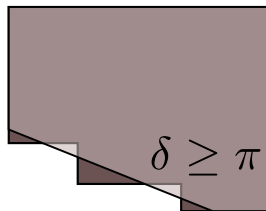
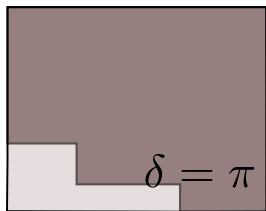
Relaxation Approach - Stochastic Subproblems



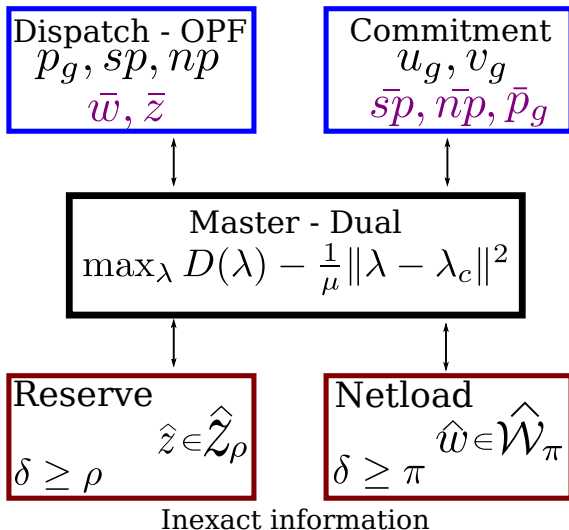
Relaxation Approach - Stochastic Subproblems



Scenarios $\omega \in \Omega$, $w(\omega)$, $z(\omega)$
 $\hat{w}_k^t = [w_k^t]_\delta$, $\hat{z}^t = [z^t]_\delta$, $\delta \geq \pi$



Approximate Bundle Method

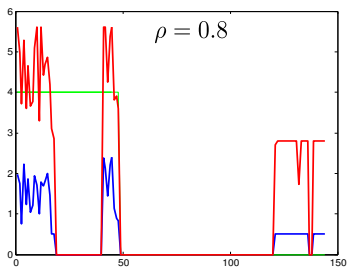
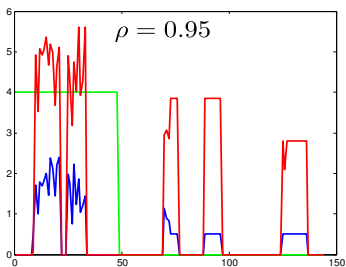
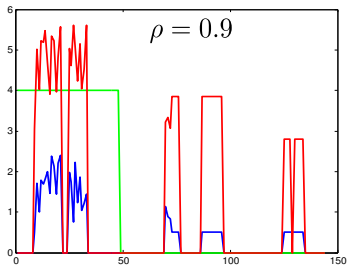
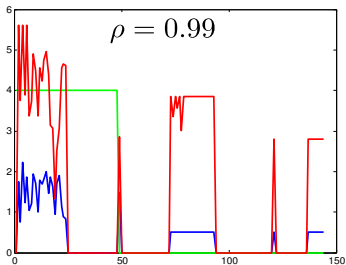


Results - IEEE30 bus system

Wind farms: 1,5,21,22,26. Generators:1,2,22,27,23. $\pi = 0.9$



— Generation — Non-spinning R. — Spinning R.

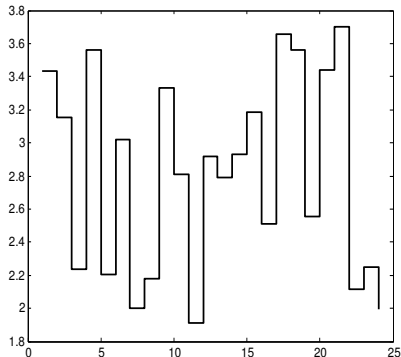


Results - IEEE30 bus system

Wind farms: 1,5,21,22,26. Generators:1,2,22,27,23. $\pi = 0.9$

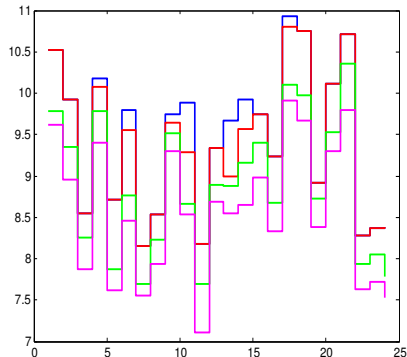


Deterministic reserve base:

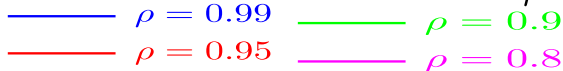


$9\%L$

Probabilistic reserve:



$0.09L + 0.15z_\rho$



Results - IEEE118 bus system

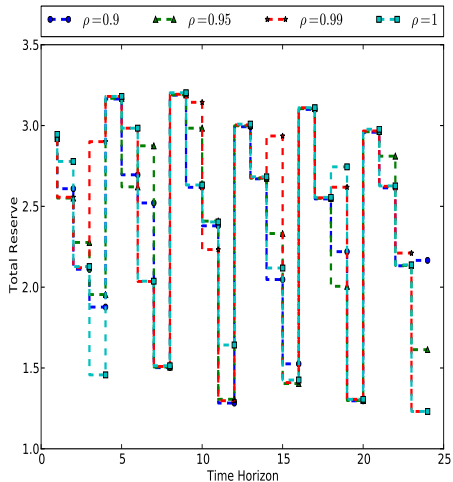
Wind farms: 53, 56, 32, 106, 6 – possible max generation 30%.

Nuclear: 30, 40, 37, 5.

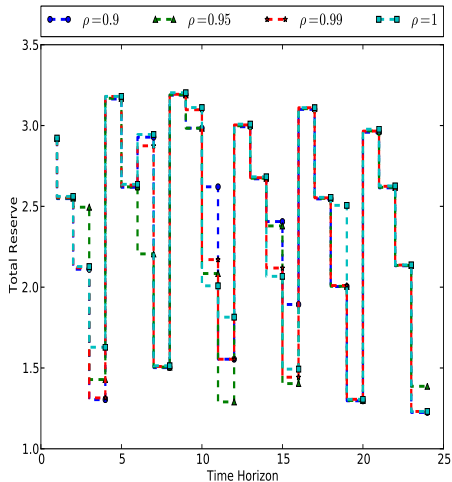
Committed Units: 5,6,11,12,14,20,21,22,25,26,28,29,30,37,38,40,45,46,54



Net-load $\pi = 0.9$



Net-load $\pi = 0.95$



Results - IEEE118 bus system

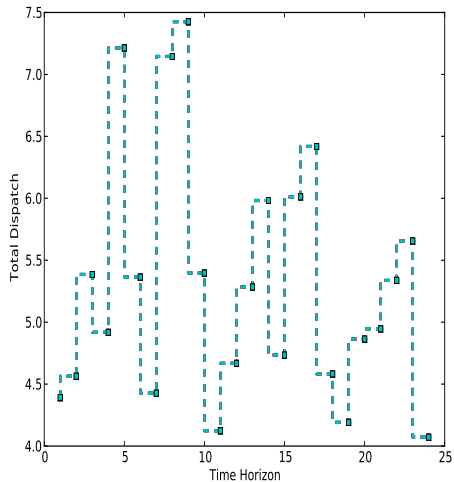
Wind farms: 53, 56, 32, 106, 6 – possible max generation 30%.

Nuclear: 30, 40, 37, 5.

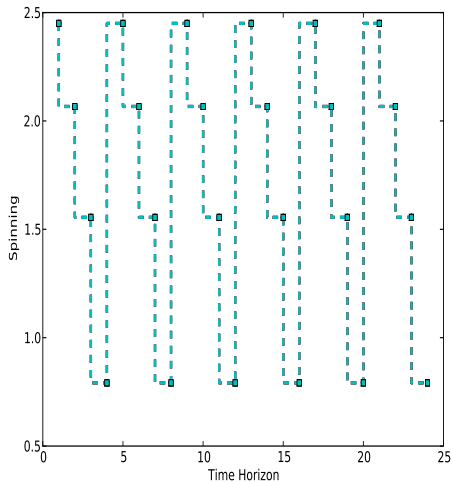
Committed Units: 5,6,11,12,14,20,21,22,25,26,28,29,30,37,38,40,45,46,54



Generation, $\pi = 0.95, \rho = 0.95$



Spinning R., $\pi = 0.9, \rho = 0.95$



Results - IEEE118 bus system

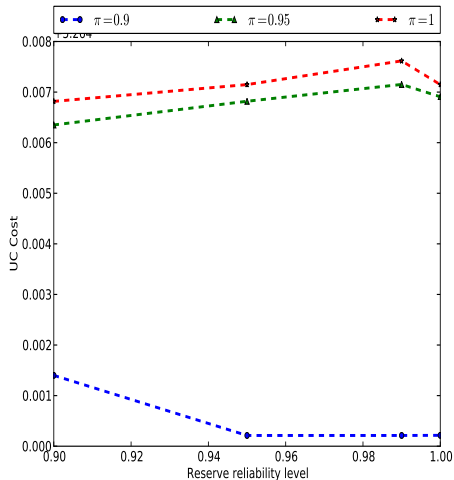
Wind farms: 53, 56, 32, 106, 6 – possible max generation 30%.

Nuclear: 30, 40, 37, 5.

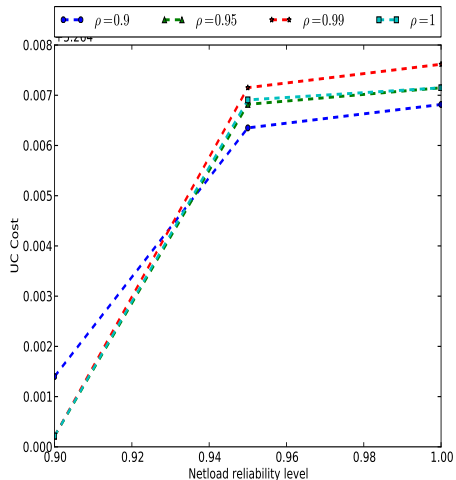
Committed Units: 5,6,11,12,14,20,21,22,25,26,28,29,30,37,38,40,45,46,54



Cost vs ρ -Reserve



Cost vs π -Net-load



The approach described has a number of advantages

- The risk-parameters can be set up by the user.
- The formulation is flexible and it can be implemented with OPF tools available - MATPOWER.
- Different number of realization can be used to estimate the percentiles at each period of time and node (where is needed)- important to accommodate forecast errors.
- Probabilistic reserves could be used to prepare the system for possible variations of wind power.
- The approach could be used to analyze safety renewable integration levels.
- The approach identifies risk-averse commitment



- Robust analysis of safety levels of renewable energy integration - UC
- Given UC and renewable integration levels: Refinement of dispatch
- Test the approach with different characterization of wind power: cluster representatives