

# MODEL-PREDICTIVE CASCADE MITIGATION IN ELECTRIC POWER SYSTEMS WITH STORAGE AND RENEWABLES

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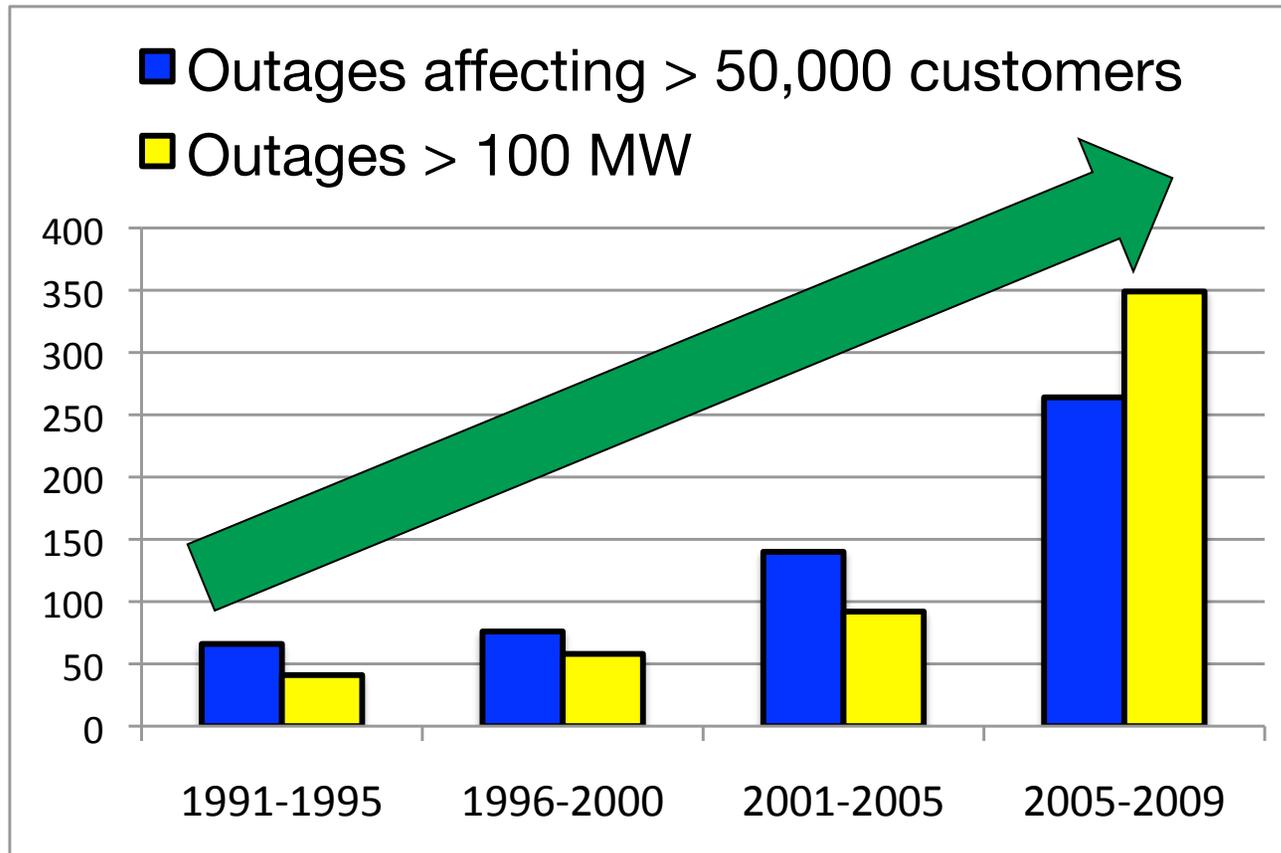
The New York Times



Source: Vincent Laforet / The New York Times Photo Archives.

# Was 2003 Blackout atypical?

**US electric infrastructure is operating closer to its limits**



**Example:** PJM system at all-time winter high in Jan 2014, *warned of rolling blackouts*

# Can't we just build our way out?

- **New high-voltage lines are expensive**
  - Up to \$2,000,000 per mile
- **Construction is protracted process**
  - Takes up to 10 years (planning + construction)

**→ Need to do better with what we already have**

# What kind of grid do we have?

## In the 20<sup>th</sup> century

- Supply follows demand
- Large thermal generation
- Limited renewable generation



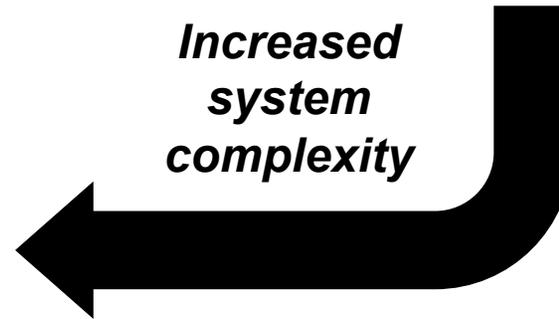
## For the 21<sup>st</sup> century

- Some demand can follow supply
- Increased renewable generation
- New technologies
  - Improved controllability
  - Improved observability
- Energy storage
  - tighter temporal coupling

## Human grid operators @ PJM

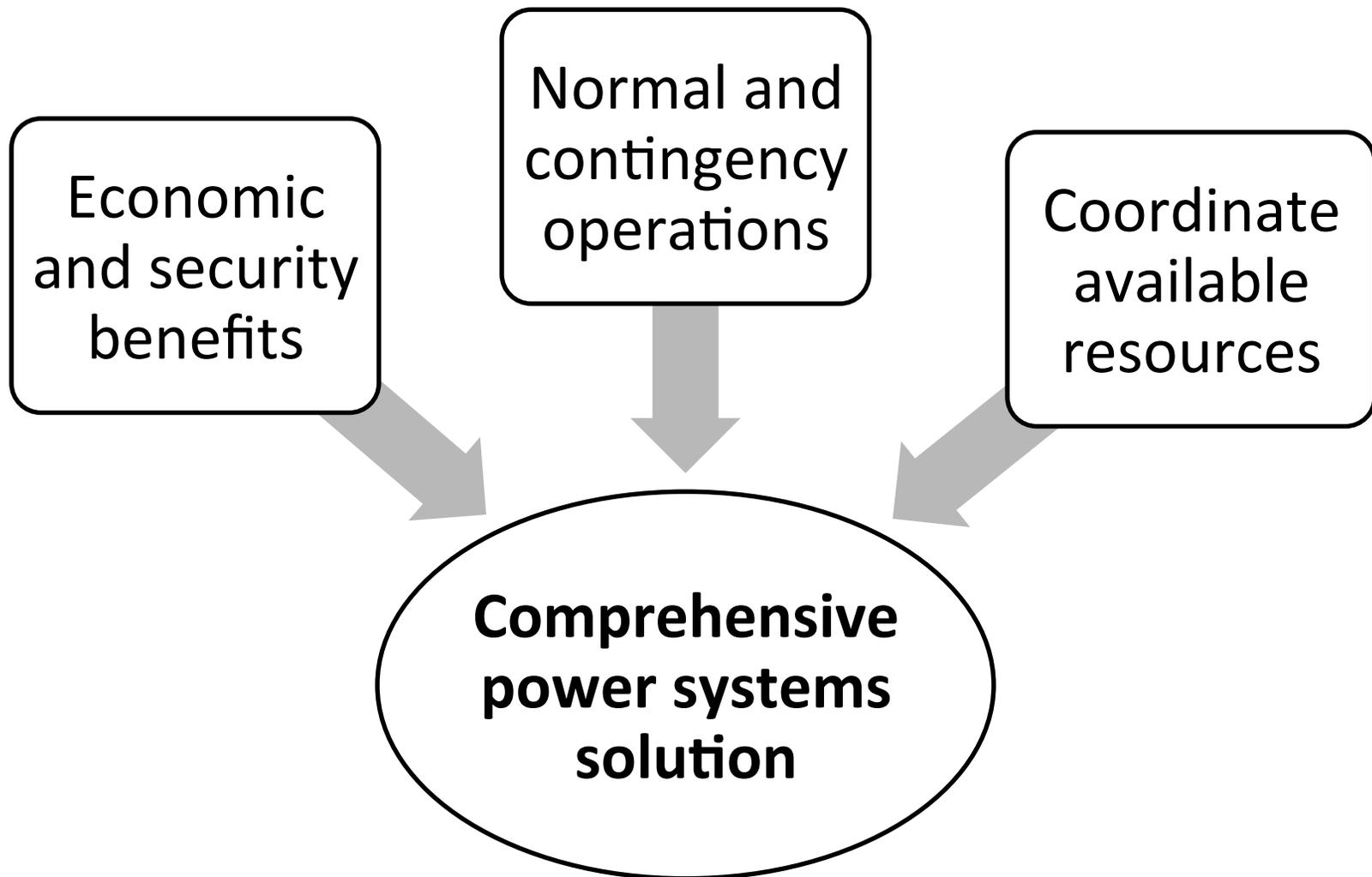


*Increased  
system  
complexity*

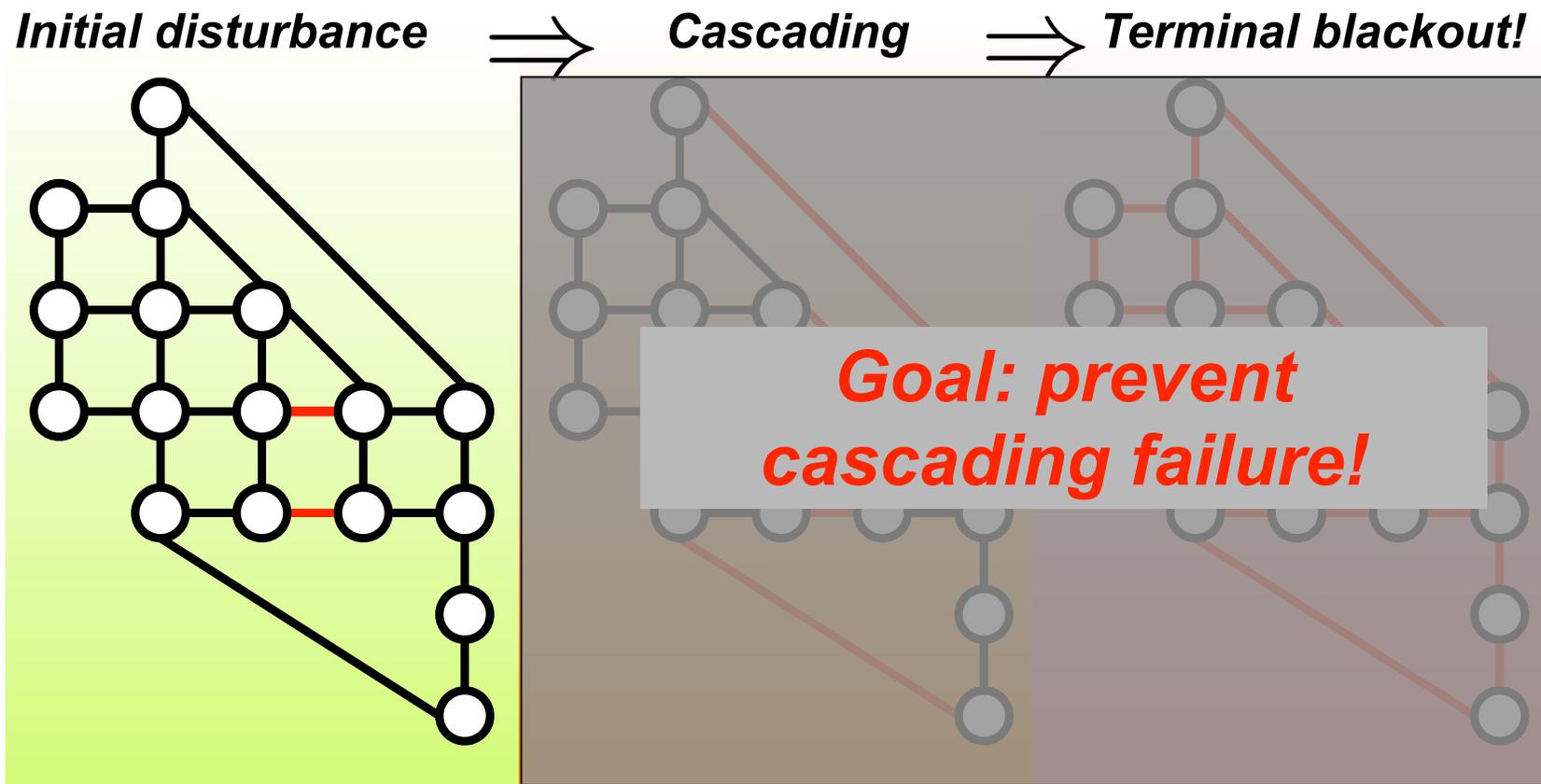


**During unanticipated events, human operators need new tools to aid in decision-making**

# Research Objective

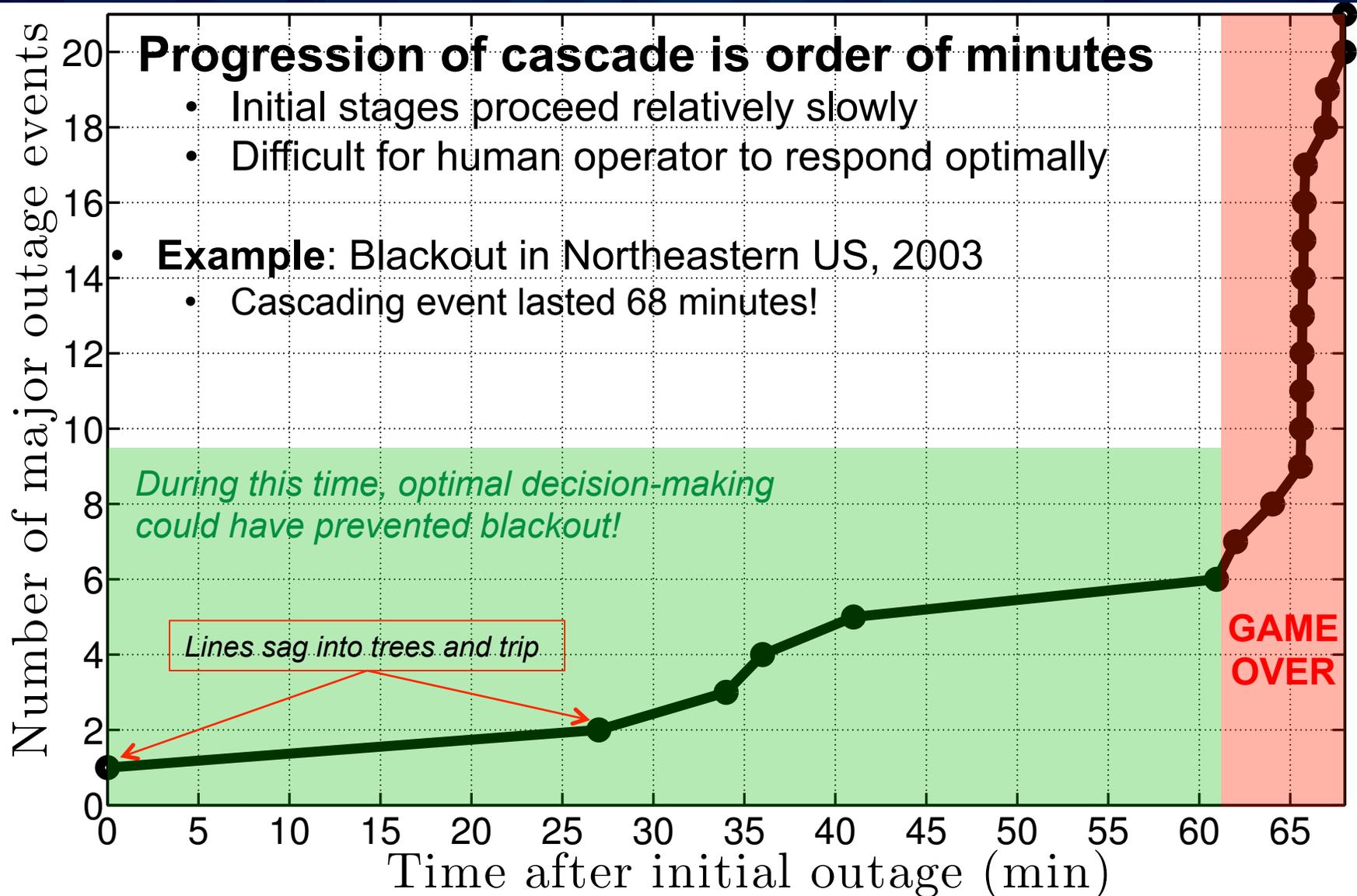


# Cascading failure



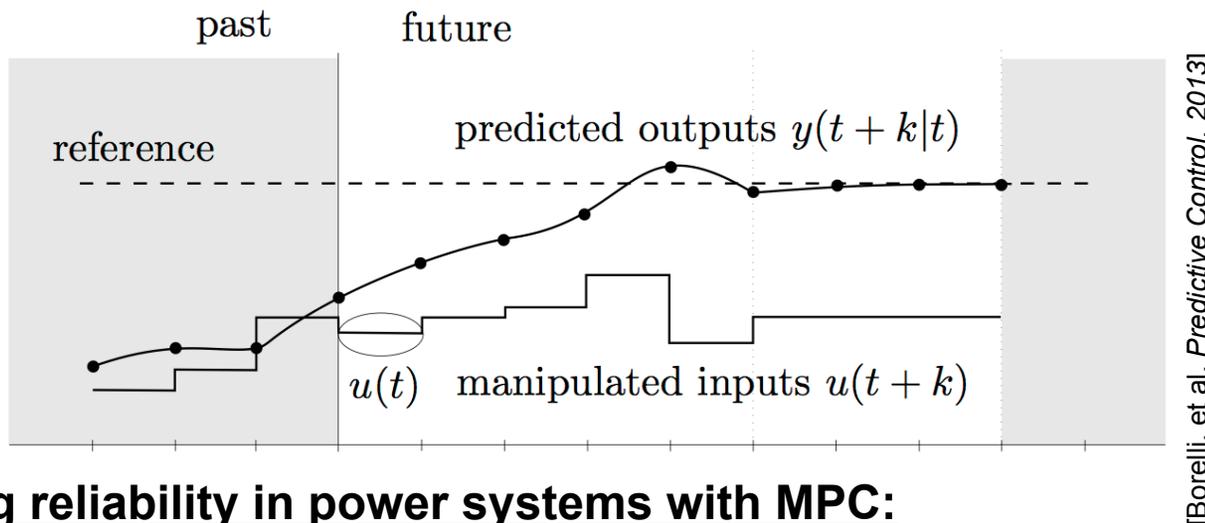
- Cascade is a uncontrolled cycle of flow redistribution, line outages
- Non-trivial to predict and protect against all failures ( $N-k$  schemes)

# Cascading failure



# Cascade Mitigation Approach

- **Power systems suffused with constraints on states/inputs**
  - Gen ramp-rate limits, storage power limits, temperature limits, ...
- Use **model-predictive control (MPC)** scheme to halt cascade
  - Compute optimal control law by solving an optimization problem on-line
  - Computationally expensive: need **simple but sufficient model** ← **hard!**



- **Ensuring reliability in power systems with MPC:**
    - Voltage stability [Larsson 2002, Zima 2003, Hiskens 2004]
    - Static/thermal line overloads [Galiana 2005, Hines 2009, Carneiro 2010]
- **Underestimate line losses**
- **No comprehensive solution. No active role for energy storage.**

# Relevant power system concepts and models

- **Power balance:** for each node,  $i$

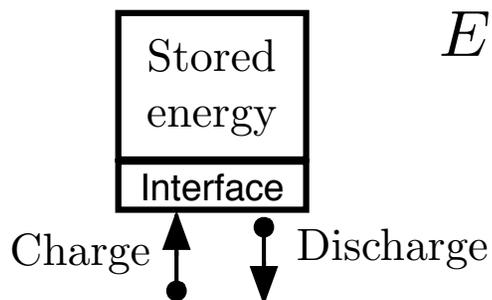
$$\text{Flow out} - \text{flow in} = \text{produced} - \text{consumed}$$

- **Power flow:** for each line,  $(i, j)$

- Models the underlying physics of an AC power network
- Common models: *nonlinear* AC vs. simplified *linear* “DC” models
- “DC” assumes fixed voltage magnitudes, no reactive power, no losses

$$\text{“DC” Power Flow: } f_{ij}^{DC}[k] = \frac{\theta_{ij}[k]}{x_{ij}}$$

- **Energy storage model:** an simple first-order model

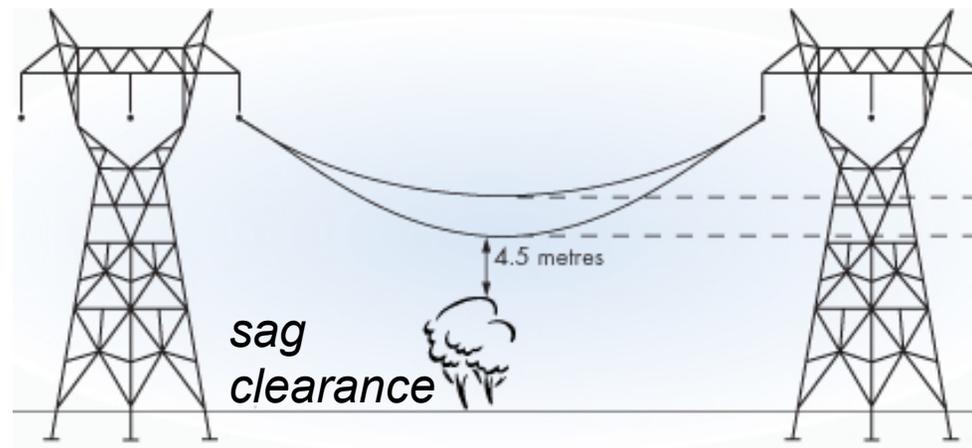


$$E[k + 1] = E[k] + \eta_{ch} f_{ch}[k] + \frac{1}{\eta_{dis}} f_{dis}[k]$$

$$0 = f_{ch}[k] f_{dis}[k]$$

# Relevant power system concepts and models

Transmission lines are characterized by **static power ratings**  
*Power rating* → *Current rating* → *Temp limit* → *sag clearance*



## IEEE Standard 738: conductor temperature model

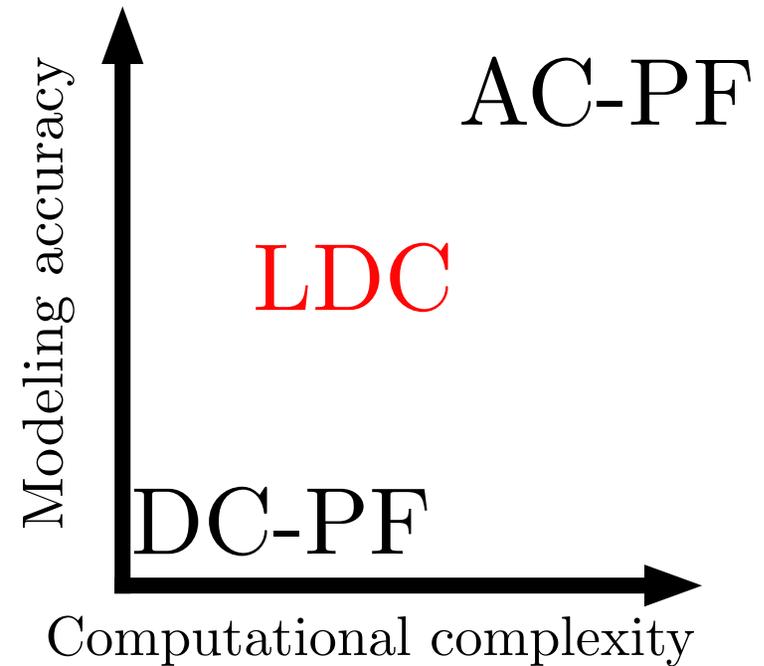
$$\dot{T}(t) = \frac{1}{mC_p} \left( \underset{\text{solar heat gain}}{q_s(t)} + \underset{\text{convection heat loss}}{f^{loss}(t)} - \underset{\text{radiated heat loss}}{q_c(t, T(t))} - q_r(t, T(t)^4) \right)$$

To reduce temperature, must alleviate  **$I^2R$  (ohmic) losses** subject to power flows and nominal demand and other constraints

# Relevant power system concepts and models

- **Main Technical Challenge**

- ☑ Optimally alleviate line temperature overloads
- ☑ AC-PF is accurate but non-convex!
- ☑ DC-PF is linear but not as accurate!
- ☑ Temperature *depends* on  $I^2R$ -loss
- ☐ Need a simple but sufficient model

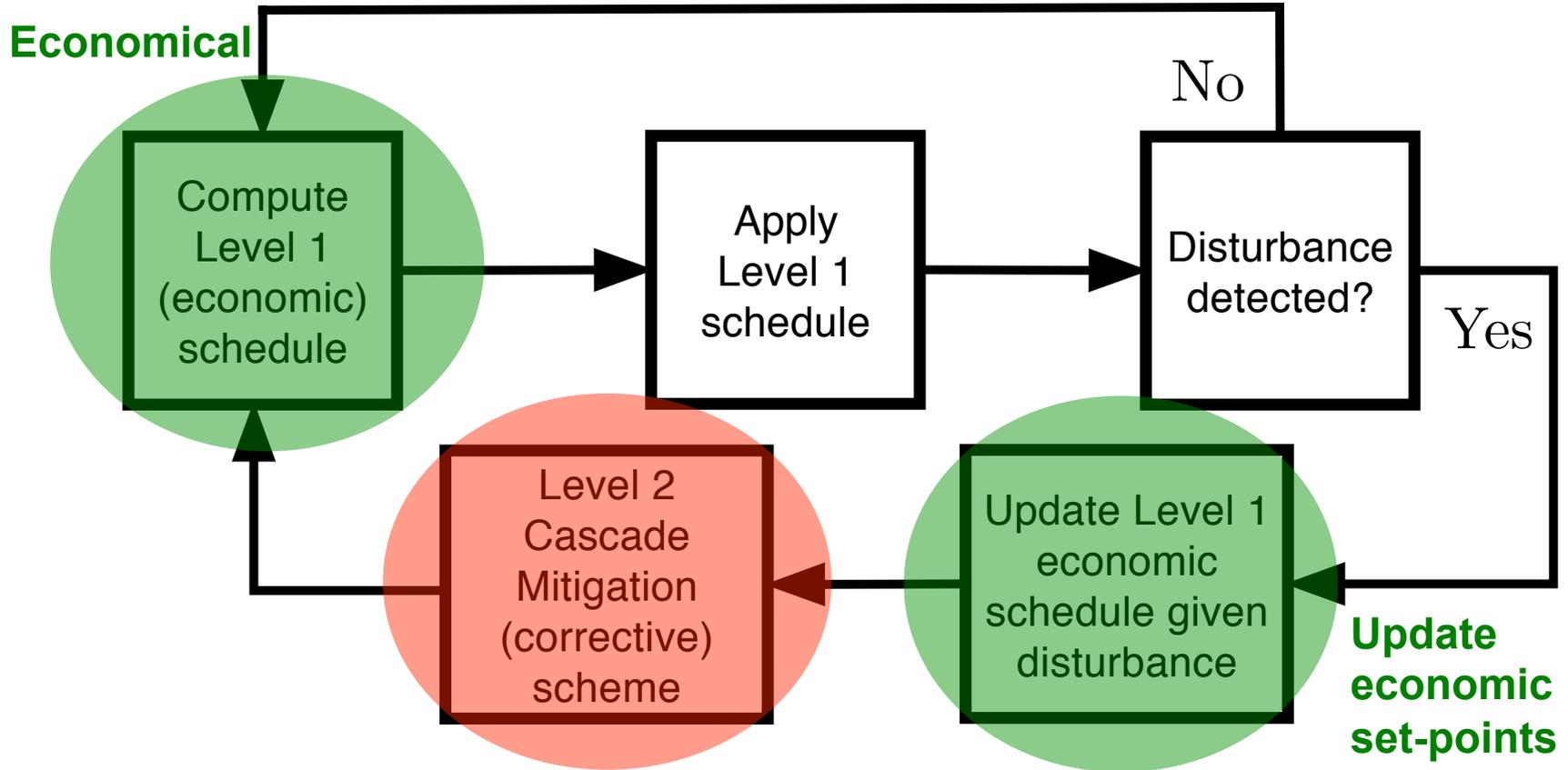


- **Need for compromise: “lossy DC power flow” (LDC)**

- *Intuitive*: line losses are given by

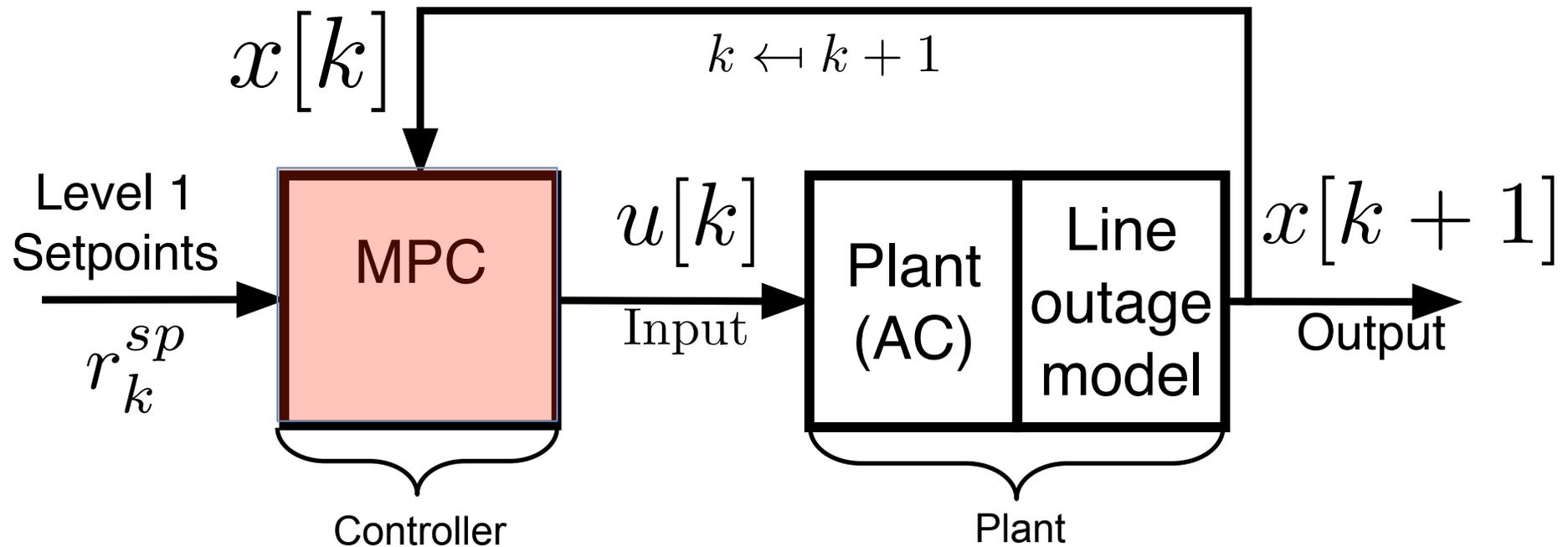
$$f_{ij}^{loss}[k] \approx (f_{ij}^{DC}[k])^2 R_{ij}$$

# Cascade Mitigation Overview



**MPC-based reliability  
(alleviate line overload)**

## Level 2: Cascade Mitigation Scheme



$x$  : generator power output, storage energy level, line temperature

$u$  : change to generator output, storage dis/charge rate, load control, wind spill

$r$  : economically optimal set points for  $x, u$

# Finite Horizon Open-loop Optimization for MPC

**Minimize**

- *Line temperature overloads*

$$(\max\{0, T_{ij}[k] - T_{ij}^{lim}\})^2$$

- *Deviations from Level 1 set points*

$$(x_m[k] - x_{m,k}^{sp})^2 + (u_n[k] - u_{n,k}^{sp})^2$$

**subject to**

- Discrete dynamical constraints
- Linearized temperature dynamics
  - Energy storage dynamics
  - Generator integrator dynamics
- Algebraic constraints
- *Power balance equation*
  - *DC power flow*
  - *DC line losses*
  - *Storage complementarity condition*
  - *Limits on states and inputs*
  - *Terminal temperature constraint*
  - *Measured/estimated initial state*

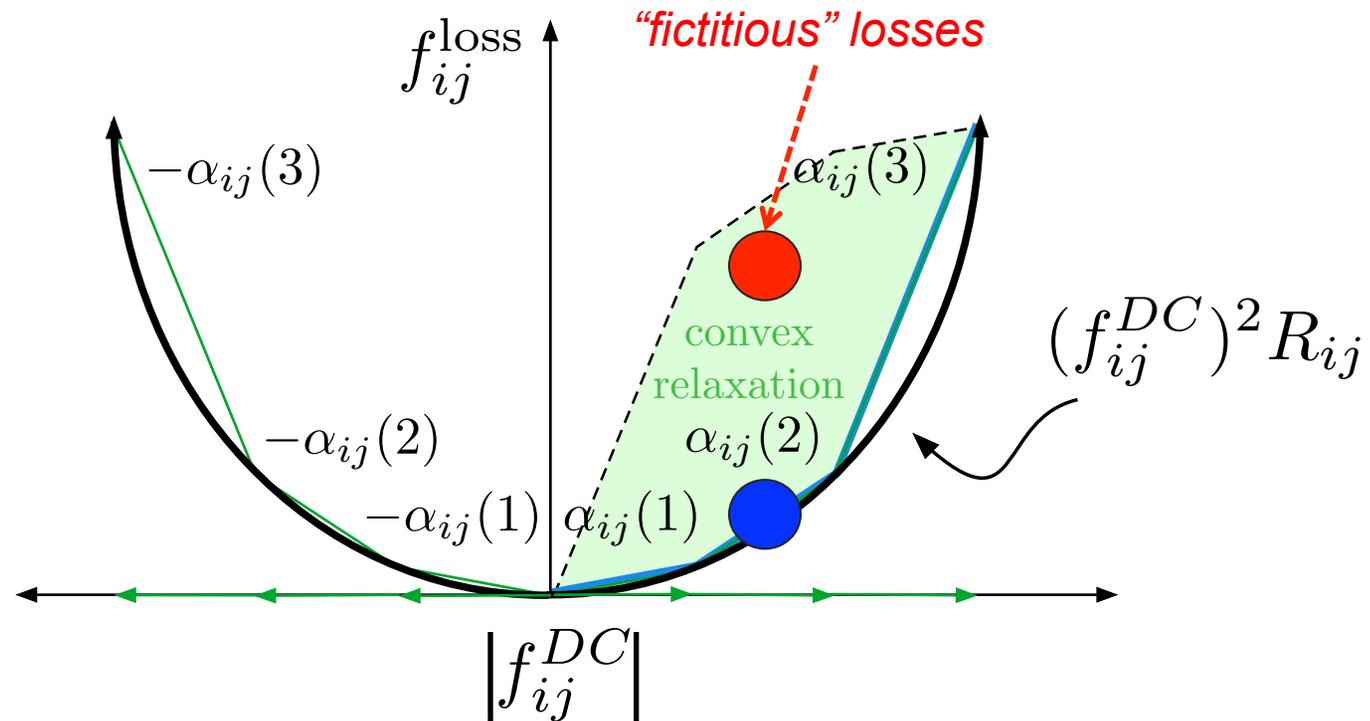
A) Nonlinear non-convex losses

B) Nonlinear complementarity constraint

← *Limits overload magnitude*

# A) Relaxation of Nonlinear Line Loss Constraint

- Overcome non-linearity by relaxing constraint:



**Definition:** The convex relaxation is **locally tight** if losses are exact for a line

# A) Relaxation of Nonlinear Line Loss Constraint

## • **Questions**

- when is relaxation (locally) tight at optimality?
  - Easy: line temperature is overloaded  $\rightarrow$  minimal losses
- when is relaxation **not** (locally) tight?
  - Negative nodal prices? Forced generator ramp-down?
  - Need to consider such conditions...

**Idea:** modify algebraic power balance constraint:

$$\sum_{(i,j) \in \mathcal{N}_i} f_{ij}^{DC}[k] + \frac{1}{2} f_{ij,k}^{loss,est} = f_{gen,i}[k] - f_{load,i}[k]$$

***In controller, use fixed estimate of losses based on last AC measurement***

Effectively decouples temperature from network topology and states

# A) Relaxation of Nonlinear Line Loss Constraint

## ***Theorem for predicted line losses:***

If  $T_{ij}[k + 1] > T_{ij}^{lim} \Rightarrow f_{ij}^{loss}[l]$  is locally tight for all  $l \leq k$

*Proof follows from KKT conditions*

## **Reflecting on the convex relaxation:**

- Theorem enables MPC to alleviate temperature overloads
- ***Independent of topology, negative LMPs, etc.***

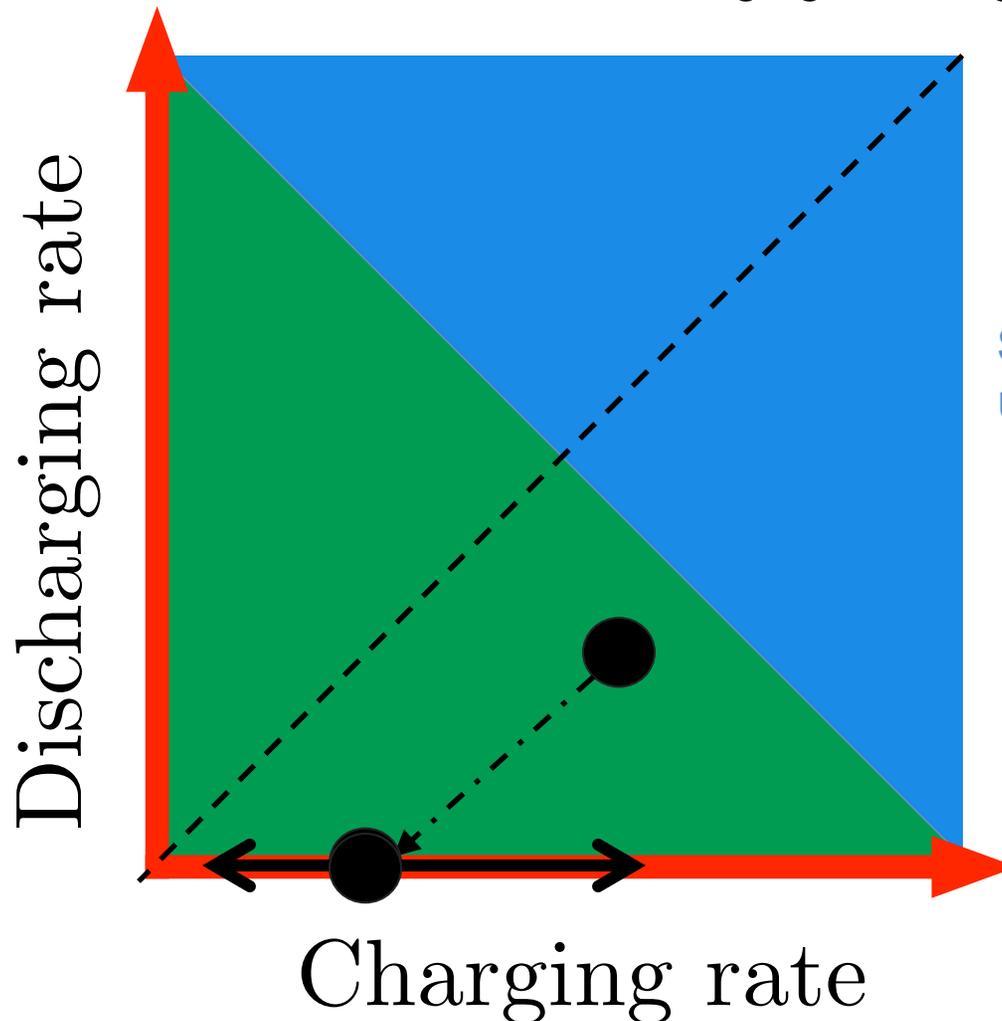
## **“Price” of fixed estimate of losses**

- Creates power mismatch between model and actual system
  - Generators and storage are scheduled against mismatch
  - Mismatch is negligible and rejected through feedback

## B) Relaxation of complementarity constraint

Complementarity condition is not convex → want something simple

*But, simultaneous charging/discharging allows storage to waste energy*



$$0 = f_{ch}[k] f_{dis}[k]$$

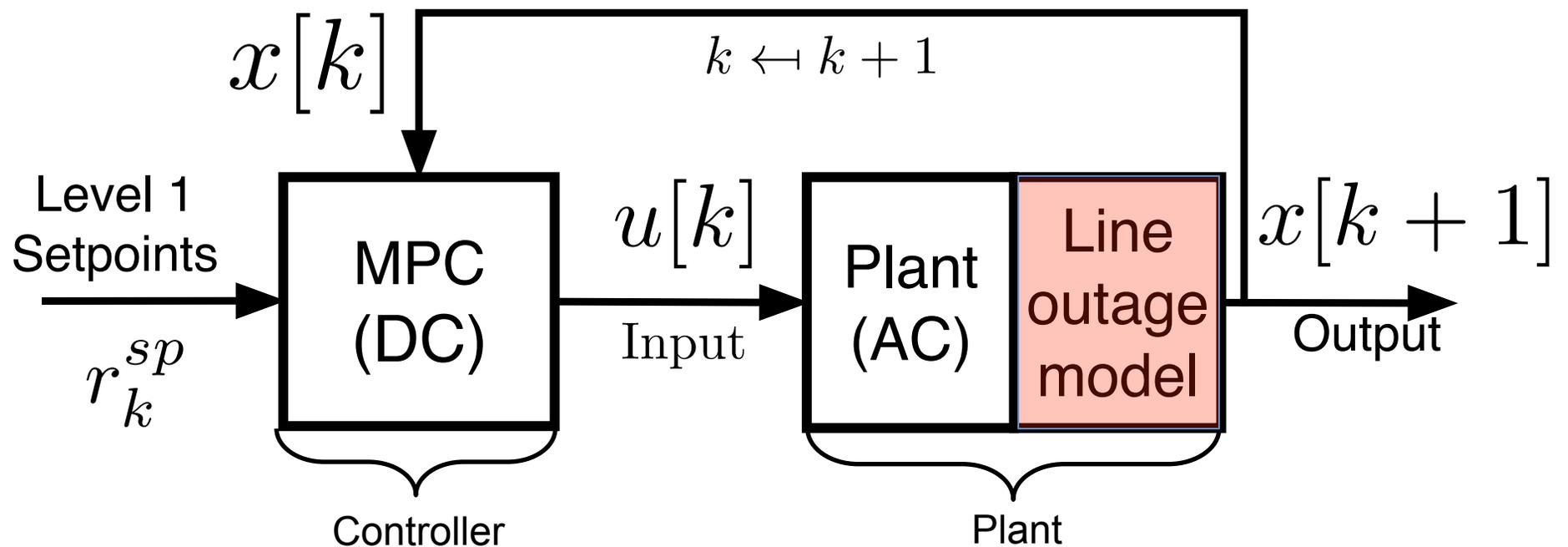
$$0 \gtrless f_{ch}[k] f_{dis}[k]$$

Simulcharge models can significantly underestimate the state-of-charge

### Proposed Heuristic

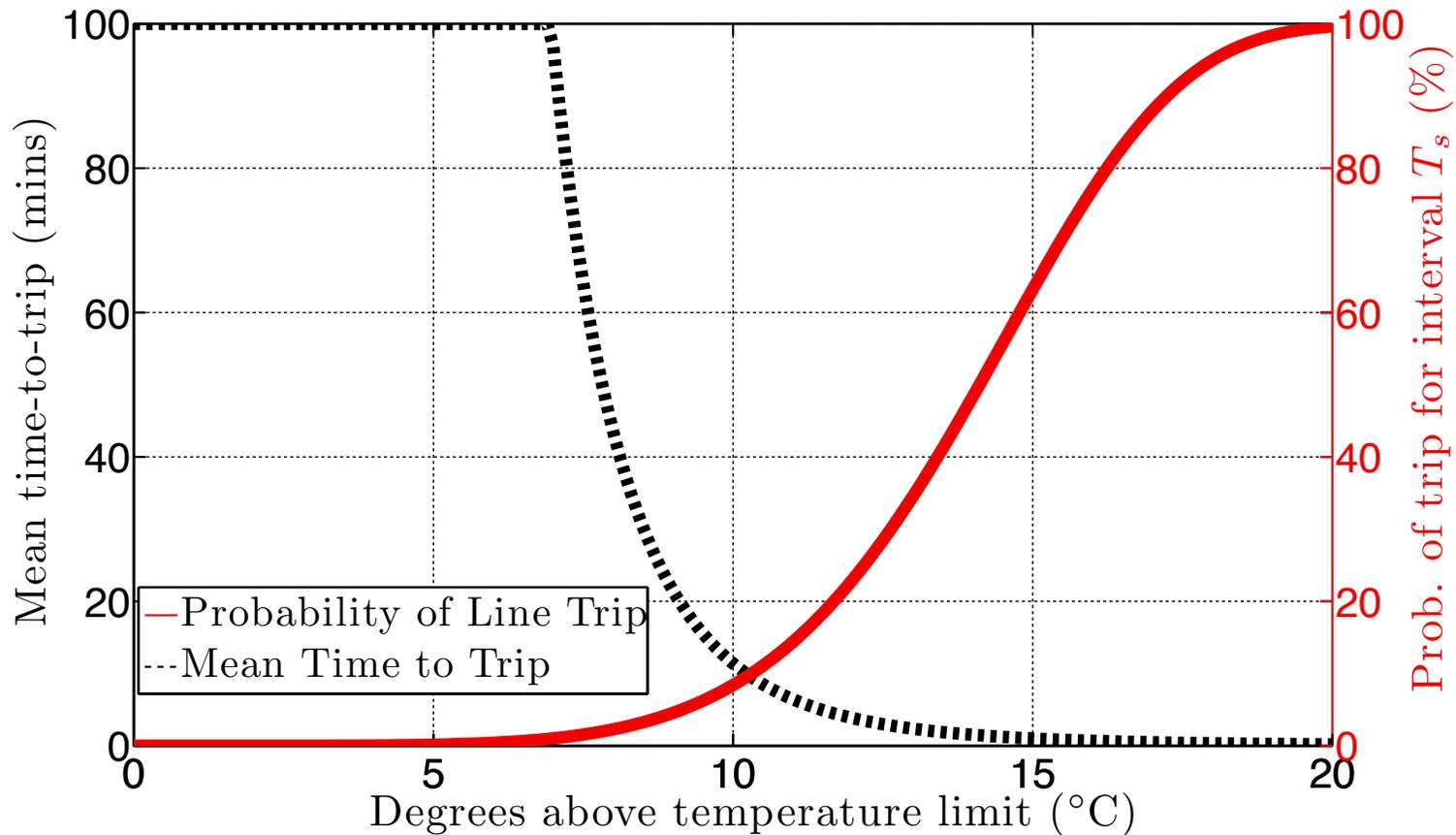
1. Directly limit simulcharge effect
  - a. Add constraint to MPC:
$$f_{ch}[k] + f_{dis}[k] \leq \overline{f_E}$$
2. Only selectively allow simulcharge
  - a. When MPC is initializing (1<sup>st</sup> run)
  - b. When switching storage state
3. Enforce complementarity based on ***previous*** MPC trajectory

# MPC Cascade Mitigation



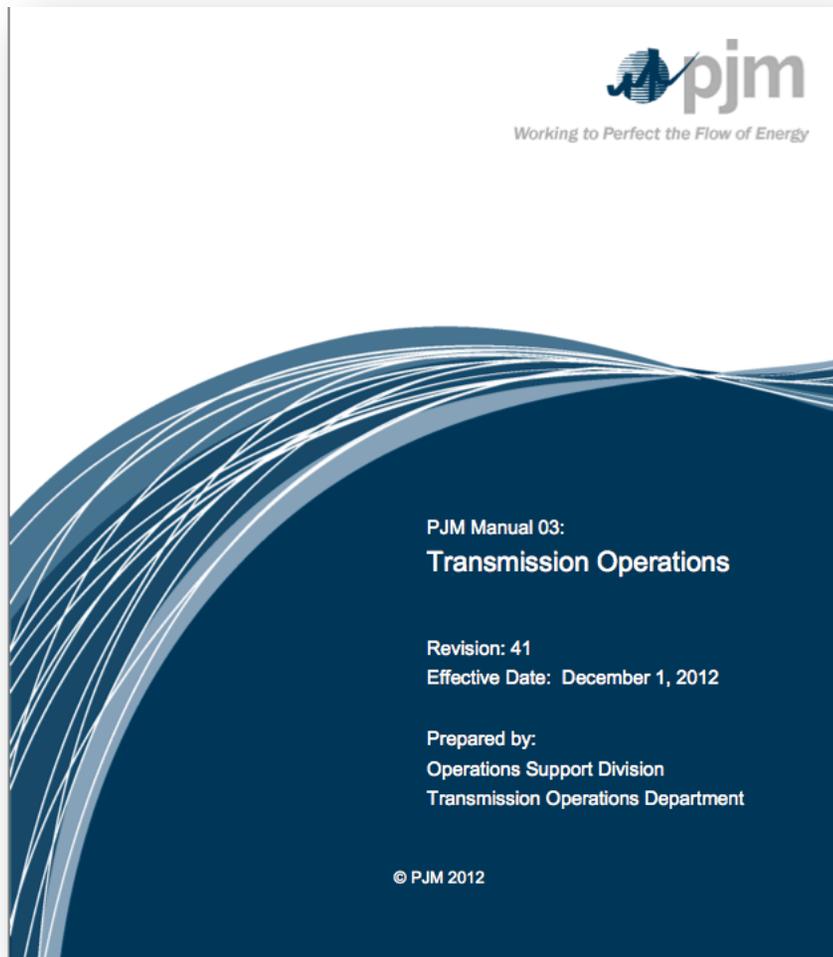
# Line outage model

- Line-tripping based on temperature conditions
  - Large temperature overload  $\rightarrow$  decreased mean time-to-trip



*Based on short-term emergency line rating = sustain 25% overload for 15 minutes*

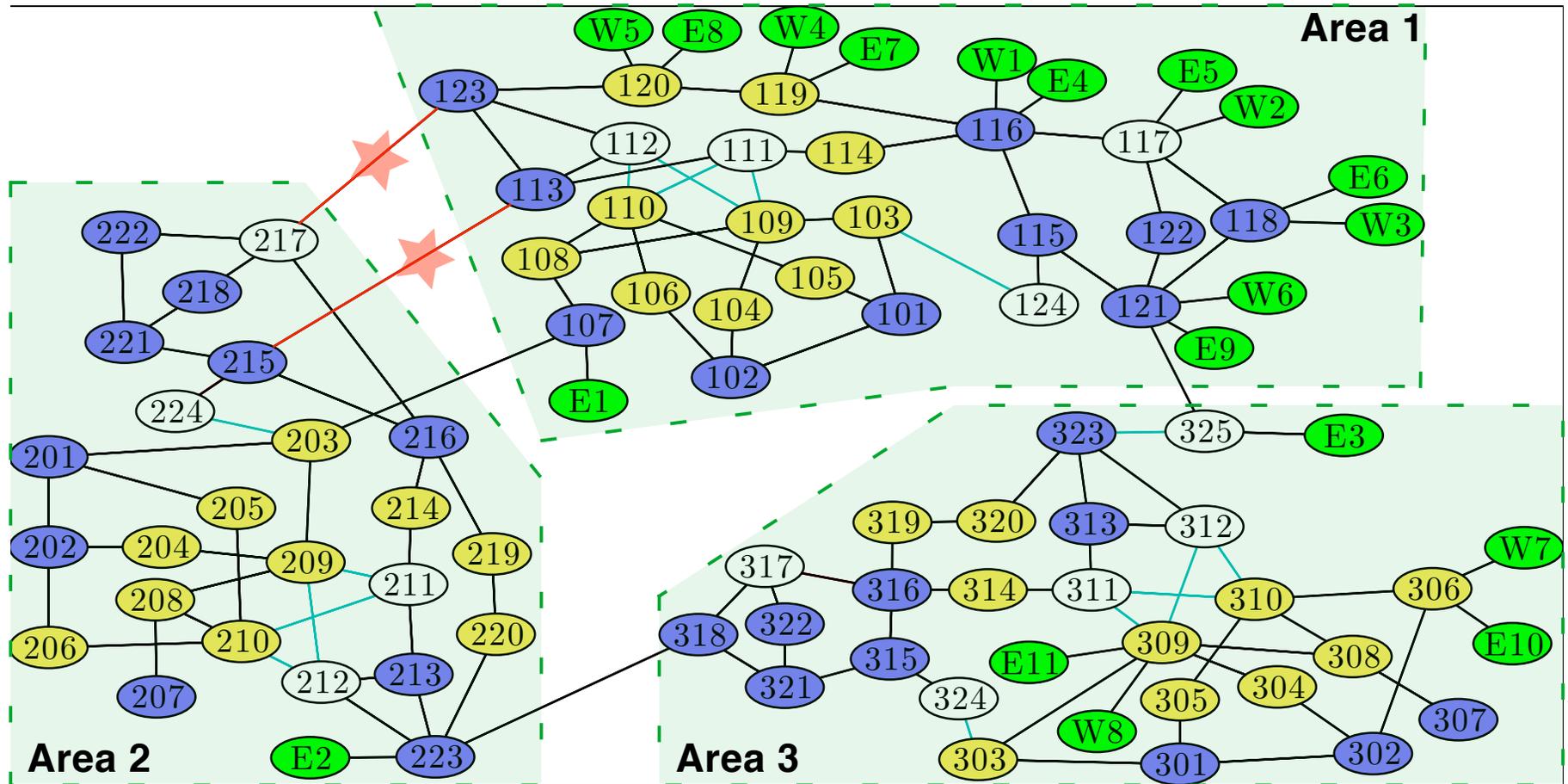
# Defining a base-case for comparison



- Based on PJM transmission operator manual
- Focus on power overloads
- Akin to 1-step MPC
- Penalize load control severely
- No control of energy storage

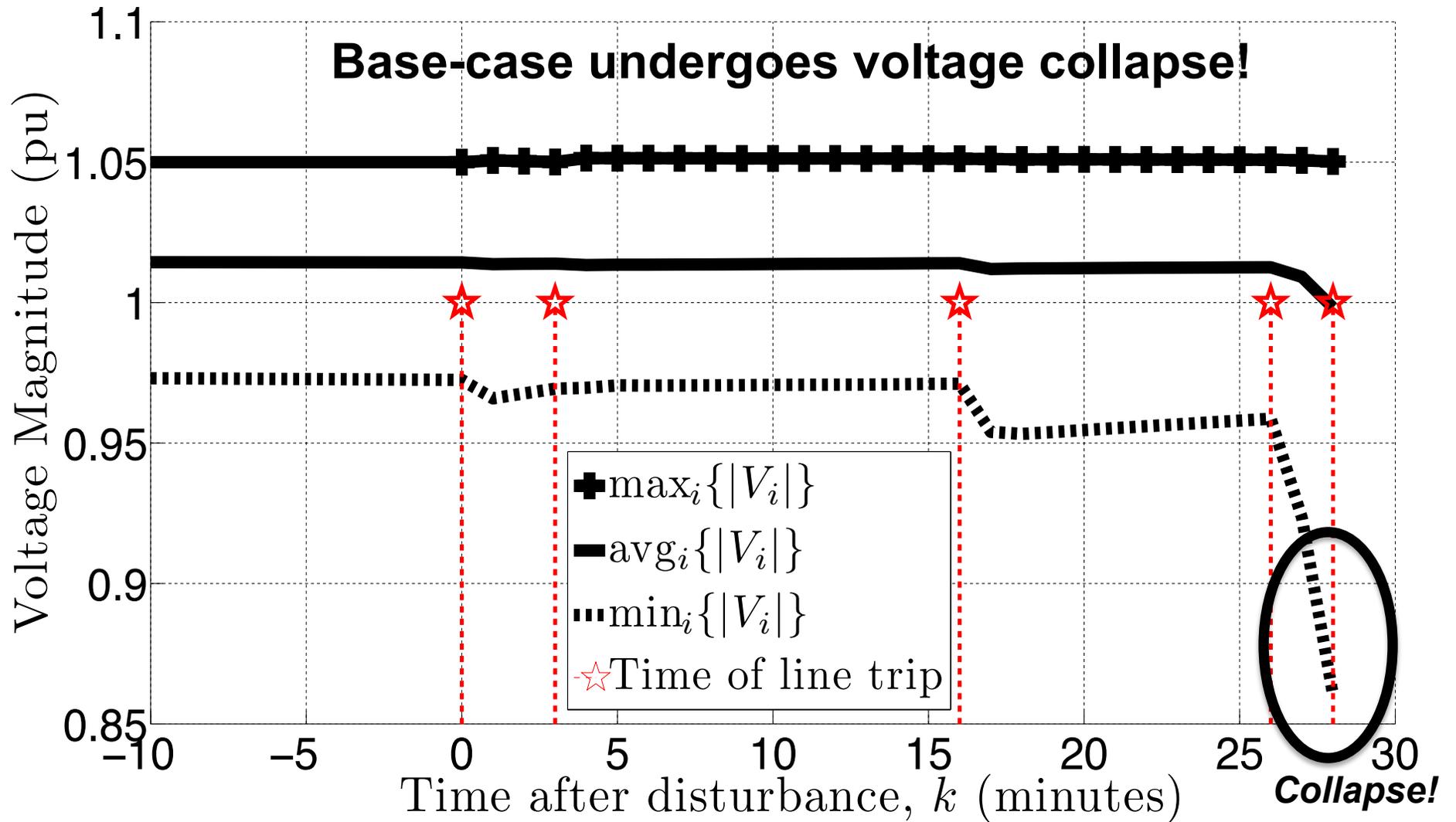
*Warning! It's a simple but crude model of human operator!*

# The IEEE Reliability Test System

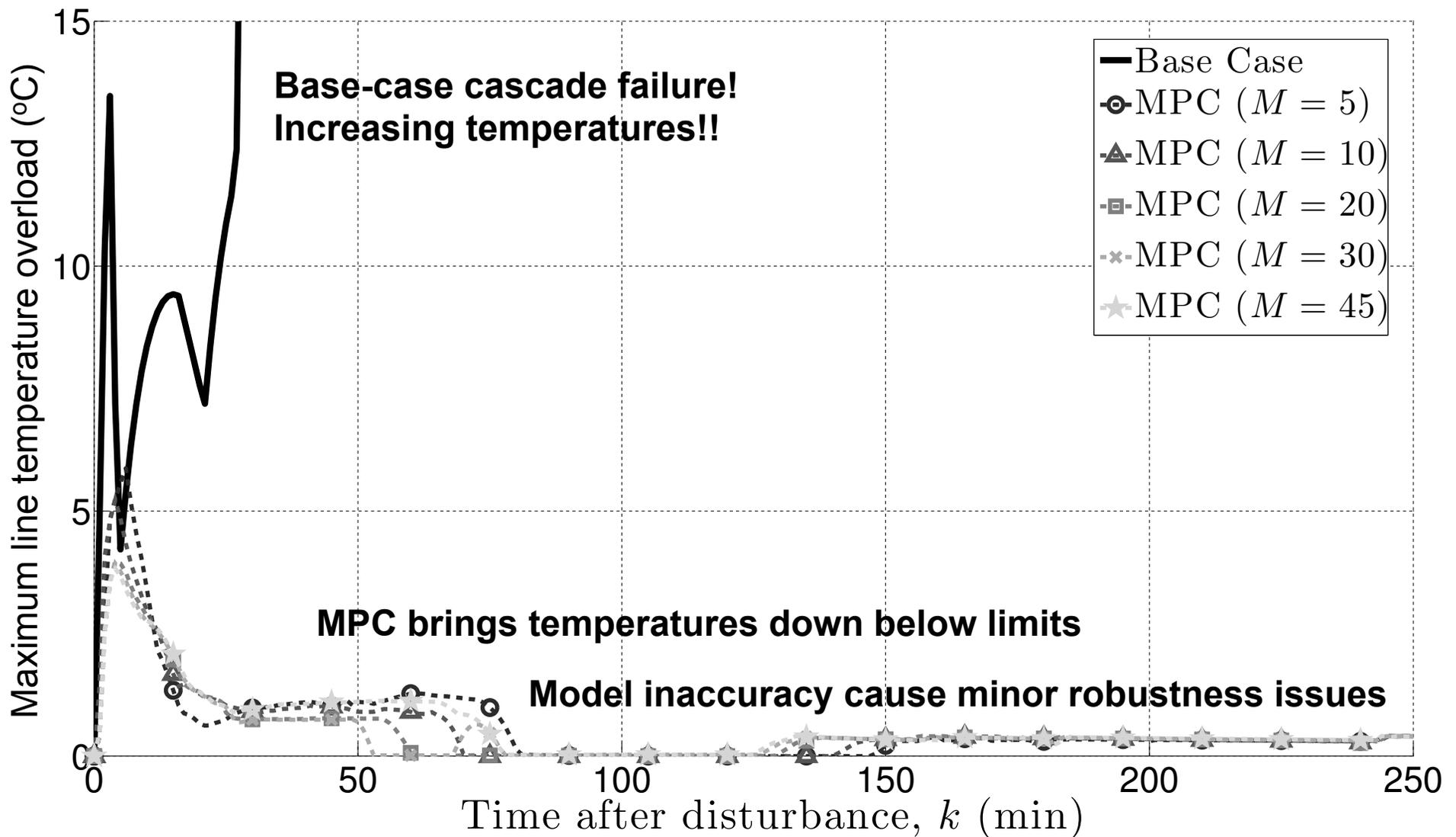


- Load
- Generator
- Storage/Wind injections
- Zero-injection
- Disturbance/outage
- Transmission branch
- Transformer branch

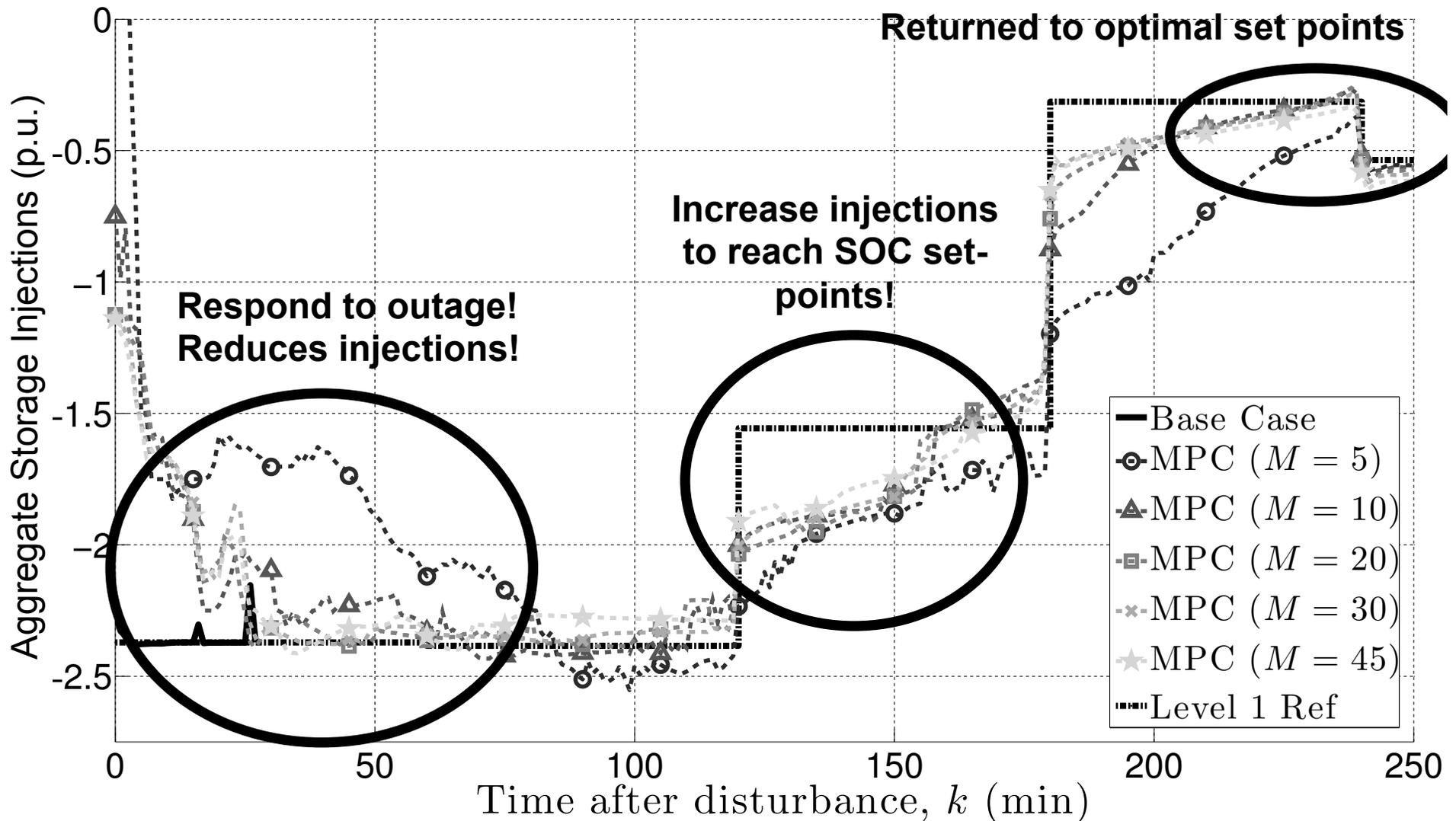
# Base-case performance



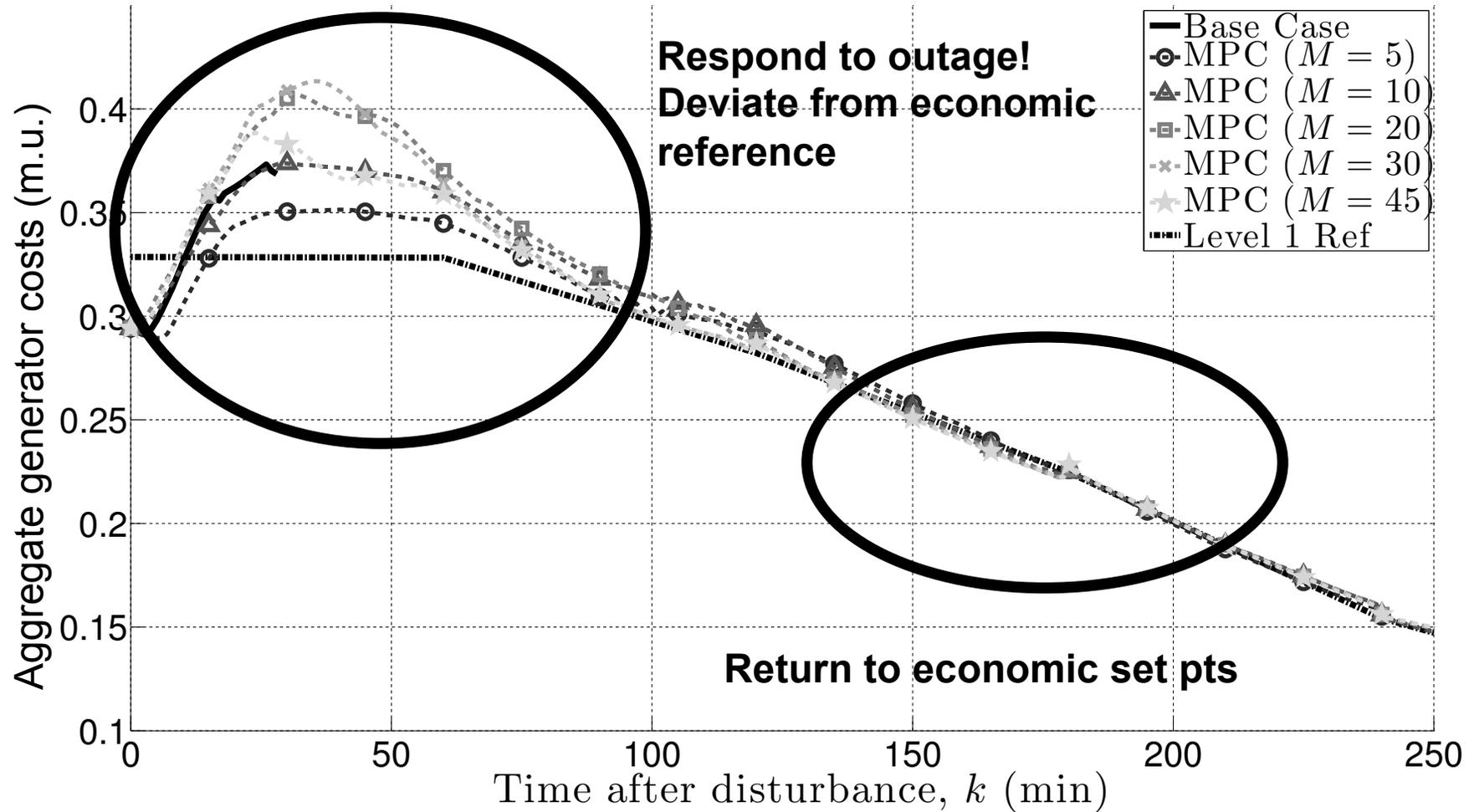
# Case-study on IEEE Reliability Test System



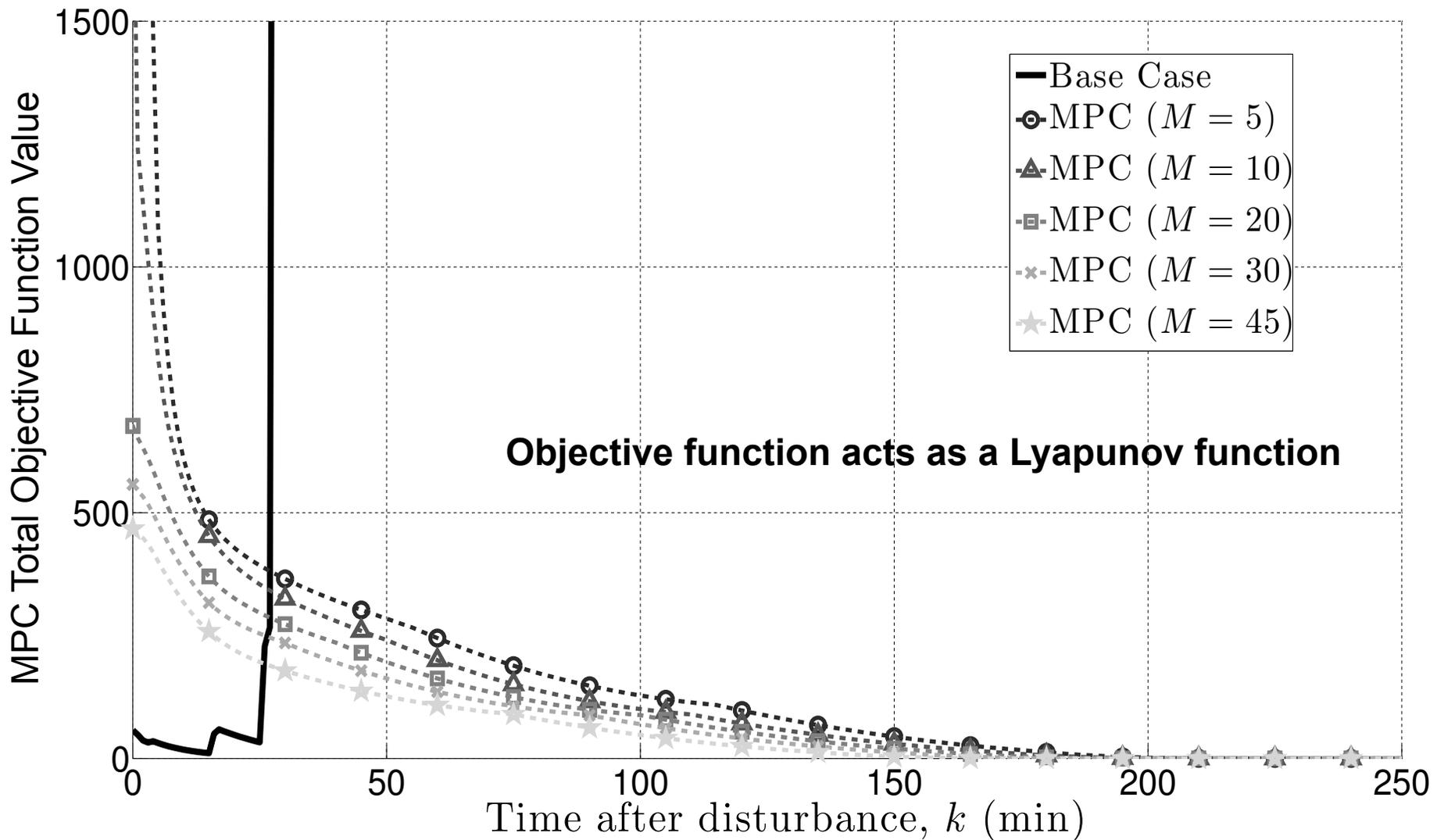
# Case-study on IEEE Reliability Test System



# Case-study on IEEE Reliability Test System



# Case-study on IEEE Reliability Test System



# Immediate next steps...

- **Proof of stability for MPC-scheme is not straightforward**
  - Convex relaxations create non-uniqueness in DAE formulation
  - Hierarchical control scheme (Level 1+2) requires consideration
    - R. Scattolini, “Architectures for distributed and hierarchical Model Predictive Control – A review,” *Journal of Process Control*, vol. 19, pp. 723–731, 2009.
- **Valuable to capture voltage info in linear MPC formulation**
  - Enhances role and value of storage
    - C. Coffrin and P. Van Hentenryck, “A linear programming approximation of AC power flows,” *INFORMS Journal of Computing*. To appear.
- **Investigate robustness of control scheme**
  - MPC performance under different classes of uncertainty
  - Capture risk of failure from overloading lines → Stochastic optimization
- **Improve Base-case model (need operator data)**
- **Consider distributed MPC**

# Thank you!

- FERC organizing committee

- **Collaborators:**

## Team UW

- Prof. Daniel Kirschen (UW)
- Dr. Hrvoje Pandzic (UW)
- Ting Qui (UW)
- Yishen Wang (UW)

## Team UM

- Jennifer Felder (UM)
- Dr. Mengran Xu (UM)

- **Funding:** USDOE, ARPA-E

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# References

- **Relevant publications for details:**

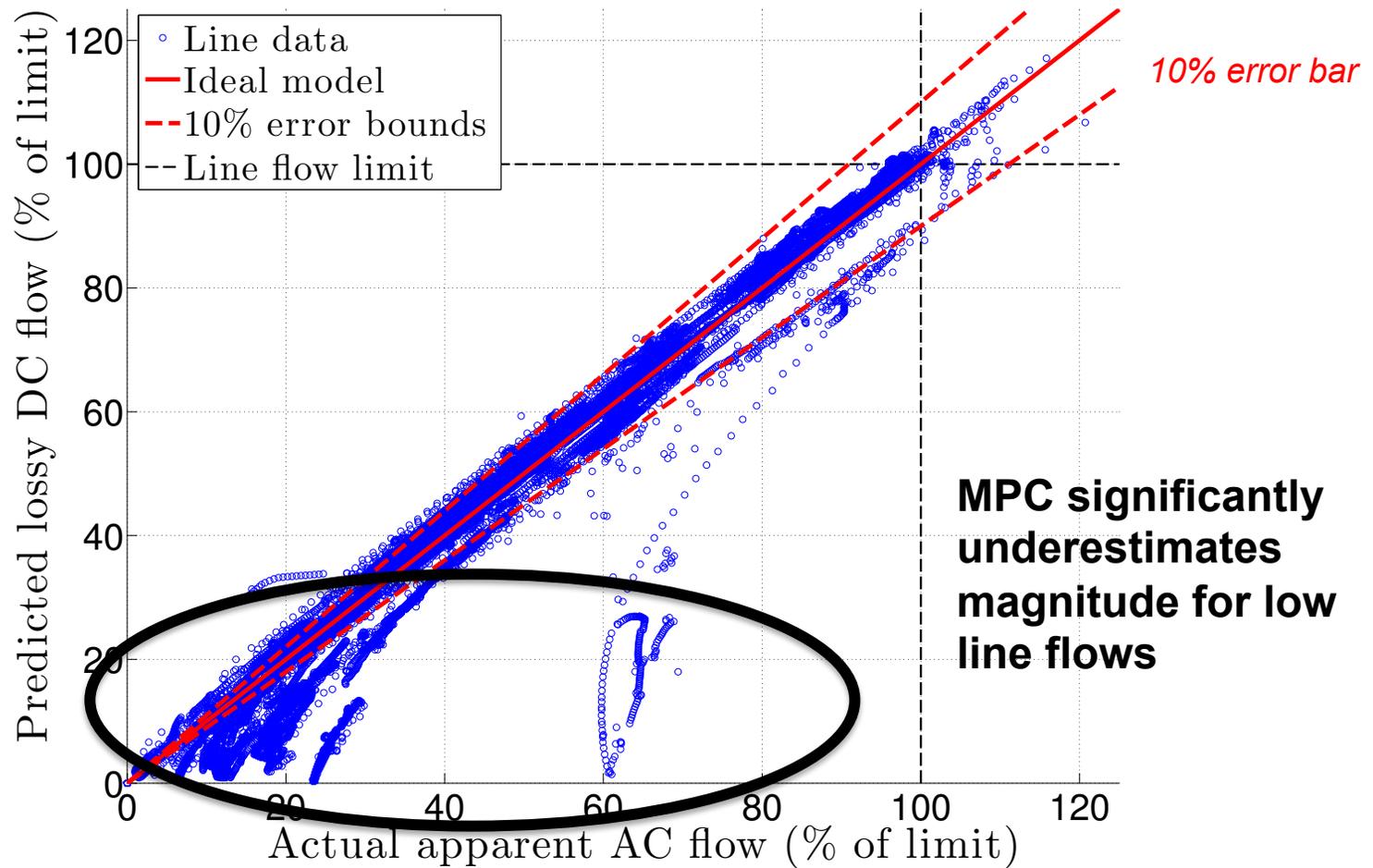
1. **Almassalkhi** and Hiskens, *Optimization Framework for the Analysis of Large-scale Networks of Energy Hubs*, IEEE PSCC '11
2. **Almassalkhi** and Hiskens, *Cascade Mitigation in Energy Hub Network*, IEEE CDC '11 (invited)
3. **Almassalkhi** and Hiskens, *Impact of Storage on Cascade Mitigation in Multi-energy Systems*, IEEE PES '12 (invited)
4. **Almassalkhi** and Hiskens, *Temperature-based Model-Predictive Cascade Mitigation in Electric Power Systems*, IEEE CDC '13 (invited)
5. I. A. Hiskens, D. Kirschen, M. Xue, **M. Almassalkhi**, and J. Felder, "Energy Positioning: Control and Economics - Part 2," *Allerton Conference on Communication, Control, and Computing* (invited), 2013
6. **Almassalkhi** and Hiskens, *Model-Predictive Cascade Mitigation in Electric Power Systems With Storage and Renewables Part I: Theory & Implementation*, IEEE TPWRS (2014)
7. **Almassalkhi** and Hiskens, *Model-Predictive Cascade Mitigation in Electric Power Systems With Storage and Renewables Part II: Case-study*, IEEE TPWRS (2014)



*Extra Content*

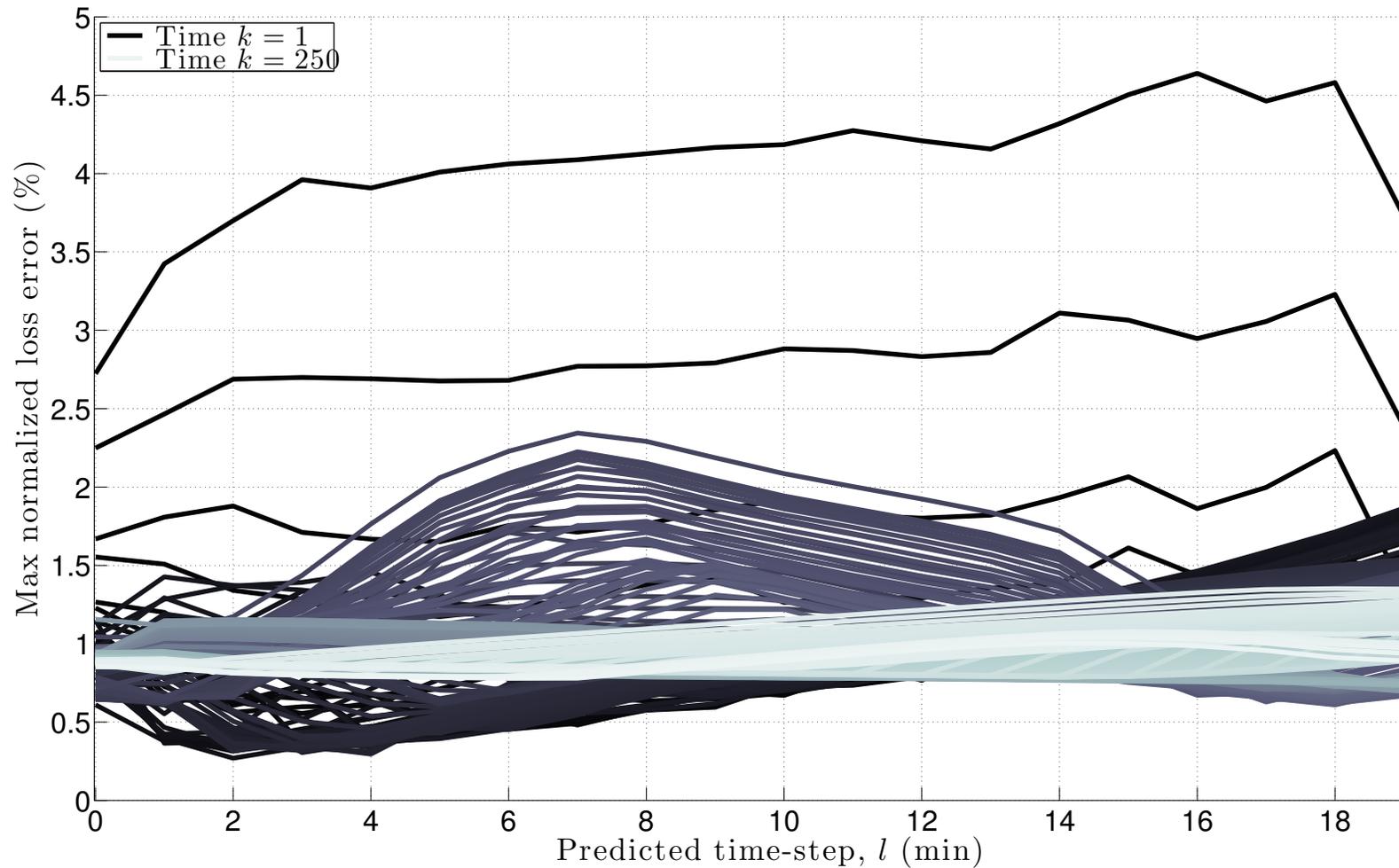
# Simple models and complex systems

## Predicted DC vs. actual AC flow magnitude



# Simple models and complex systems

## Predicted line loss errors from fixed power flow loss term



# Data management & communication

- **Initialization of MPC trajectory requires**
  1. *Conductor temperatures*
    - Thermocouple relays, hard limits, or estimation
    - “Not overly complex for EMS” [Banakar et al. 2005]
  2. *Energy storage state of charge\**
    - Systems today have telemetry for market participation
  3. *Updated network topology\**
  4. *Generation output power and load levels\**
  5. *Operating points of all FACTS devices\**
  6. *Forecasts (demand, renewables, weather) \**
  7. *Minute-by-minute communications\**
    - Slower than current control, market signals

**\*-requirements are consistent with today's operations!**