

Optimal Power Flow (OPF) in Large-scale Power Grid Simulation

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06/24/2010

Outline

- **I. Introduction and challenges of optimal power flow**
- **II. Three topics on optimal power flow**
 - Optimal power flow with post-contingency correction
 - Optimal power flow with discrete control variables and two stage MIP
 - Optimal power flow considering other energy infrastructures
- **III. Summary and future work**

Introduction to optimal power flow

■ Applications

- Optimal production cost simulation with network constraints
- Minimal network loss in power grid
- Market clearing and locational marginal price calculation

■ Mathematical formulation

- Continuous linear or nonlinear optimization problem
- Stochastic optimization

■ Algorithms

- Linear programming and successive linear programming
- Interior point method
- Quadratic programming
- Heuristic method

Three challenges in optimal power flow

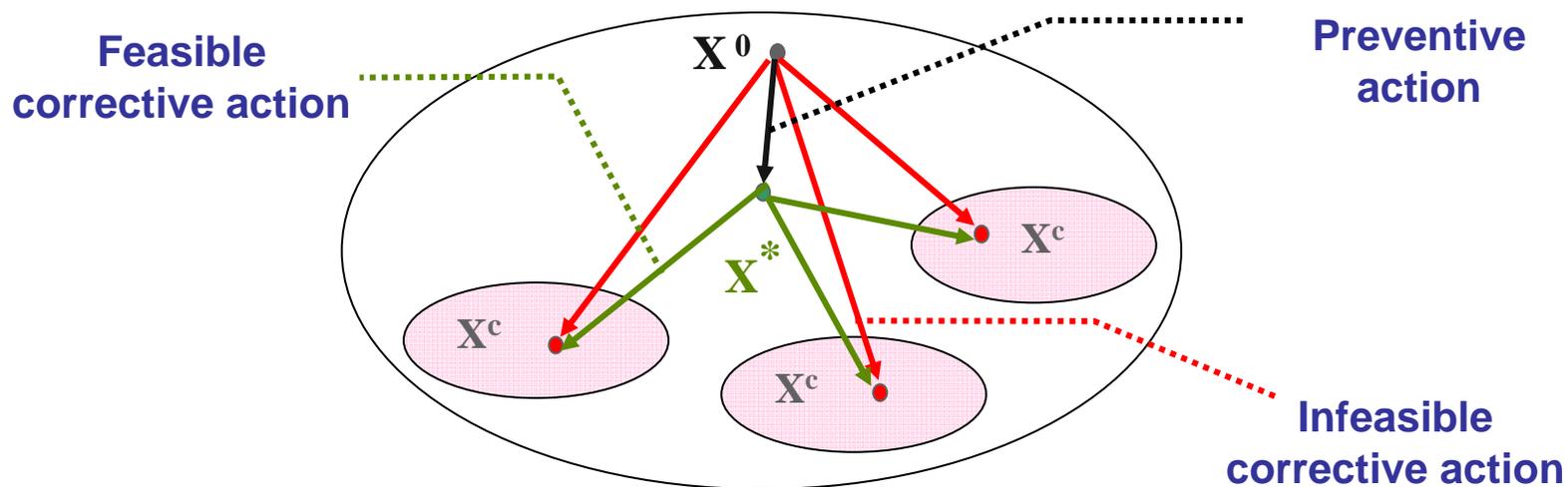
- **Optimal power flow with post-contingency correction**
 - Difficulties: Huge number of contingency cases $N-1\dots N-k$
- **Optimal power flow with discrete control variables and two-stage mixed integer linear and nonlinear problem (MIP)**
 - Quick start units
 - Discrete control variables in networks
 - Smart grid operations (energy storages, transmission switching)
- **Optimal power flow considering other energy infrastructures**
 - Security interdependency (eg., natural gas network)
 - Coordinated operation and planning

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Corrective and preventive actions in power system operations

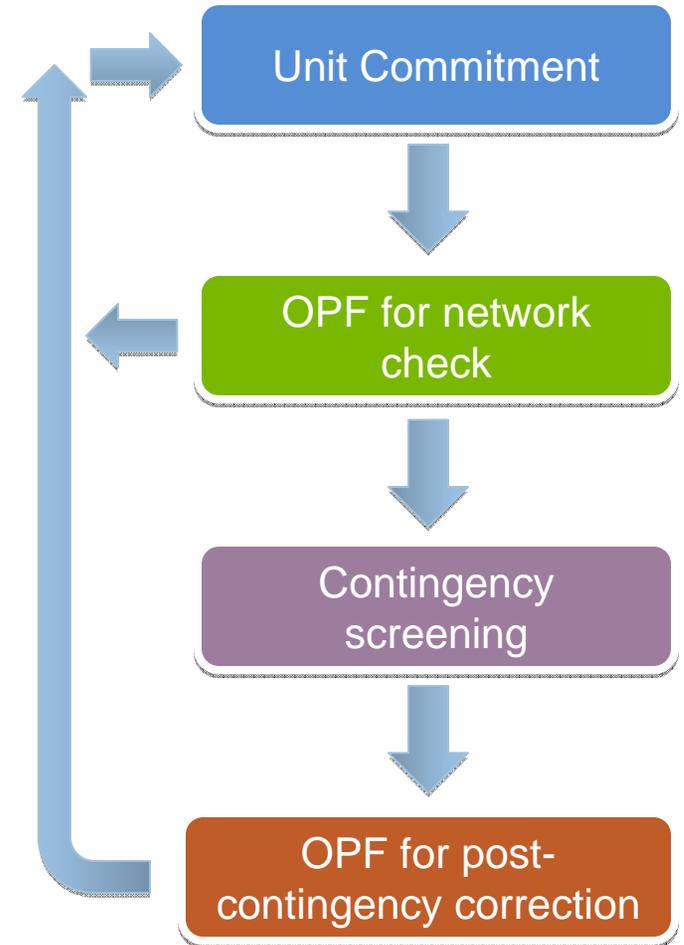
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Optimal power flow (OPF) with post-contingency correction

Contingency Cases	Number
WECC N-1	~ 20,000
WECC N-2	~154,000
WECC N-3	~10 ⁸
WECC N-4	~10 ¹²

- **Huge number of contingencies**
 - Contingency screening (CS)
 - Degree of severity
- **Inclusion of probability into CS**
 - Probability of outage



Contingency screening

- Extensive use of sparse linear algebra

$$Y = LDU$$

- Fast decoupled AC power flow

$$\Delta\theta^{(k)} = -[B']^{-1} \frac{\Delta P}{U}, \quad \Delta U^{(k)} = -[B'']^{-1} \frac{\Delta Q}{U}$$

- Compensation theory

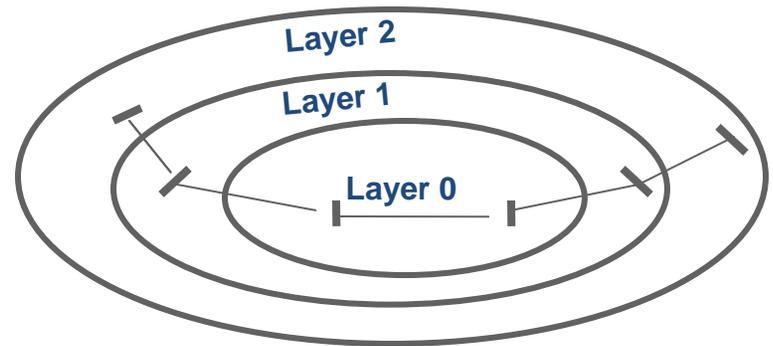
- Branch outages can be considered as minor change of Y (B' or B'') matrices. An efficient way is to add additional elements into matrices B' and B''.

$$B' = B' + M\delta y'M^T$$

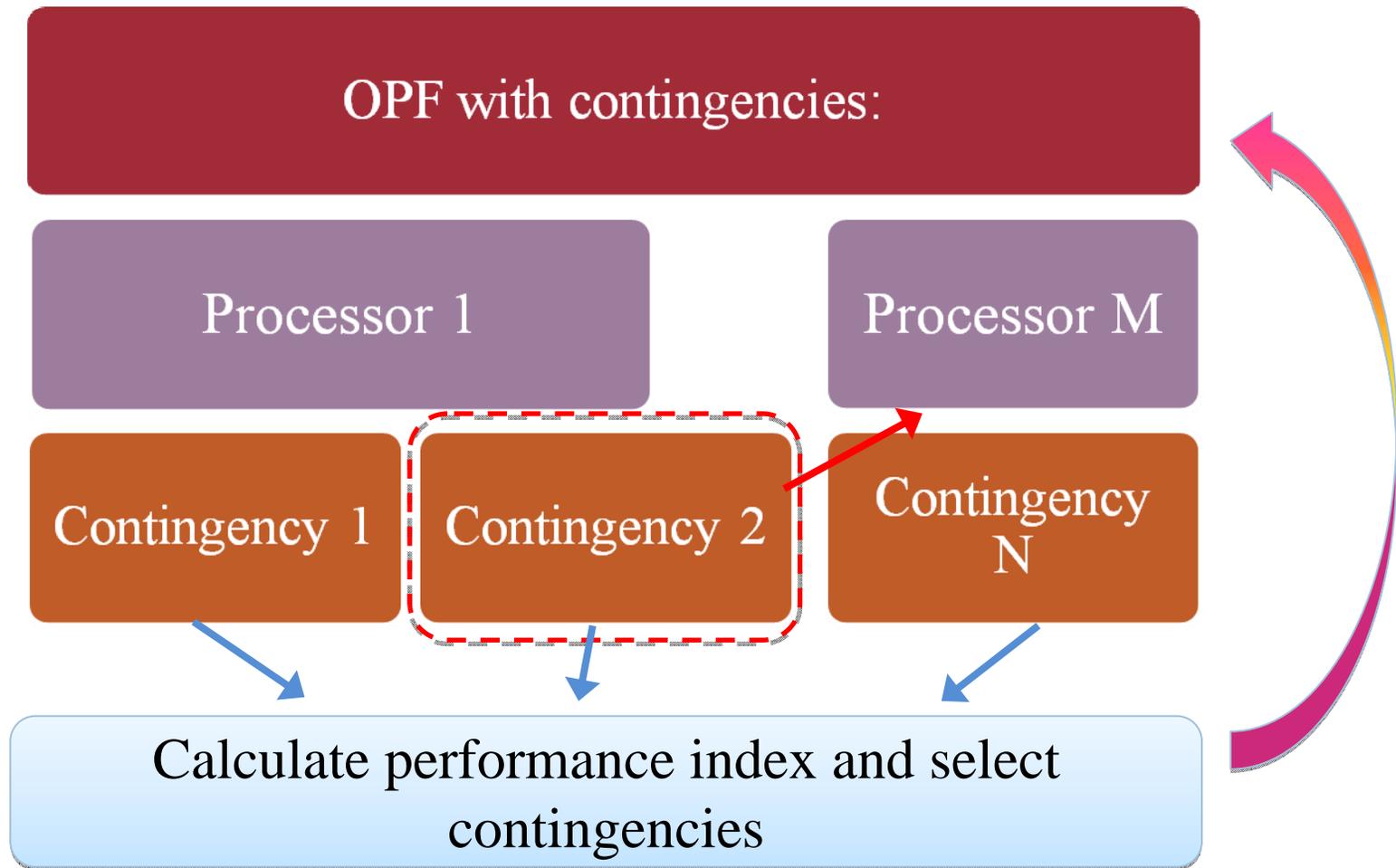
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Contingency screening (CS)

- **Concentric relaxation or bounding**
 - An outage only has a limited geographical effect on steady-state power flow.
- **1P1Q or 2P2Q method**
- **Multi-area power flow**
 - Partitioning of admittance matrix
- **Consider probability of outage into CS**
 - It is difficult to consider all N-1 to N-k contingencies.
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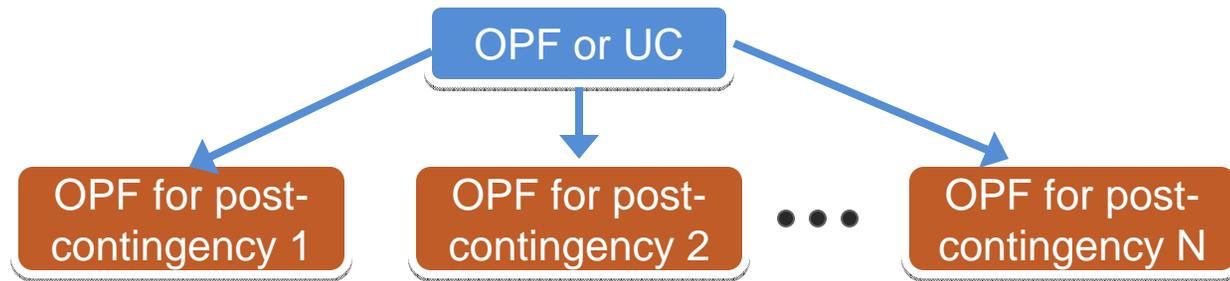


Parallelism for contingency screening

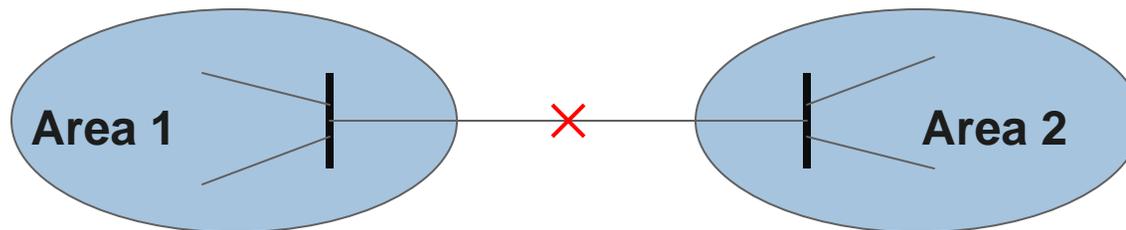


Parallelism of OPF after dual or L-shaped decomposition

- Contingency check can be implemented in a parallel way



- Multi-area optimal power flow
 - Relax power flow in the tie-line or voltage variables in the boundary bus
 - Dual decomposition by Lagrangian relaxation



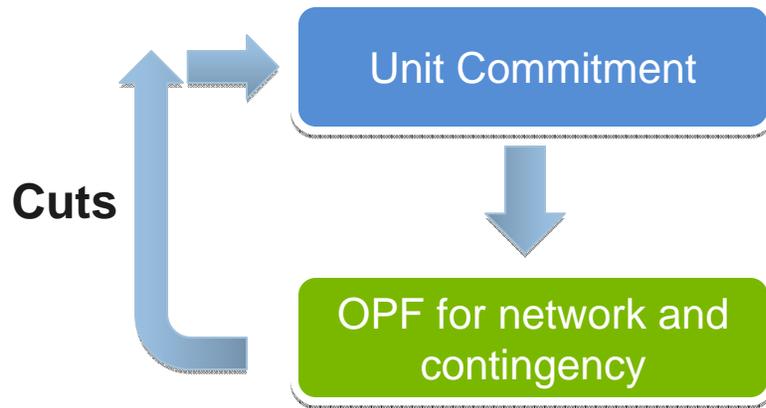
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Optimal power flow with discrete variables

- **Discrete control variables in power network**
 - Quick- start unit,
 - Transmission switching, transformer tap-changer, capacitors,
 - Smart grid flexible operations
- **Mixed integer linear or nonlinear programming (MIP)**
 - Optimal power flow with discrete control variables has a similar mathematic structure to the unit commitment problem. Both of them are MIP.
 - Branch and cut method
 - Mathematic decomposition (e.g. Benders decomposition)

Two stage MIP



Traditional

Current

MIP

MIP

Continuous linear
or nonlinear
programming

MIP

■ Original Problem

$$\text{Min} \quad \mathbf{c} \cdot \mathbf{x}$$

Objective

$$\text{S.t.} \quad \mathbf{A} \cdot \mathbf{x} \leq \mathbf{b}$$

First-stage constraints

$$\mathbf{E}^c \cdot \mathbf{x} + \mathbf{F} \cdot \mathbf{y}^c \leq \mathbf{h}^c$$

Second-stage constraints for each contingency

$$\mathbf{x} \in \mathbb{R}^{m1} \quad \{0,1\}^{n1} \quad \mathbf{y}^c \in \mathbb{R}^{m2} \quad \{0,1\}^{n2}$$

L-shaped structure and decomposition

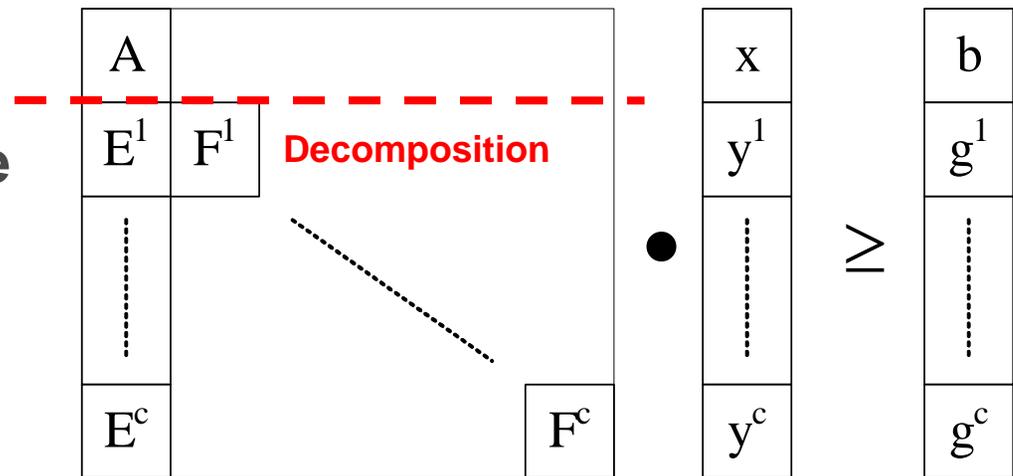
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- Feasibility of corrective action check subproblems for each contingency

$$\begin{aligned} \text{Min} \quad & \mathbf{w}^c(\hat{\mathbf{x}}) = \mathbf{1}^T \cdot \mathbf{S}^c \\ \text{S.t.} \quad & \mathbf{F}^c \mathbf{y}^c - \mathbf{S}^c \leq \mathbf{h}^c - \mathbf{E}^c \hat{\mathbf{x}} \end{aligned}$$

L-shaped structure



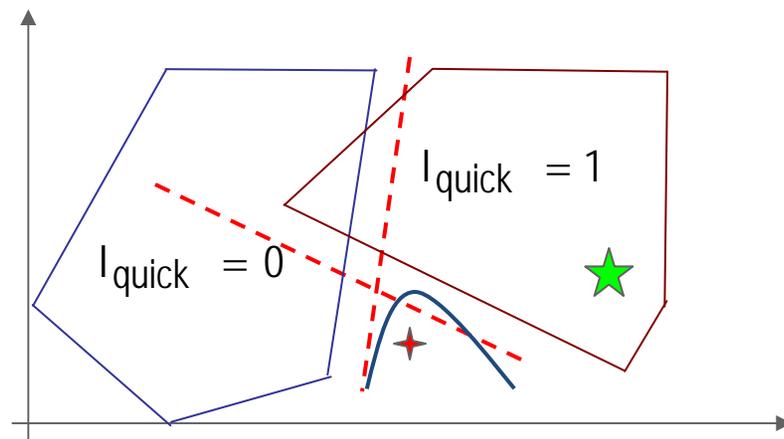
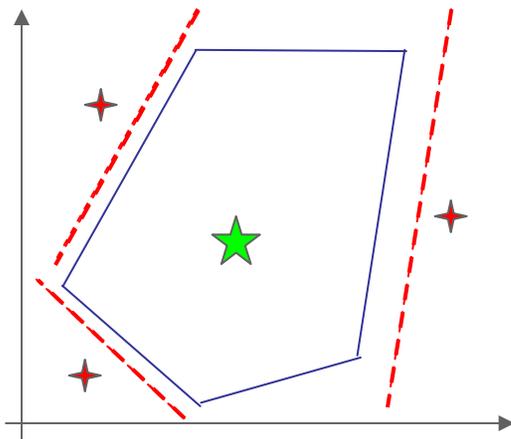
Global optimal solution

- Without quick-start units, second-stage subproblems are LP (or successive LP)

$$\text{Min } w^{c,k}(\hat{x}^k) = \mathbf{1}^T \cdot \mathbf{s}^c$$

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- With quick-start units, second-stage subproblems are MIP, and its feasible region is **non-convex**.



Extended Benders decomposition for SCUC with post-contingency correction

- With quick-start units, second-stage subproblems are MIP
 - A straightforward approach is to enumerate all possible combinations of quick-start units' commitments in each contingency subproblem
 - If the objective value is zero for at least one combination, this subproblem is feasible, and no feasibility cut is necessary
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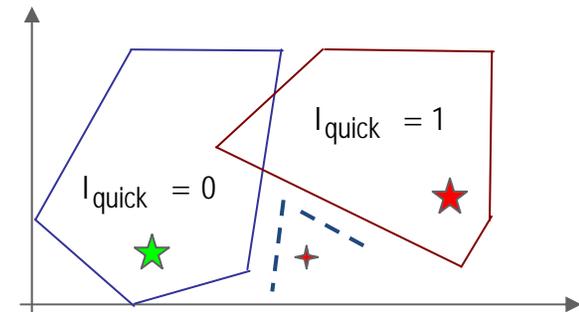
$$\text{S.t.} \quad \mathbf{F}^c \mathbf{y}^c + \mathbf{S}^c \leq \mathbf{h}^c - \mathbf{E}^c \hat{\mathbf{x}}^k$$

$$\mathbf{y}_i^c = \hat{\mathbf{y}}_i^c \quad \mathbf{y}_i^c \in \{0,1\}^{n_2}$$

$$\mathbf{w}^{c,k}(\hat{\mathbf{x}}^k) - (\boldsymbol{\pi}^{c,k})^T \cdot \mathbf{E}^c \cdot (\mathbf{x} - \hat{\mathbf{x}}^k) - M \cdot (1 - \delta_n) \leq 0$$

$$\sum_n \delta_n = 1$$

$\boldsymbol{\pi}^{c,k}$



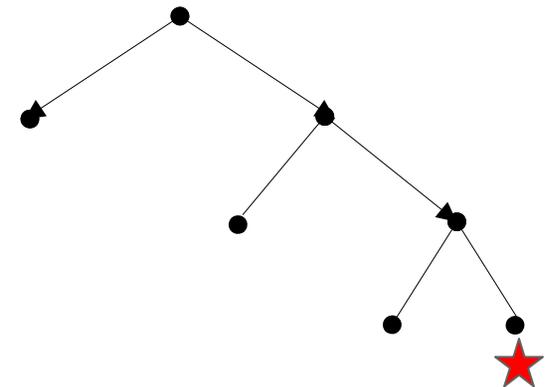
Extended Benders decomposition for SCUC with post-contingency correction (continued)

- Since the second stage subproblems may be feasible after post-contingency corrections, feasibility cuts are formed only in infeasibility case. Optimality cuts are not required in this two-stage MIP.
- The process can be accelerated by using branch and cut method

$$w^{c,k}(\hat{x}) - (\pi^{c,k})^T \cdot E^c \cdot (x - \hat{x}^k) - M \cdot (1 - \delta_n) \leq 0$$

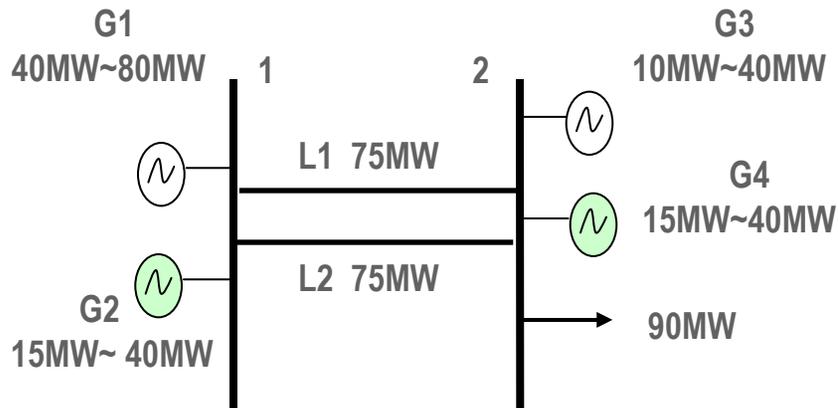


$$\sum_n \delta_n = 1$$



A simple example

System



Contingency

Contingency	Equipment Outage	Load (MW)
1	G3	85
2	L2	93

- G1 and G3: they can be re-dispatched by 5 MW
 - **G2 and G4**: 30MW quick-start capability

- **Three different models and solutions for quick-start units in post-contingency correction subproblems**
 - 1) **MIP-LP model**: Relax integer variables in the second stage (approximation model). **G2 and G4 (0~40MW)**
 - 2) **Two-stage MIP model**: solve MIP in the second stage. Then fix integer variables in the second stage and form cuts from resulted LP.
 - 3) **Two-stage MIP model**: Extended Benders decomposition

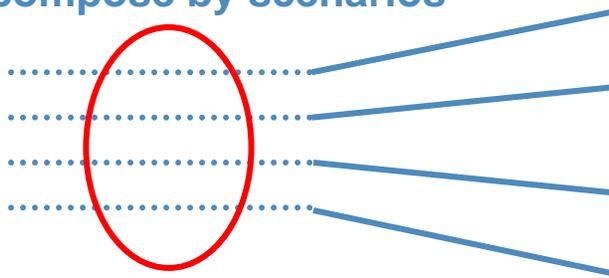
- **Results:**
 - 1) **Infeasible for contingency correction**
 - 2) **Suboptimal**
 - 3) **Global optimal**

Other two stage MIP in power grid simulation

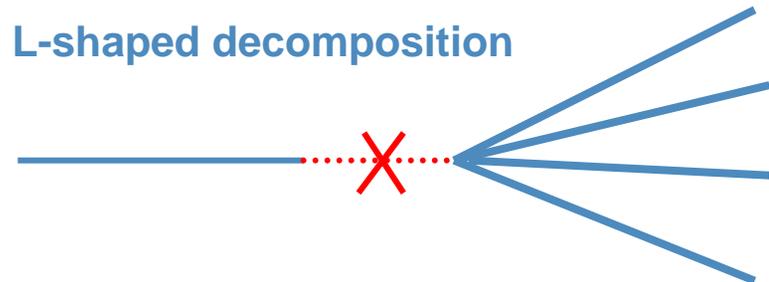
Problem	First Stage	Second Stage
UC with network constraints	UC	Transmission constraints
Contingency-based SCUC	UC with pre-contingency transmission constraints	Post- contingency transmission constraints
Two-stage stochastic SCUC	Decision costs and constraints	Recourse costs and constraints
Two stage distribution network expansion	Decision of building new distribution line	Reconfiguration

- Dual decomposition and L-shaped (Benders) decomposition: pros and cons**

Decompose by scenarios



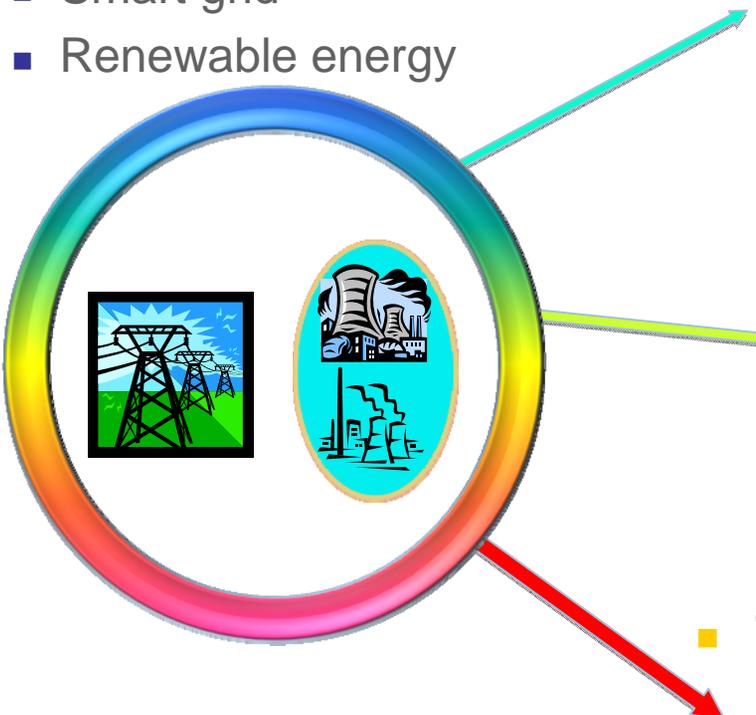
L-shaped decomposition



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Optimal power flow with other energy infrastructures

- **Electricity infrastructure**
 - Smart grid
 - Renewable energy
 - **Natural gas transmission system**
 - Texas: 70% electricity are generated by natural gas units
 - Coordination between peaking units and renewable energy
 - **River and cascaded hydropower station**
 - Hydrothermal coordinated scheduling
 - **Transportation**
 - PHEV, Vehicle to Grid
 - Coal, Oil transportation
- 

Coupled energy flow

- **Steady-state integrated model have been proposed in the last decade**
- **Different energy flows travel via different speed through infrastructures**
 - Power flow: very small time constant
 - Water flow: large time constant
 - Natural gas flow: medium time constant
 - transportation flow: medium time constant
- **Use dynamic model instead of steady-state linear or nonlinear algebraic equations**
- **Potential application: security monitoring, reliability evaluation, planning**

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Summary and future work at Argonne

- **Three challenges of optimal power flow in power grid simulation are addressed.**
- **Contingency screening method is nested into unit commitment and optimal power flow with post-corrective action. Contingency analysis and optimal power flow study can be extended to a large-scale power system with parallel computing. Probability of outage cloud be included into contingency screening process.**

Summary and future work at Argonne

- **Discrete variables will bring more difficulties in solving optimal power flow especially for two-stage MIP problems. Dual decomposition and L-shaped (Benders) decomposition techniques can be used to divide the original problem into several small-scale subproblems.**
- **Energy infrastructures are highly coupled, it is envisioned that using an integrated method to model optimal power flow and other energy flows together is necessary.**

Reference

- [1] Jianhui Wang, Mohammad Shahidehpour, and Zuyi Li, “Contingency- Constrained Reserve Requirements in Joint Energy and Ancillary Services Auction,” *IEEE Transactions on Power Systems*, Vol.24, No.3, pp.1457-1468, Aug. 2009
- [2] Cong Liu, Mohammad Shahidehpour, Yong Fu and Zuyi Li “Security-Constrained Unit Commitment with Natural Gas Transmission Constraints,” *IEEE Transactions on Power Systems*, Vol. 24, No. 3, Aug. 2009.
- [3] Lei Wu, Mohammad Shahidehpour, and Cong Liu “MIP-based Post-Contingency Corrective Action with Quick-Start Units,” *IEEE Transactions on Power Systems*, Vol. 24, No. 4, Nov. 2009.
- [4] Cong Liu, Mohammad Shahidehpour, and Lei Wu, “Extended Benders Decomposition for Two-Stage SCUC,” *IEEE Transactions on Power Systems*, Vol. 25, No. 2, May. 2010.

Thank You for Attention!

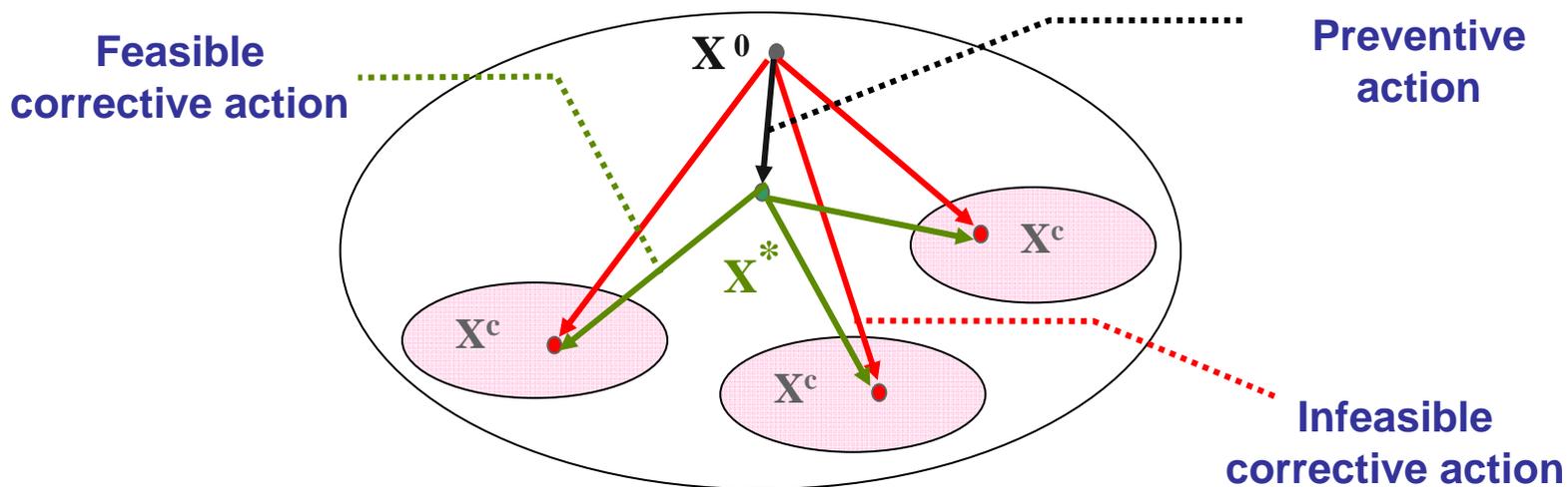
Question?

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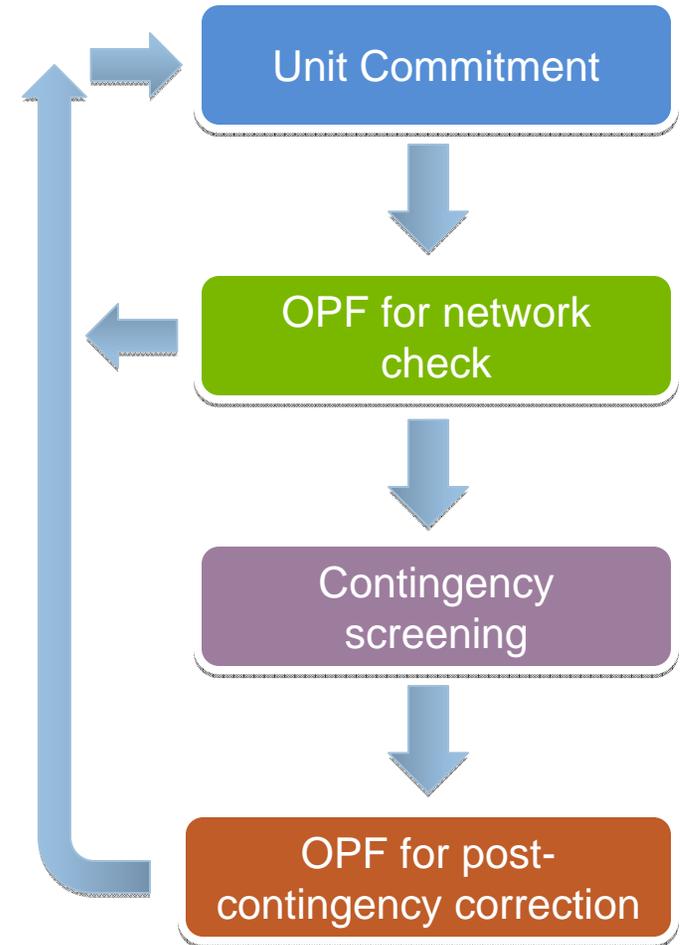
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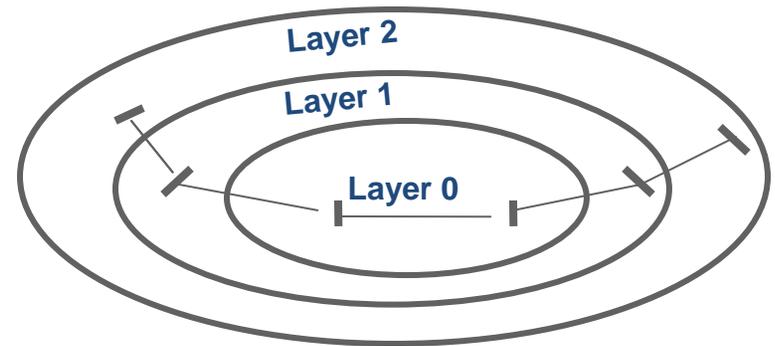
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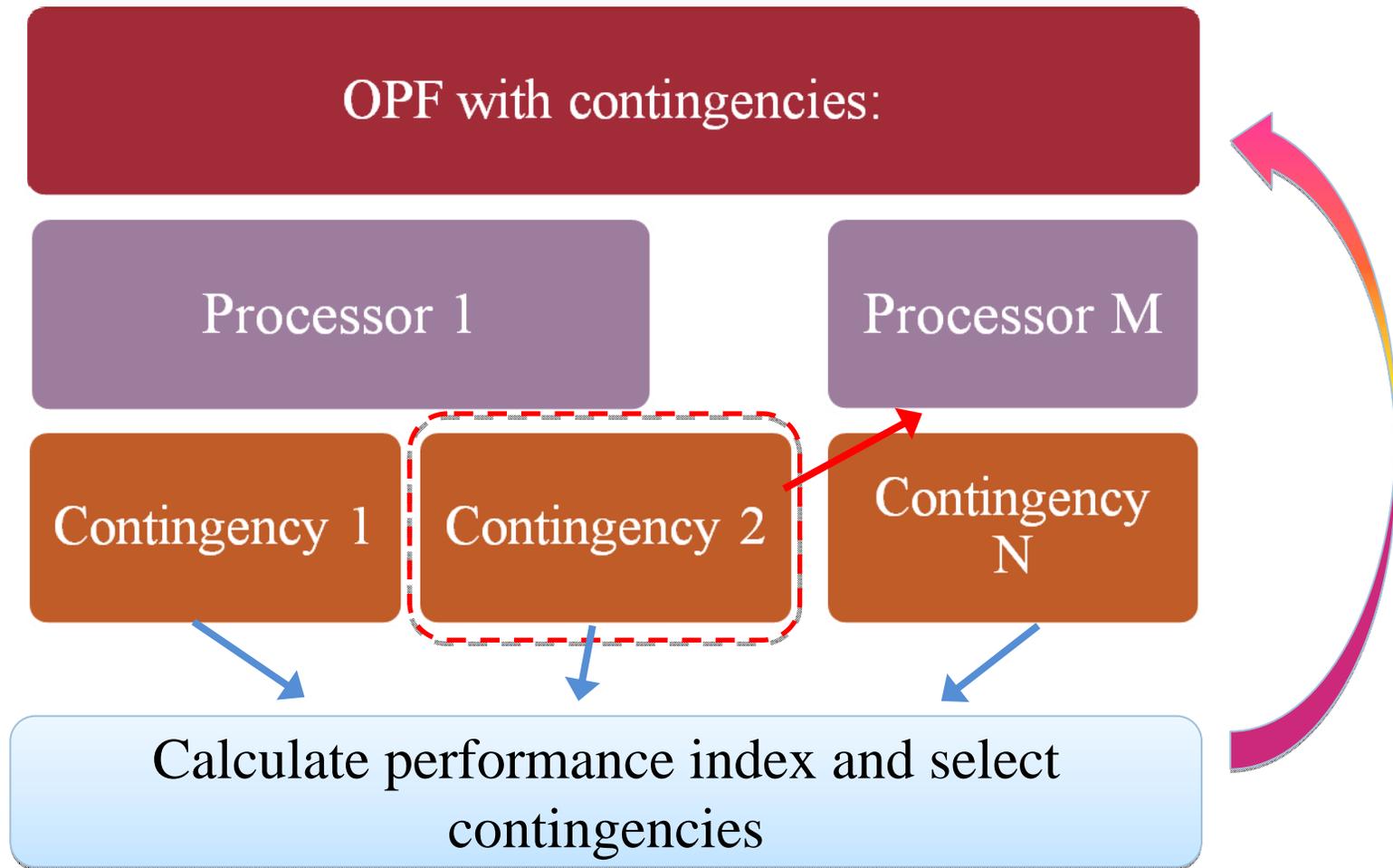
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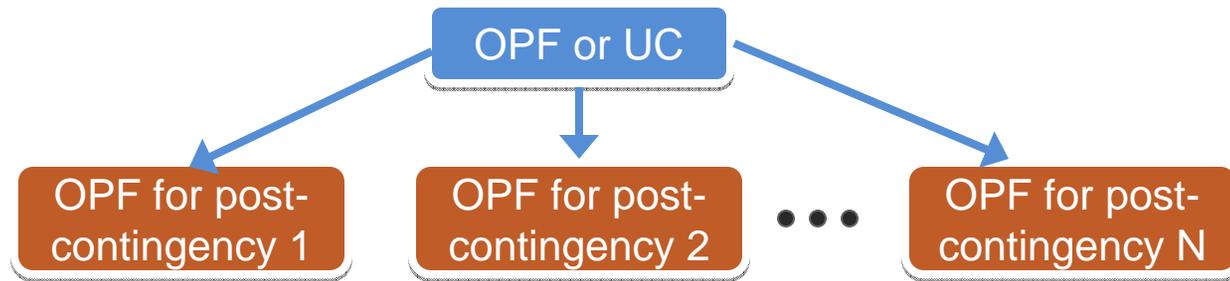


Parallelism for contingency screening

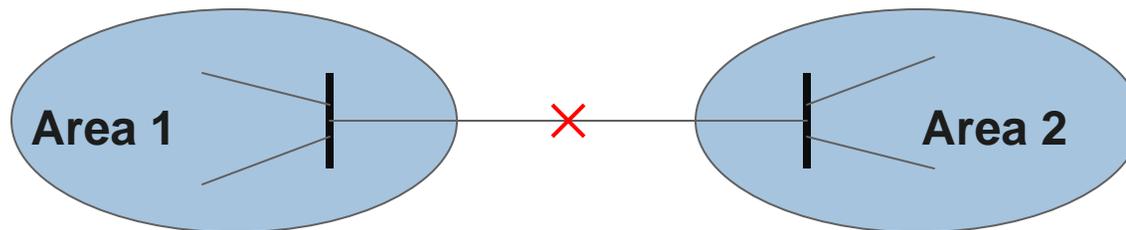


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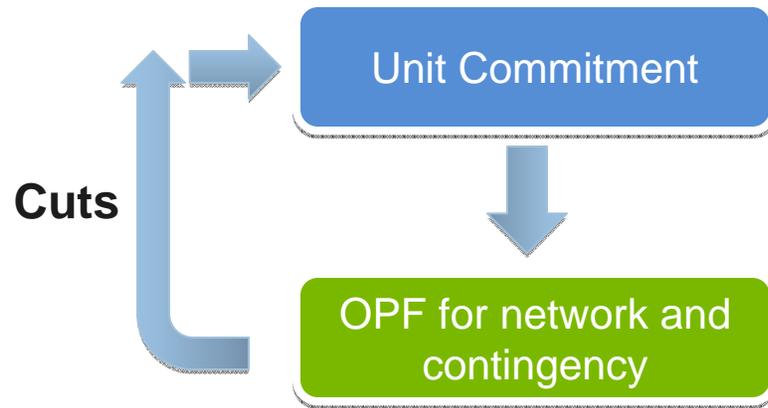
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MIP

Continuous linear
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MIP

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Second-stage constraints for each contingency

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L-shaped structure and decomposition

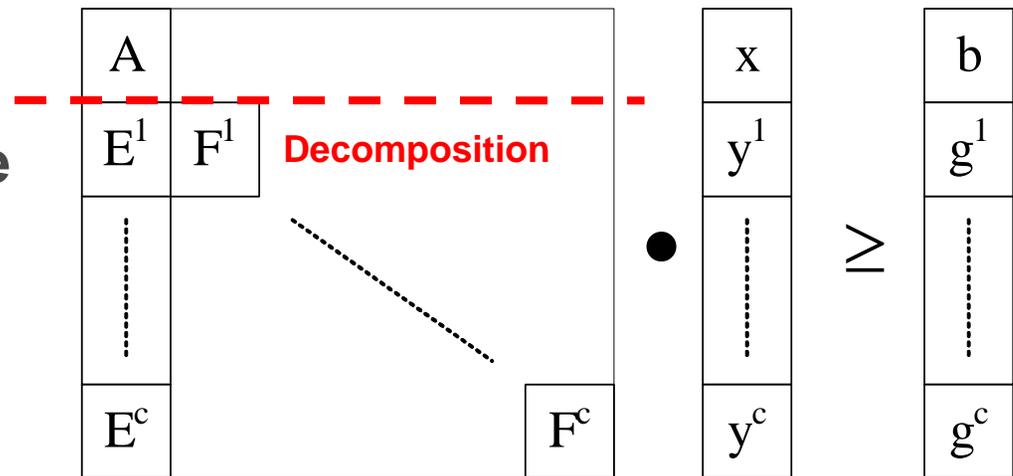
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L-shaped structure



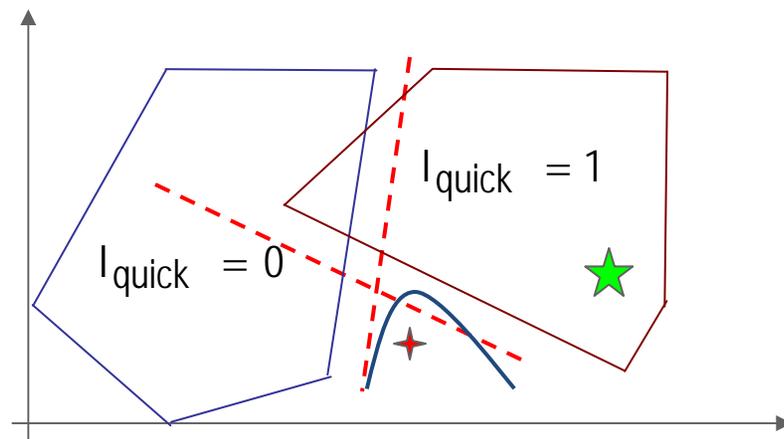
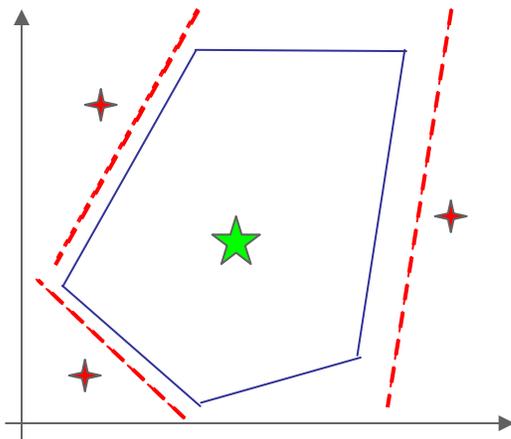
Global optimal solution

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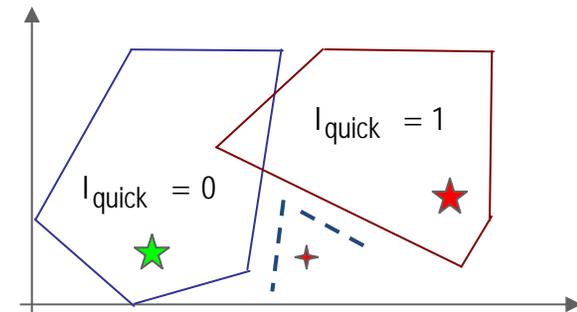
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$\boldsymbol{\pi}^{c,k}$



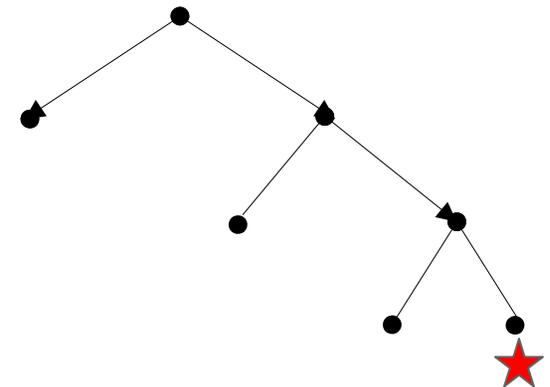
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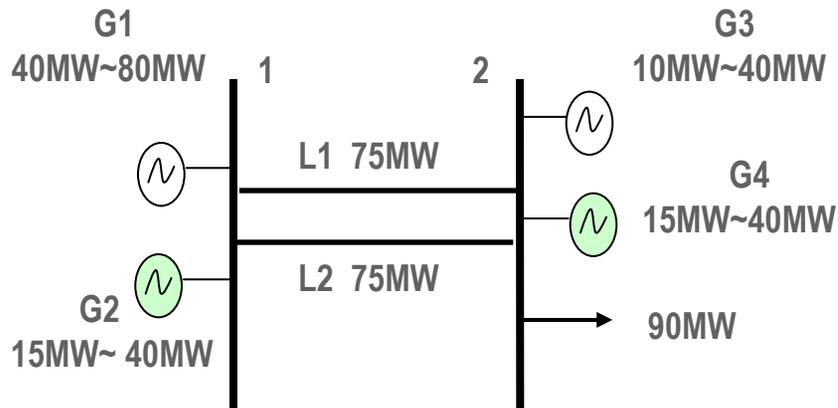


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- G1 and G3: they can be re-dispatched by 5 MW
 - **G2 and G4**: 30MW quick-start capability

- **Three different models and solutions for quick-start units in post-contingency correction subproblems**
 - 1) **MIP-LP model**: Relax integer variables in the second stage (approximation model). **G2 and G4 (0~40MW)**
 - 2) **Two-stage MIP model**: solve MIP in the second stage. Then fix integer variables in the second stage and form cuts from resulted LP.
 - 3) **Two-stage MIP model**: Extended Benders decomposition

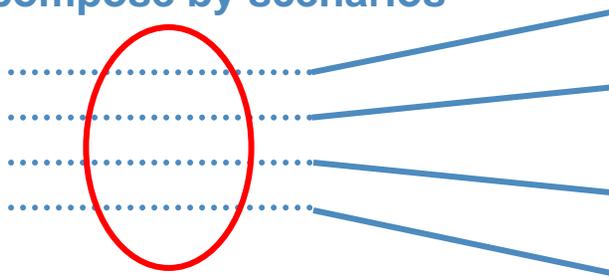
- **Results:**
 - 1) **Infeasible for contingency correction**
 - 2) **Suboptimal**
 - 3) **Global optimal**

Other two stage MIP in power grid simulation

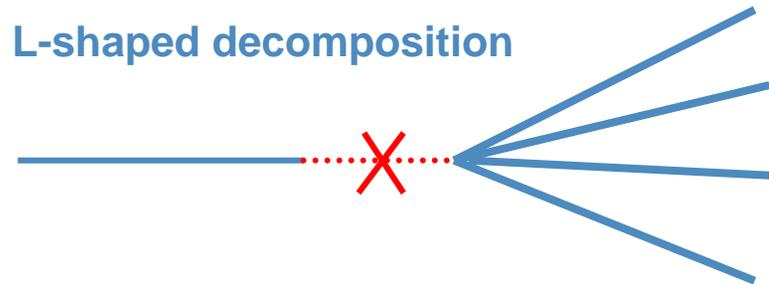
Problem	First Stage	Second Stage
UC with network constraints	UC	Transmission constraints
Contingency-based SCUC	UC with pre-contingency transmission constraints	Post- contingency transmission constraints
Two-stage stochastic SCUC	Decision costs and constraints	Recourse costs and constraints
Two stage distribution network expansion	Decision of building new distribution line	Reconfiguration

- Dual decomposition and L-shaped (Benders) decomposition: pros and cons**

Decompose by scenarios



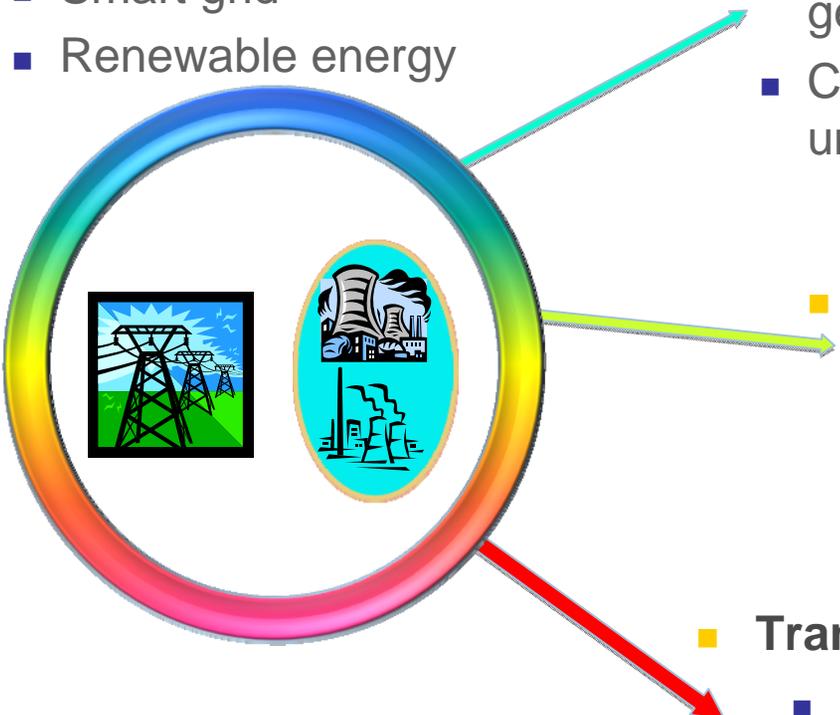
L-shaped decomposition



Outline

- I. Introduction and challenges of optimal power flow
- **II. Three topics on optimal power flow**
 - Optimal power flow with post-contingency correction
 - Optimal power flow with discrete control variables and two stage MIP
 - **Optimal power flow considering other energy infrastructures**
- III. Summary and future work

Optimal power flow with other energy infrastructures

- **Electricity infrastructure**
 - Smart grid
 - Renewable energy
 - **Natural gas transmission system**
 - Texas: 70% electricity are generated by natural gas units
 - Coordination between peaking units and renewable energy
 - **River and cascaded hydropower station**
 - Hydrothermal coordinated scheduling
 - **Transportation**
 - PHEV, Vehicle to Grid
 - Coal, Oil transportation
- 

Coupled energy flow

- **Steady-state integrated model have been proposed in the last decade**
- **Different energy flows travel via different speed through infrastructures**
 - Power flow: very small time constant
 - Water flow: large time constant
 - Natural gas flow: medium time constant
 - transportation flow: medium time constant
- **Use dynamic model instead of steady-state linear or nonlinear algebraic equations**
- **Potential application: security monitoring, reliability evaluation, planning**

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Summary and future work at Argonne

- **Three challenges of optimal power flow in power grid simulation are addressed.**
- **Contingency screening method is nested into unit commitment and optimal power flow with post-corrective action. Contingency analysis and optimal power flow study can be extended to a large-scale power system with parallel computing. Probability of outage cloud be included into contingency screening process.**

Summary and future work at Argonne

- **Discrete variables will bring more difficulties in solving optimal power flow especially for two-stage MIP problems. Dual decomposition and L-shaped (Benders) decomposition techniques can be used to divide the original problem into several small-scale subproblems.**
- **Energy infrastructures are highly coupled, it is envisioned that using an integrated method to model optimal power flow and other energy flows together is necessary.**

Reference

- [1] Jianhui Wang, Mohammad Shahidehpour, and Zuyi Li, “Contingency- Constrained Reserve Requirements in Joint Energy and Ancillary Services Auction,” *IEEE Transactions on Power Systems*, Vol.24, No.3, pp.1457-1468, Aug. 2009
- [2] Cong Liu, Mohammad Shahidehpour, Yong Fu and Zuyi Li “Security-Constrained Unit Commitment with Natural Gas Transmission Constraints,” *IEEE Transactions on Power Systems*, Vol. 24, No. 3, Aug. 2009.
- [3] Lei Wu, Mohammad Shahidehpour, and Cong Liu “MIP-based Post-Contingency Corrective Action with Quick-Start Units,” *IEEE Transactions on Power Systems*, Vol. 24, No. 4, Nov. 2009.
- [4] Cong Liu, Mohammad Shahidehpour, and Lei Wu, “Extended Benders Decomposition for Two-Stage SCUC,” *IEEE Transactions on Power Systems*, Vol. 25, No. 2, May. 2010.

Thank You for Attention!

Question?