

Review on Stochastic Methods Applied to Power System Operations with Renewable Energy

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Outline

- **Overview**
- **Addressing Uncertainty and Variability with Operating Reserves**
 - Probabilistic evaluation of reserves with renewable energy
 - Operating reserves in integration studies and industry
 - Stochastic scheduling formulations with implicit reserves
- **Stochastic Programming Formulations of the Unit Commitment Problem**
 - Stochastic programming based UC formulations
 - Uncertainty modeling
 - Modeling tools and solution algorithms
 - Test systems and performance comparison metrics
- **Other Unit Commitment Formulations under Uncertainty**
- **Industrial Applications**
- **Conclusion and Future Directions**



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■ Overview

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Literature Review Overview

- Focus on
 - Power system operations with renewable energy
 - Stochastic UC and ED methods from day-ahead scheduling to real-time operations.
 - Operating reserve strategies based on probabilistic methods
 - Uncertainty modeling and representation for operation scheduling
 - Case studies and industry adoption
- Overview statistics of papers

| Category | UC/ED | Operating Reserve | Uncertainty Modeling |
|----------|-------|-------------------|----------------------|
| Total | 119 | 48 | 24 |



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Summary – Operating Reserve Requirement Estimation and Acquisition

■ Thermal Systems

- Probabilistic estimates of LOLP
 - Based on load forecasting error and forced outage rate
 - Reserves in UC to meet reliability constraints
 - Update risk index based on UC and schedule reserve to meet constraints
 - Integrate outage distribution into UC formulation to meet LOLP constraints.
- Reserves in UC to minimize total system cost
 - Include reserve scheduling cost in the objective function
- Ensure that all selected contingencies can be met in UC

■ Thermal Systems with Renewables

- Meet probabilistic reliability target assuming Normal distribution for renewable forecast error
- Reserves in UC to minimize total system cost, including expected load shedding
- Reserve evaluation based on probabilistic wind power forecasts
- Operating reserve demand curves
- New reserve products

■ Stochastic scheduling with implicit reserves

- Bouffard et al. 2005, 2009; Morales et al. 2009; Papavasiliou et al. 2011



Summary - Probabilistic reserve estimates for thermal systems

| Application | Method | Reference |
|---|--|---|
| Probabilistic reserve estimates for thermal systems | Probabilistic estimates of LOLP | Anstine et al. (1963) [28] Garver (1966) [29] |
| | Reserves in UC to meet reliability constraints | Dillon et al. (1978) [30] Gooi et al. (1999) [31] Chattopadhyay and Baldick (2002) [32] Bouffard and Galiana (2004) [33] Ahmadi-Khatir et al. (2013) [36] |
| | Reserves in UC to minimize total system cost, including expected load shedding | Ortega-Vazquez and Kirschen (2007) [34] |
| | Ensure that all selected contingencies can be met in UC | Wang et al. (2009) [35] |



Summary - Probabilistic reserve estimates with renewable energy

| Application | Method | Reference |
|---|--|---|
| Probabilistic reserve estimates with renewable energy | Meet probabilistic reliability target assuming Normal distribution for renewable energy forecast error | Söder 1993 [17] Doherty and O'Malley 2005 [37] Makarov et al. 2008 2009 [38] [39] |
| | Reserves in UC to minimize total system cost, including expected load shedding | Ortega-Vazquez et al. 2009 [40] |
| | Reserve evaluation based on probabilistic wind power forecasts | Matos Bessa 2011 [41] Zhou and Botterud 2014 [42] |
| | Operating reserve demand curves | ERCOT 2013b [48] Zhou and Botterud 2014 [42] |
| | New reserve products | Wang, Hobbs 2014, 2015 [49] [50] |
| | Reserves in integration studies and industry developments | Ackerman et al. 2007 [43] Ela et al. 2011 [44] Holttinen et al. 2013 [45] Enernex 2010 [24] GE Energy 2010 [25] Lew et al. 2013 [26] Mills et al. 2013 [46] ERCOT 2013a [47] ERCOT 2013b [48] Ellison et al. 2012 [56] Ela et al. 2014 [15] |

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Stochastic Programming Formulations

- A general stochastic programming formulation

$$\min \left\{ C(u) + E_{\zeta \in H} (F(u', g, \zeta) | Au \leq b_u, u \in U, W^{\zeta} g^{\zeta} \leq b_g^{\zeta}, u' = u, \forall \zeta \in H) \right\}$$

- A specific UC formulation with uncertainty from wind power

$$\text{Min} \sum_s \text{prob}_s \cdot \left\{ \sum_{t,i} [FC_{t,i}^s + C(RNS_t^s) + C(ENS_t^s)] \right\} + \sum_{t,i} SC_{t,i}$$

$$\sum_i \text{gen}_{\text{thermal},i,t}^s + \text{gen}_{\text{renewable},t}^s = \text{load}_t - ENS_t^s, \quad \forall t, s$$

$$\sum_i r_{\text{thermal},i,t}^s \geq \alpha_{sr} (OR_{\text{reg},t} + OR_{\text{renewable},t}^s) - RNS_t^s, \quad \forall t, s$$



Summary - Stochastic UC formulations

■ Extension from traditional UC formulation

- Minimizing expected operating cost (over all scenarios with associated probabilities)
- Combination of stochastic UC and operating reserve constraints
- Risk indices associated to different events
- Emissions

■ Other Variations

- Rolling basis decision making
- Sub-hourly dispatch constraints

■ Hybrid formulations

- Stochastic optimization and interval optimization combined
- Stochastic optimization and robust optimization



Summary - Probabilistic wind power forecasting

■ General Problem

$$f_p(p_{t+k}|X = x_{t+k|t}) = \frac{f_{P,X}(p_{t+k}, x_{t+k|t})}{f_X(x_{t+k|t})}$$

■ Methods based on Input

- NWP point forecasts based
- Power output point forecasts based
- NWP ensembles based

■ Performance Metrics

- Calibration
- Sharpness
- Skill Score

■ Uncertainty Representation

- Scenario tree/bundles
- Scenario set generated by Monte Carlo Simulation
- Scenario screening/selection



References - Stochastic UC formulations

| Applications | Specification | References |
|---|---|---|
| Extension from traditional UC formulation | Minimizing expected operating cost | Papavasiliou and Oren, (2013a) [64] |
| | Combination of stochastic UC and operating reserve constraints | Kalantari, et. al. (2013) [65] Ruiz, et. al. (2008) [72], (2009a) [62], (2009b) [73], (2010) [63] Zhou, et. al. (2013) [74] |
| | Risk indices associated to different events | Li, et. al. (2007) [61] Zhang, et. al. (2014) [66] Wu, et. al. (2008) [67] |
| | Emissions | Wu, et. al. (2007) [60] |
| Multi-stage decision making | Rolling basis decision making | Meibom, et. al. (2008) [75] Tuohy, et. al. (2008) [76], (2009) [77], Ela, et. al. (2010) [78] |
| Hybrid formulations | Stochastic optimization and interval optimization combined | Dvorkin, et. al. (2015) [80] |
| | Stochastic optimization and robust optimization | Zhao and Guan, (2013) [138] |
| Uncertainty Representation | Scenario tree/bundles | Li, et. al. (2007) [61] Takriti, et. al. (1996) [57], (2000) [59] Wu, et. al. (2007) [60], (2008) [67], Shiina and Birge, (2004) [69] Nowak, et. al. (2000) [122] Meibom, et. al. (2007) [131], (2010) [75], (2011) [130] Pappala, et. al. (2009) [126] Tuohy, et. al. (2008) [76] Ela, et. al. (2010) [78] Sturt and Strbac, (2011) [70] |
| | Scenario set | Ruiz, et. al. (2008) [72], (2009a) [62], (2009b) [73], (2010) [63] Papavasiliou and Oren, (2013b) [119] Nowak, et. al. (2005) [121] Carøe, et. al. (1998) [58], (1997) [117] Wang, et. al. (2008) [120] Huang, et. al. (2014) [124] Wu and Shahidehpour (2014), [81] Kalantari, et. al. (2013) [65] Dvorkin, et. al. (2015) [80] Wang, et. al. (2013) [79] Constantinescu, et. al. (2011) [116] |
| | Scenario screening/selection | Papavasiliou and Oren, (2013a) [64] Feng, et. al. (2013) [71] |

Reference - Probabilistic wind power forecasting

| Input data | References |
|------------------------------------|---|
| NWP point forecasts based | Bremnes (2004) [82], (2006) [84] Lange (2005) [83] Jeon and Taylor, (2012) [85] Kou, et. al. (2013) [86] Messner, et. al. (2014) [87] |
| Power output point forecasts based | Nielsen (2006) [88] Pinson (2006) [89], (2012) [95] Bludszuweit (2008) [90] Juban, et. al. (2007) [91] Møller, et. al. (2008) [92] Carpinone, et. al. (2010) [93] Bessa, et. al. (2012) [94] Sideratos and Hatziargyriou, (2012) [96] Haque, et. al. (2014) [97] Wan, et. al. (2014) [98] Li, et. al. (2015) [99] |
| NWP ensembles based | Nielsen, et. al. (2006) [100], (2007) [101], Pinson and Madsen, (2009) [102] Möller, et. al. (2013) [103] |



Summary - Solution methods for stochastic UC

- Extensive Form with Commercial Solver
 - Cplex/Gurobi
 - Others
 - FICO Xpress
 - CBC
- Decomposition Based Methods
 - By scenarios
 - By generation unit
 - By stage/time period
- Others
 - Heuristic-based: PSO



Reference - Solution methods for stochastic UC

| Methods | Specification | References |
|---------------------------------------|-----------------------------|---|
| Extensive Form with Commercial Solver | Cplex | Kalantari, et. al. (2013) [65] Zhang, et. al. (2014) [66] Ruiz, et. al. (2008) [72], (2009) [73] Dvorkin, et. al. (2015) [80] Zhao, et. al. (2013) [115]. |
| | CBC | Constantinescu, et. al. (2011) [116] |
| | FICO Xpress | Sturt and Strbac, (2012) [70] |
| Decomposition Based | By scenarios | Carøe, et. al. (1998) [58], (1997) [117] Wu, et. al. (2008) [67], (2012) [118] Papavasiliou and Oren, (2013a) [64], (2013b) [119] Wang, et. al. (2013) [79] Wang, et. al. (2008) [120] Nowak, et. al. (2005) [121] Goez, et. al. (2008) [125] |
| | By generation unit | Shiina and Birge, (2004) [69] Nowak and Römisch, (2000) [122] Huang, et. al. (2014) [124] |
| | By stage/time period | Takriti, et. al. (1996) [57] Schneider, et. al. (2013) [123] |
| Others | Particle swarm optimization | Pappala et. al (2009) [126] |



Summary – Test systems

- **Various IEEE test systems**

- IEEE Reliability Test System
- IEEE 118-bus system

- **Real world systems**

- WECC-240 system
- Reduce CAISO system
- CAISO interconnection with the WECC
- Eastern Interconnection
- National-wide power systems or utility companies



Summary - Cost performance of stochastic UC methods

- **Economic metrics**

- Expected cost savings
- Committed conventional generation capacity and operating reserve
- Renewable energy utilization
- Number of startups from thermal units

- **Reliability metrics**

- unserved energy and reserve

- **Examples**

| Metrics | Cost Saving | References |
|-----------------------|--------------------------------------|--------------------------------------|
| Operating cost saving | 0.82% to 1.22% | Ruiz, et. al. (2009) [62] |
| | 1% to 1.8% | Ruiz, et. al. (2010) [63] |
| | 1.93% to 2.77% | Papavasiliou and Oren, (2013a) [64] |
| | 5.4% | Papavasiliou and Oren, (2013b) [119] |
| | 1.6% | Gröwe, et. al. (1995) [127] |
| | 0.39% to 1.18% | Takriti, et. al. (1996) [57] |
| | 4% | Takriti, et. al. (2000) [59] |
| | 1.26% | Wang, et. al. (2008) [120] |
| | 2.8% to 3.8% | Pappala, et. al. (2009) [126] |
| | 0.6% | Tuohy, et. al. (2008) [76] |
| 1% | Constantinescu, et. al. (2011) [116] | |



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Other Unit Commitment Formulations under Uncertainty

■ Robust optimization based UC

$$\min_{\mathbf{x}} (\mathbf{c}^T \mathbf{x} + \max_{\mathbf{d} \in D} \min_{\mathbf{y} \in \Omega(\mathbf{x}, \mathbf{d})} \mathbf{b}^T \mathbf{y})$$

$$s. t. \mathbf{F}\mathbf{x} \leq \mathbf{f}, \mathbf{x} \text{ is binary}$$

$$\Omega(\mathbf{x}, \mathbf{d}) =$$

$$\{\mathbf{H}\mathbf{y}(\mathbf{d}) \leq \mathbf{h}(\mathbf{d}), \mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{y}(\mathbf{d}) \leq \mathbf{g}, \mathbf{I}_u \mathbf{y}(\mathbf{d}) = \mathbf{d}\}$$

■ Formulations

– First introduce robust optimization into UC model with wind power (Zhang and Guan 2009)

– Variations:

- Include n-k contingency into uncertainty set
- Multi-stage robust UC
- Consider nonparametric correlations between nodal demands
- Stochastic robust model, Accommodate multiple uncertainty sets
- Robust UC with demand response
- Consider non-anticipativity constraints in the dispatch process
- Minimax regret model

■ Solution Methods

– Column and constraint generation

– Benders decomposition and outer approximation



Reference – Robust Optimization based Unit Commitment Formulation Under Uncertainty

| Application | Specification | Reference |
|--|---|--|
| Robust optimization based UC | First introduce robust optimization into UC model with wind power | Zhang and Guan 2009 [146] Jiang et al. 2013 [148] |
| | Include n-k contingency into uncertainty set | Street et al. (2011) [147] Xiong and Jirutitijaroen (2012) [149] Wang, et. al. (2013) [153] Matos Bessa (2011) [41] |
| | Multi-stage robust UC | Zhao et al. (2013) [152] |
| | Combined stochastic and robust UC formulation | Zhao and Guan (2013) [139] |
| | Consider nonparametric correlations between nodal demands | Moreira et al. (2014) [158] |
| | Stochastic robust model, Accommodate multiple uncertainty sets | An and Zeng (2015) [159] Liu et al. (2015) [163] |
| | Robust UC with demand response | Zhao et al. (2013) [152] Liu and Tomsovic (2015) [162] |
| | Consider non-anticipativity constraints in the dispatch process | Lorca and Sun (2014) [160] Lorca et al. (2014) [161] |
| | Minimax regret model | Jiang et al. (2013) [164] |
| | Column and constraint generation | Zhao and Zeng (2012) [150] An and Zeng (2015) [159] Lee et al. (2014) [156] Liu et al. (2015) [163] |
| | Benders decomposition and outer approximation | Bertsimas et al. (2013) [151] Zhao and Guan (2013) [140] Moreira et al. (2014) [158] Zhao et al. (2013) [152] |
| | Column generation, Dynamically include critical transmission line constraints | Lee et al. (2014) [156] |
| Different method to construct uncertainty sets | Guan and Wang (2014) [154] | |



Other Unit Commitment Formulations under Uncertainty

- Chance constrained Based UC

$$\begin{aligned} & \min_{x,y} c^T x + b^T y + E(P(x, y, \xi)) \\ \text{s. t.} \quad & Fx \leq f, x \text{ is binary} \\ & Hy \leq h \\ & Ax + By \leq g \\ & I_u y(d) = d \\ & \Pr(G(x, y, \xi) \leq 0) \geq 1 - \epsilon \end{aligned}$$

- Other Miscellaneous UC Formulation with Uncertainty

- Stochastic dynamic programming
- Fuzzy constraints/objective function

- Summary

| Application | Specification | Reference |
|---|--|---|
| Chance Constrained based UC | First introduce wind into chanced constrained UC model | Ozturk (2003) [142] Ozturk et al. (2004) [143] |
| | Combined sample average approximation (SAA) algorithm | Wang et al. (2012) [144] |
| | alpha-quantile measure to determine the confidence level | Pozo et al. (2013) [145] |
| Other Miscellaneous UC Formulation with Uncertainty | fuzzy set | Hosseini, et. al. (2007) [165] Venkatesh et al. (2008) [166] |
| | Stochastic dynamic programming | Hargreaves and Hobbs (2012) [134] Schneider et. al. (2013) [124] |
| | | |

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Industrial applications

■ MISO

- Overcome Computational Challenges on Large Scale SCUC Problems
- A Probabilistic Optimization Reliability Assessment Commitment Framework
- Operational and Practical Considerations for Stochastic Unit Commitment Solutions
- Applying Robust Optimization to MISO Look-ahead Unit Commitment

■ ISO-NE

- Study of Two-Stage Robust Unit Commitment
- Wind Dispatch Using Do-Not-Exceed Limit

■ ERCOT

- Optimizing Wind Generation in ERCOT Nodal Market



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Conclusion and Future Directions

■ Conclusions

- The **stochastic UC problem** has received most of the attention among researchers, but new approaches for **probabilistic estimates of operating reserves** have also been proposed to account for the stochastic nature of transmission and generation outages.
- The main focus in the literature on stochastic scheduling and dispatch is on **cost savings** and **reliability impacts**. There is also increasing attention to **market implications**.
- Most of the studies report **operating cost savings** from using stochastic formulations, especially if potential savings on penalties for load or reserve curtailment are considered.
- There is no **standard framework** and **metrics** to compare the pros and cons of different operational strategies.
- **Industry adaptation** of probabilistic methods for operational decisions is still limited, but there is increasing interest in the topic.



Conclusion and Future Directions

■ Directions

- More **systematic testing** and **comparison** of different operational strategies, accounting for a larger set of the real-world issues, constraints, and potential future regulatory policies in power system and electricity market operations.
- A closer investigation of the **interaction between explicit operating reserve requirements** imposed by traditional reserve constraints **and the implicit reserves** provided by stochastic scheduling and dispatch formulations.
- Further investigation of the **potential implications for pricing and market incentives** under stochastic UC and ED, with the goal of providing efficient signals for operations and investments for all market participants.
- Further refinements of methods for **probabilistic forecasting, scenario generation and reduction**, as critical inputs to stochastic methods for power system operations.
- **Testing on real-world and large-scale systems**. More utility companies and ISOs should get involved to validate the performance of stochastic methods. Industry feedback and suggestions for improvements in research grade tools and algorithms will contribute to pave the way forward to more economic and reliable power systems with large share of renewables.



Q & A

